



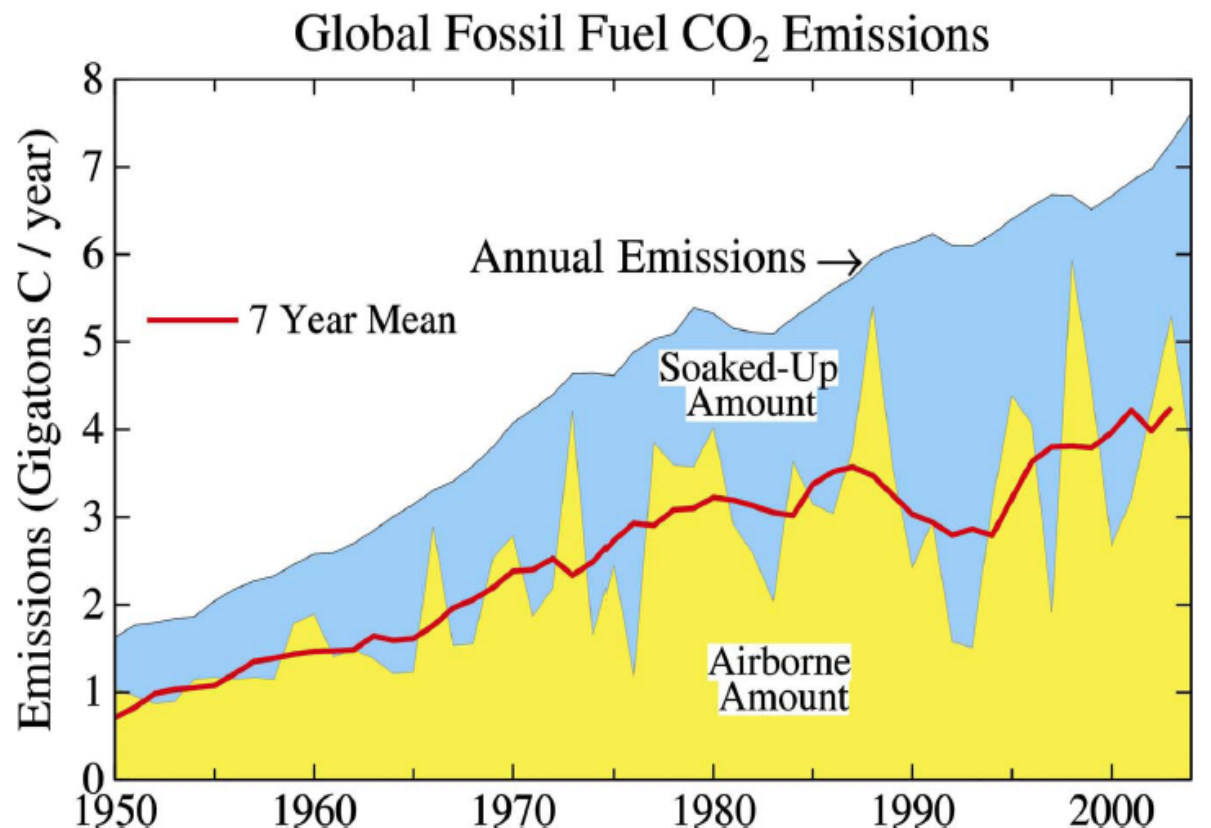
CO₂ and Vertical Mixing

Inez Fung
University of California, Berkeley

Center for Multiscale Modeling of Atmospheric Processes
UC Berkeley, January 11 2011

Holy Grail: Where is the Elusive Carbon Sink?

- Only half of the CO₂ produced by human activities is remaining in the atmosphere
- Where are the *sinks* that are absorbing over 40% of the CO₂ that we emit?
 - Land or ocean?
 - Eurasia/North America?
- Why does CO₂ buildup vary dramatically with nearly uniform emissions?
- How will CO₂ sinks respond to climate change?



Global fossil fuel CO₂ emissions with division into portions that remain airborne or are soaked up by the ocean and land.

Source: Hansen and Sato, *PNAS*, 101, 16109, 2004.

Fate of Anthropogenic CO₂ Emissions (2000-2009)

1.1±0.7 PgC y⁻¹



7.7±0.5 PgC y⁻¹

+



4.1±0.1 PgC y⁻¹

47%

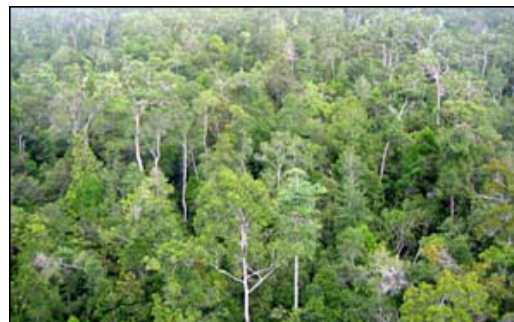
Radiatively active



2.4 PgC y⁻¹

27%

Calculated as the residual of all other flux components



26%

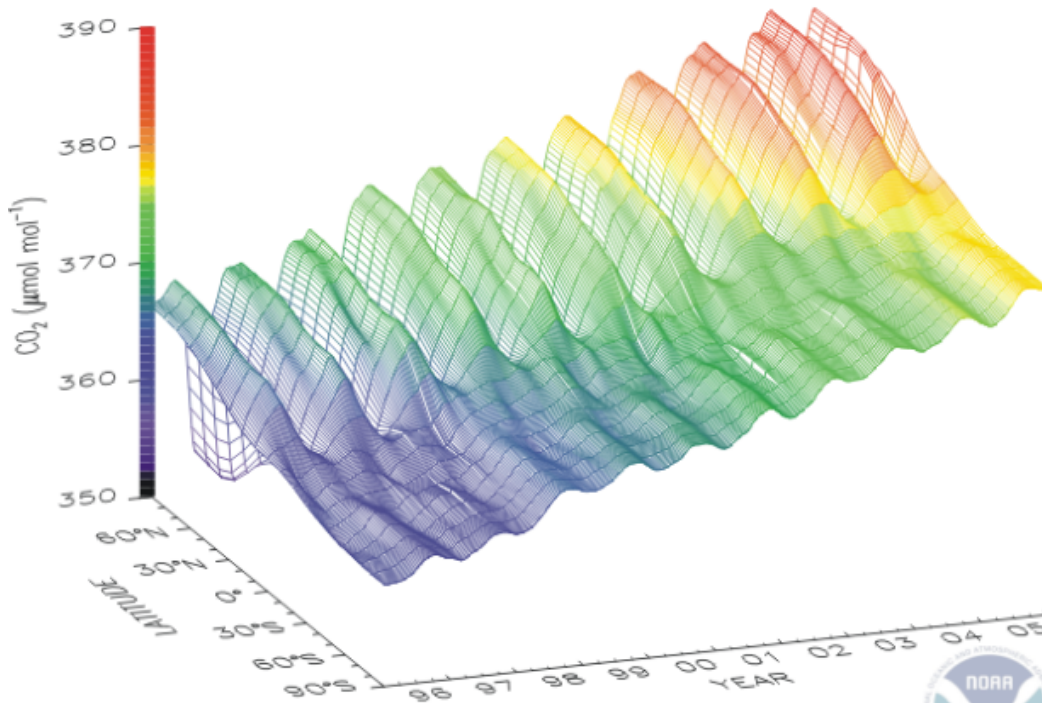
2.3±0.4 PgC y⁻¹

Average of 5 models



CO₂ Distribution in the atmosphere

Global Distribution of Atmospheric Carbon Dioxide
NOAA ESRL GMD Carbon Cycle

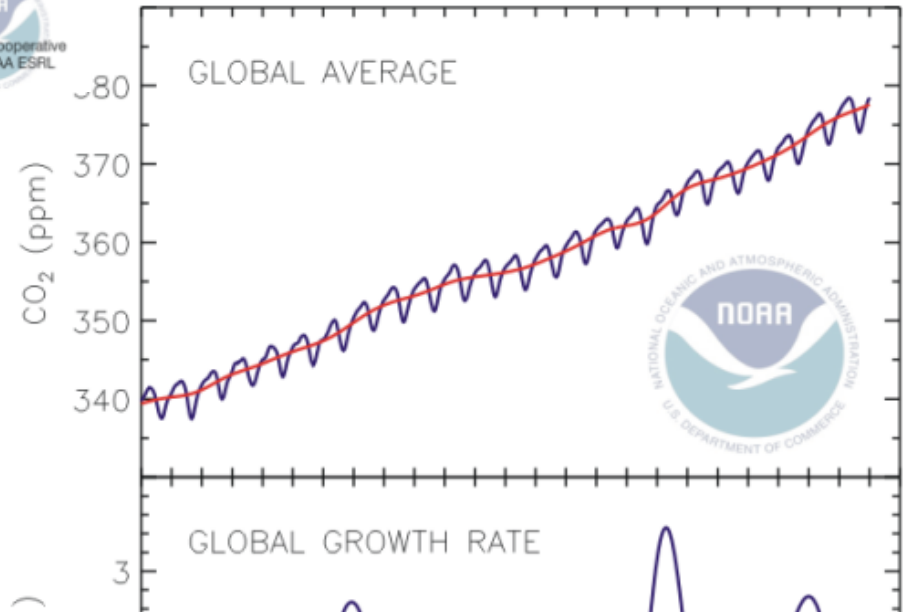


Three dimensional representation of the latitudinal distribution of atmospheric carbon dioxide in the marine boundary layer. Data from the GMD cooperative air sampling network were used. The surface represents data smoothed in time and latitude. Contact: Dr. Pieter Tans and Thomas Conway, NOAA ESRL GMD Carbon Cycle, Boulder, Colorado, (303) 497-6678 (pieter.tans@noaa.gov, <http://www.cmdl.noaa.gov/cogg>).

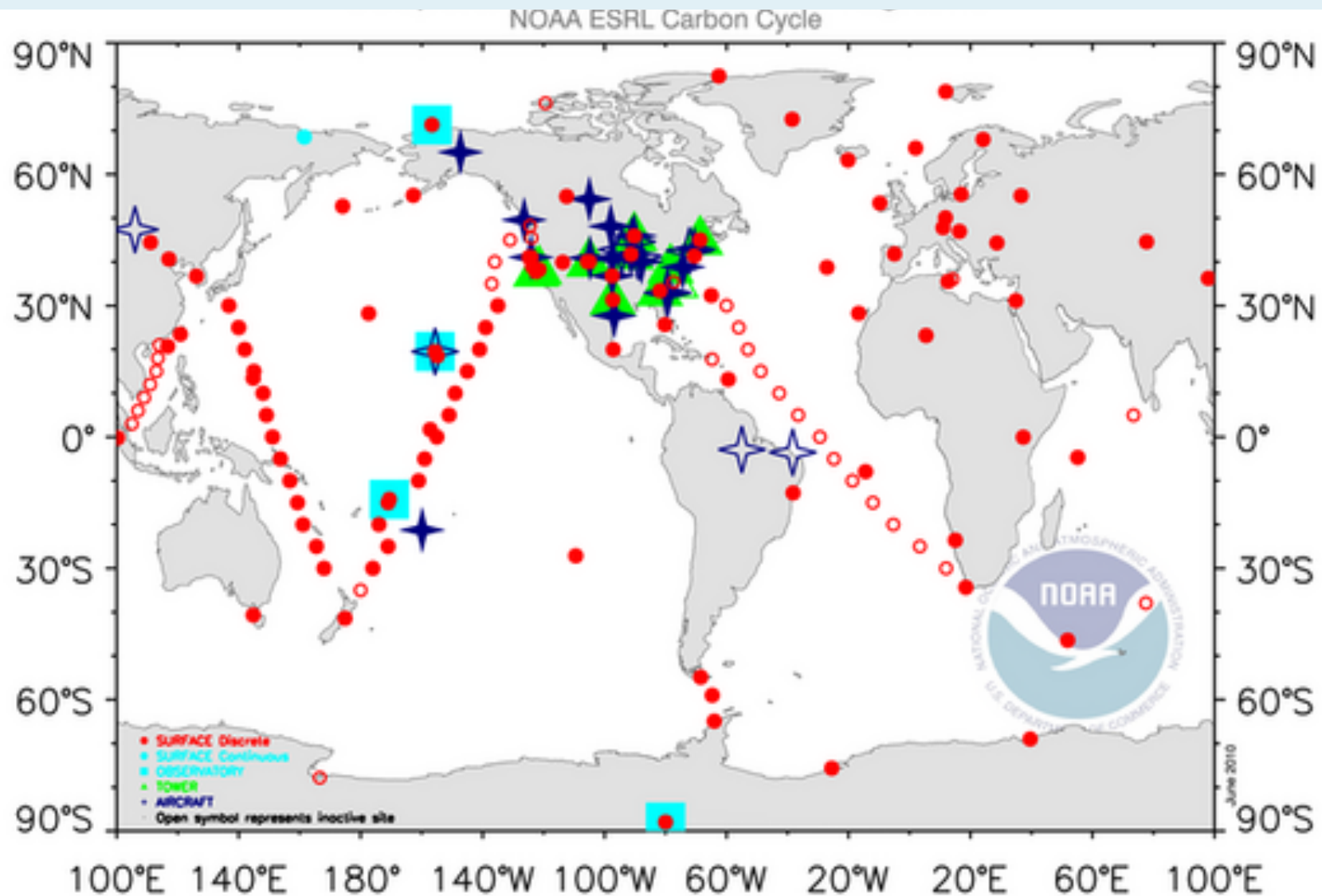
NOAA-ESRL

- ~ 100 sites at remote marine locations, bi-weekly flasks, 2m
- Long-term increase 2-3ppm/yr
- Seasonal cycle ~O(10 ppm)
- N-S gradient ~ 1% of global mean

Carbon Dioxide Measurements
NOAA ESRL GMD Carbon Cycle

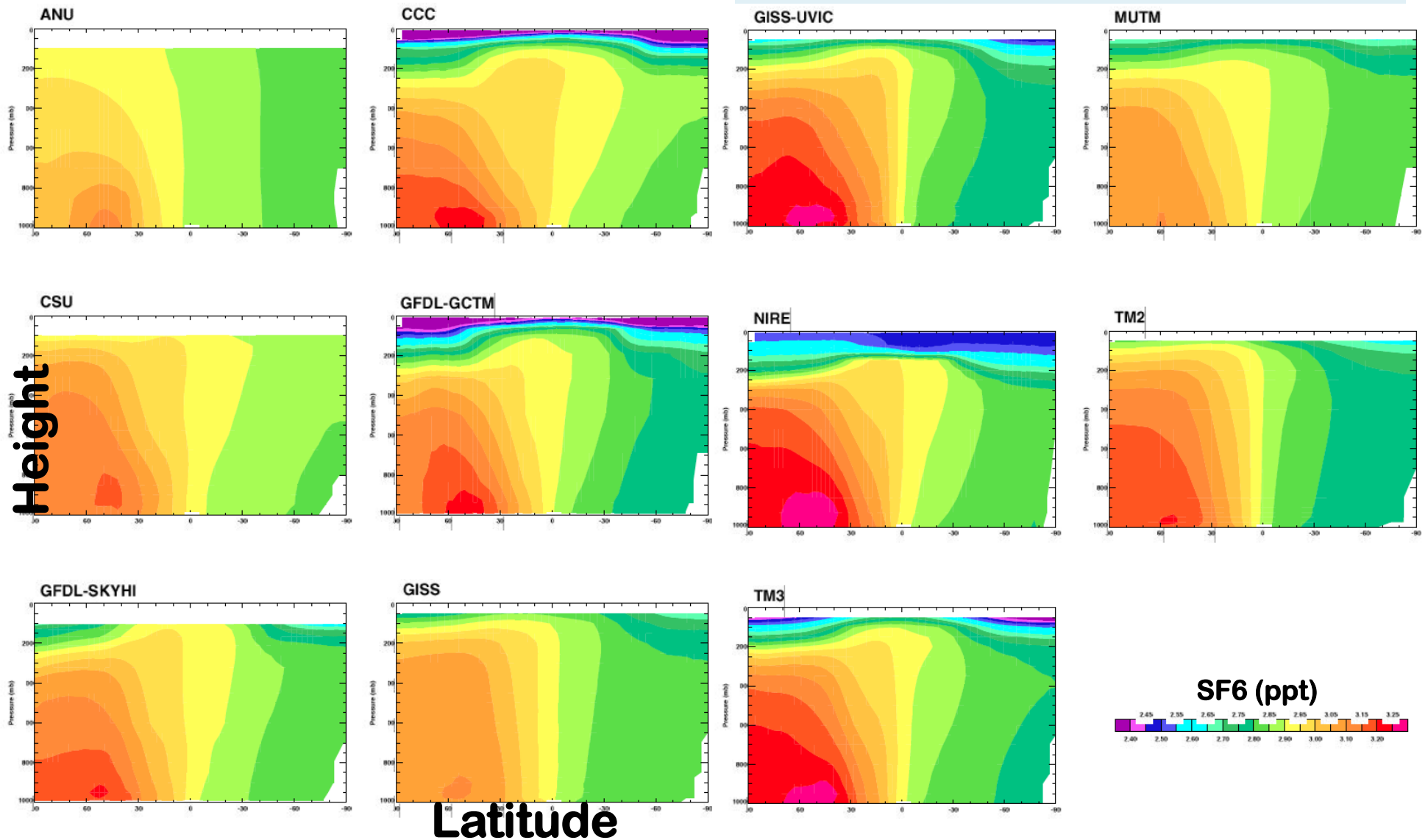


Current sampling in remote marine locations

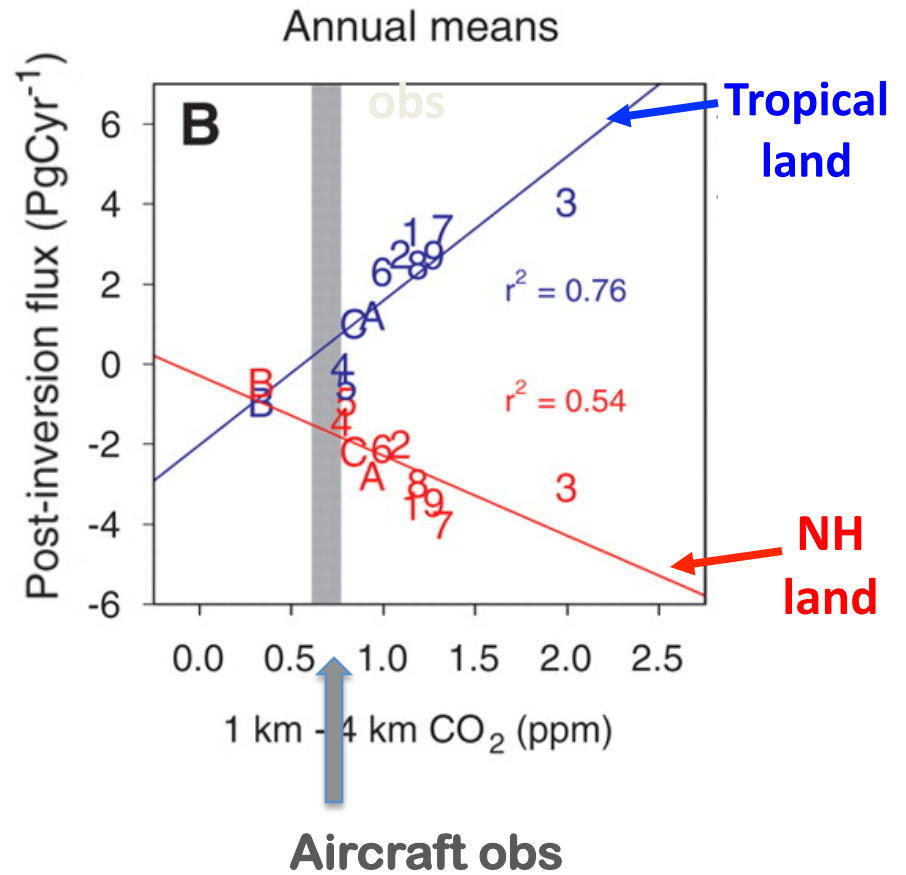
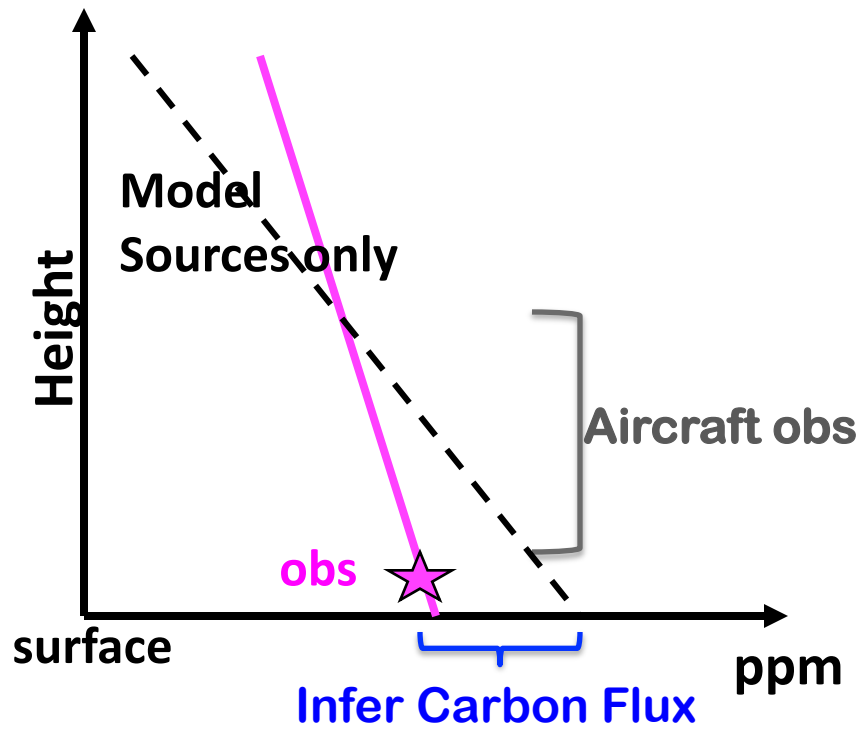


NOAA ESRL Carbon Cycle operates 4 measurement programs. Semi-continuous measurements are made at 4 baseline observatories, a few surface sites and from tall towers. Discrete surface and aircraft samples are measured in Boulder, CO. Presently, atmospheric carbon dioxide, methane, carbon monoxide, hydrogen, nitrous oxide, sulfur hexafluoride, the stable isotopes of carbon dioxide and methane, and halocarbon and volatile organic compounds are measured. Contact: Dr. Pieter Tans, NOAA ESRL Carbon Cycle, Boulder, Colorado, (303) 497-6678, pieter.tans@noaa.gov, <http://www.esrl.noaa.gov/gmd/ccgg/>.

Inert Tracer: NH Industrial Source



CO2 Sink sensitive to CO2 vertical gradient



- Carbon Sink inferred as that required to match the observations;

Underestimate ←

→ Overestimate flux

Stephens et al., 2007, (*Science*)

Ensemble Kalman filter: application to carbon cycle data assimilation

- Assimilate **meteorological** observations together with **satellite and surface CO₂** observations into a carbon-climate model
- Goals:
 - improve representation of carbon processes in carbon-climate model
 - Improve estimation of carbon sources/sinks
 - Articulate uncertainties in carbon sources/sinks due to uncertainties in transport

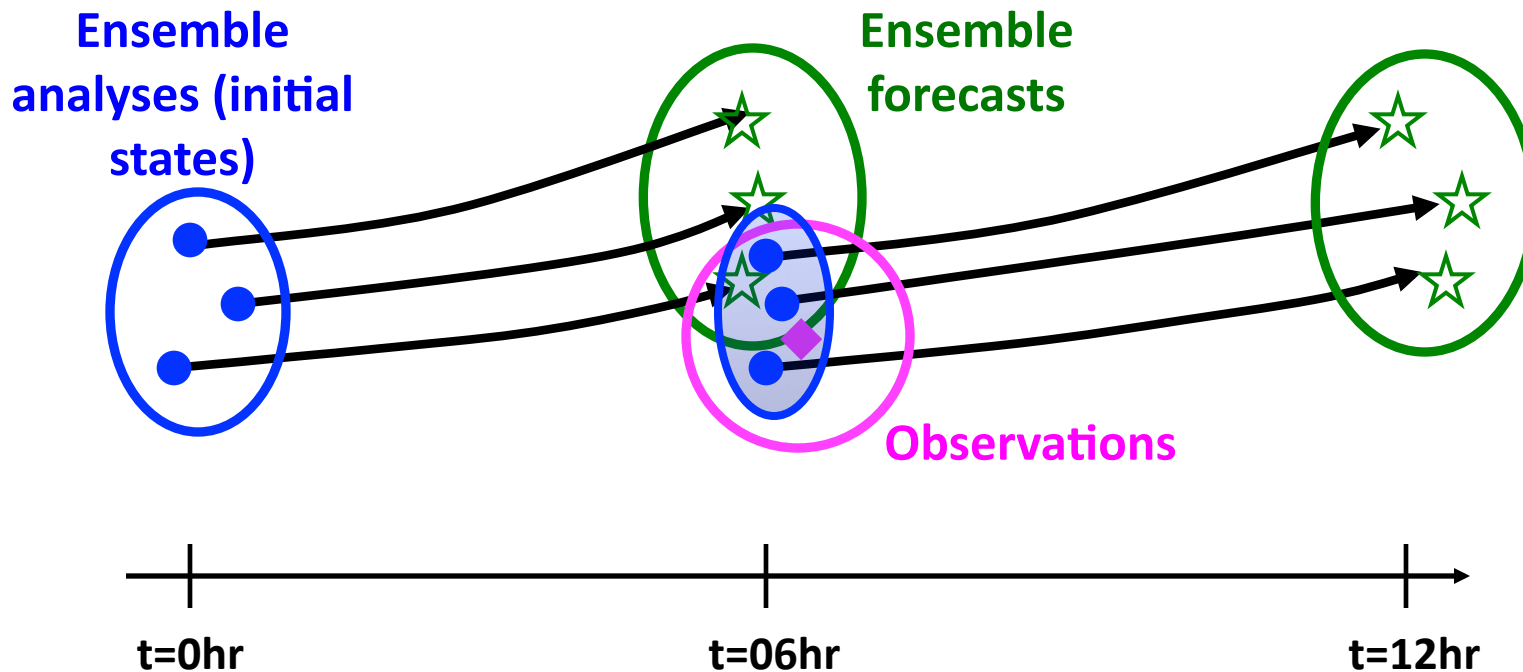
Junjie Liu, Inez Fung (University of California, Berkeley)

Eugenia Kalnay, Ji-Sun Kang (University of Maryland)

Supported by DOE

All the computations were carried out in DOE NERSC

Ensemble Kalman Filter (EnKF) process



- Background error changes with time;
- Obtain ensemble analyses.

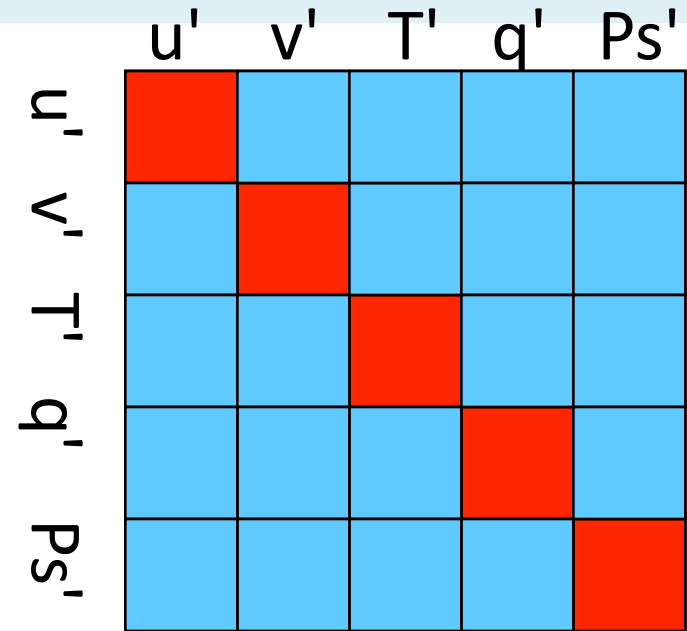
Forecast error statistics in EnKF

- Run K ensemble members $\rightarrow \mathbf{x}_i^b; i=1..K$

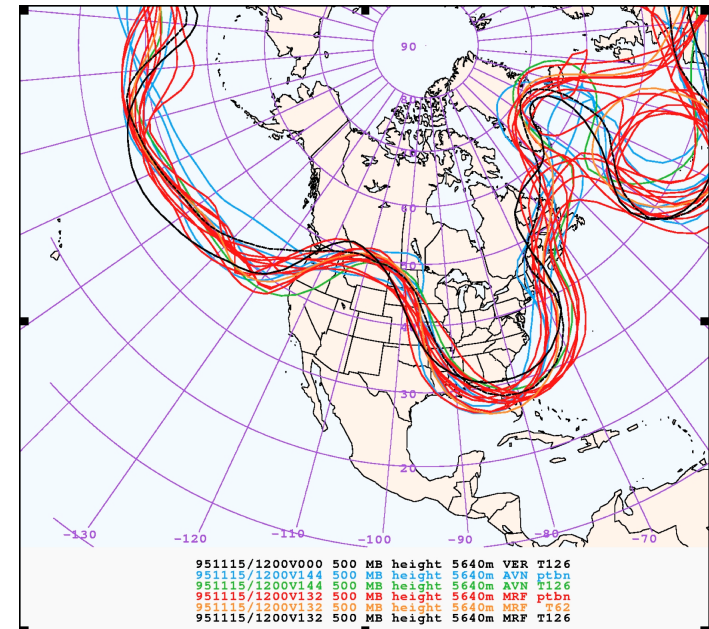
- $\bar{\mathbf{x}}^b$: ensemble mean.

$$\mathbf{P}^b = \frac{1}{K-1} \sum_{i=1}^K (\mathbf{x}_i^b - \bar{\mathbf{x}}^b)(\mathbf{x}_i^b - \bar{\mathbf{x}}^b)^T$$

$$= \begin{Bmatrix} u'u' & u'v' & u'T' & u'q' & u'Ps' \\ v'u' & v'v' & v'T' & v'q' & v'Ps' \\ T'u' & T'v' & TT' & T'q' & T'Ps' \\ q'u' & q'v' & q'T' & q'q' & q'Ps' \\ Ps'u' & Ps'v' & Ps'T' & Ps'q' & Ps'Ps' \end{Bmatrix}$$



std dev in u' etc \rightarrow error of the day
 Large std dev \rightarrow atm is dynamically unstable



Forecast error statistics in EnKF

- Run K ensemble members $\rightarrow \mathbf{x}_i^b; i=1..K$

- $\bar{\mathbf{x}}^b$: ensemble mean.

$$\mathbf{P}^b = \frac{1}{K-1} \sum_{i=1}^K (\mathbf{x}_i^b - \bar{\mathbf{x}}^b)(\mathbf{x}_i^b - \bar{\mathbf{x}}^b)^T$$

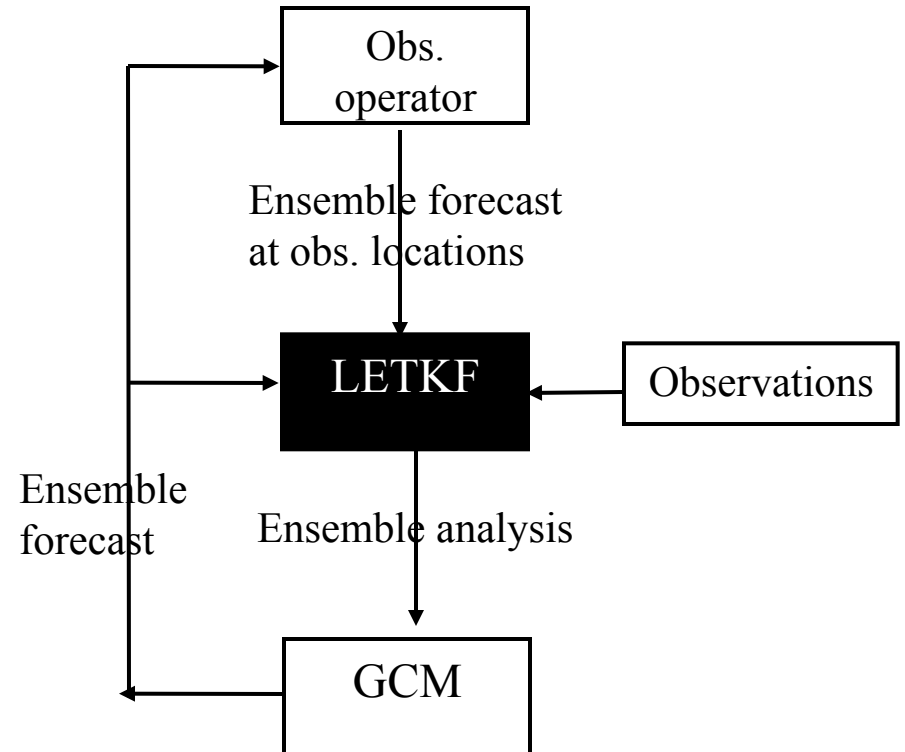
$$= \begin{Bmatrix} u'u' & u'v' & u'T' & u'q' & u'Ps' \\ v'u' & v'v' & v'T' & v'q' & v'Ps' \\ T'u' & T'v' & TT' & T'q' & T'Ps' \\ q'u' & q'v' & q'T' & q'q' & q'Ps' \\ Ps'u' & Ps'v' & Ps'T' & Ps'q' & Ps'Ps' \end{Bmatrix}$$

	u'	v'	T'	q'	Ps'
u'					
v'					
T'					
q'					
Ps'					

- Propagate info from the dynamical variables with observations to the dynamical variables with no observation.
- From location with observation to locations with no obs.

Summary steps of LETKF

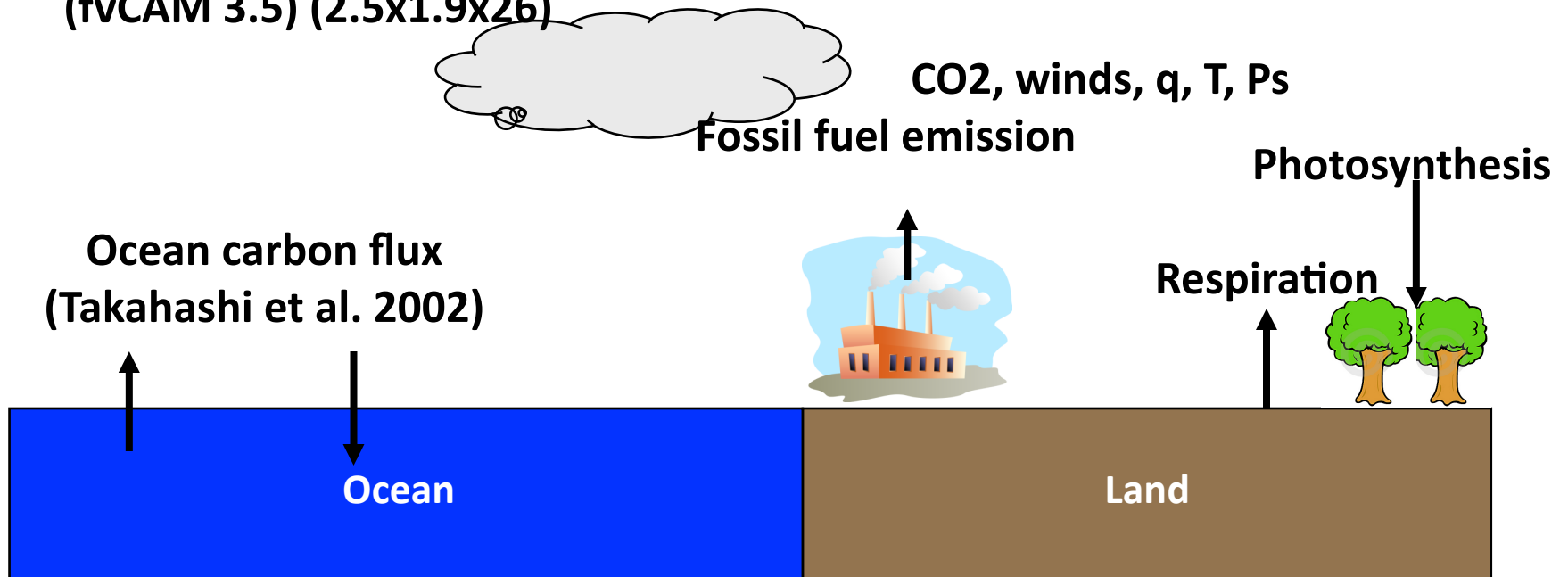
- 1) Global 6 hr ensemble forecast starting from the analysis ensemble
- 2) Choose the observations used for each grid point
- 3) Compute the matrices of forecast perturbations in ensemble space X^b
- 4) Compute the matrices of forecast perturbations in observation space Y^b
- 5) Compute P^b in ensemble space and its symmetric square root
- 6) Compute w^a , the k vector of perturbation weights
- 7) Compute the local grid point analysis and analysis perturbations.
- 8) Gather the new global analysis ensemble.



DOE-NCAR Carbon-Climate Model

Community Atmospheric Model

(fvCAM 3.5) (2.5x1.9x26)



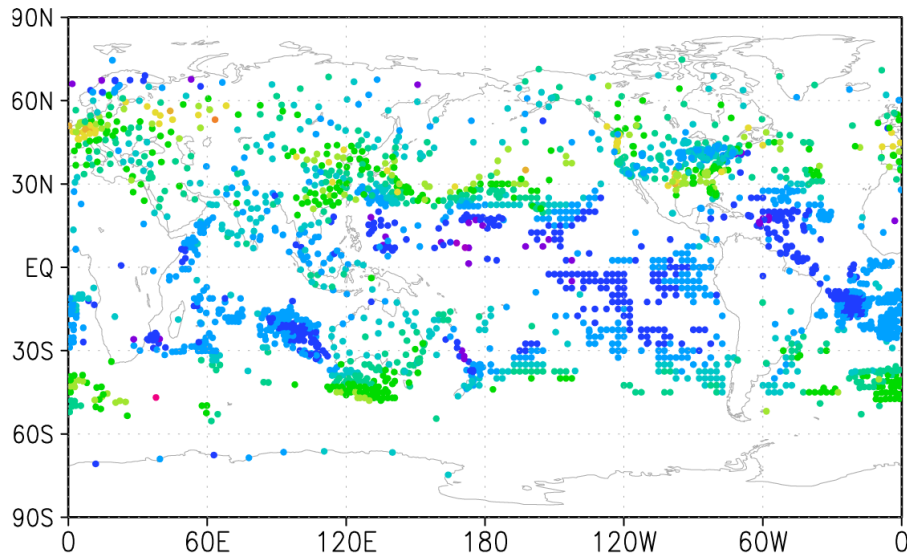
- CO₂ is transported as a tracer in CAM 3.5.
- Land carbon flux: 6-hourly flux from biogeochemical model.
- **Model produces CO₂ distribution that matches major features in surface CO₂ obs**
- Time period: the first half year of 2003.

The DATA

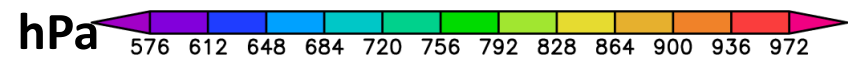
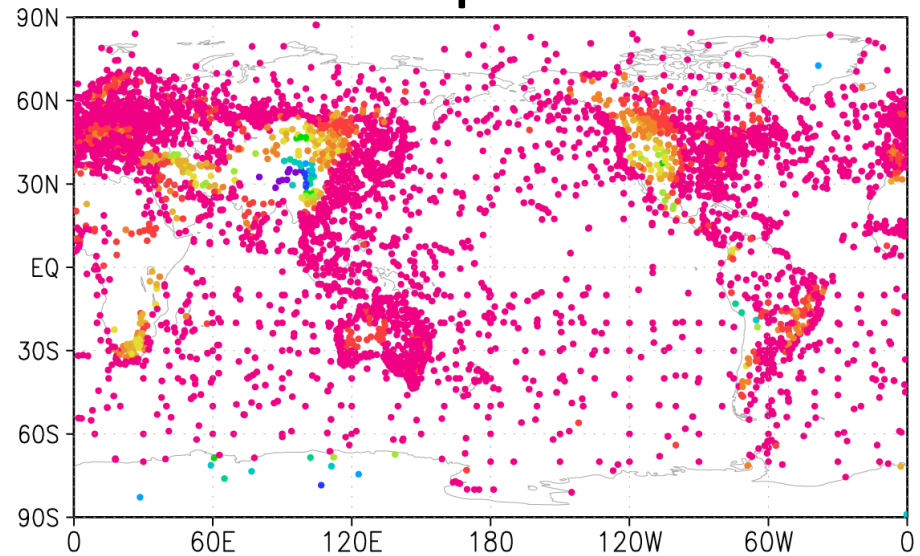
- **Raw Meteorology** every 6 hours: u , v , T , q , P_s
- **In-situ CO₂**: continuous near-surface CO₂ at Pt Barrow, AK; Mauna Loa; American Samoa; and South Pole
- **Satellite CO₂**: AIRS, ~100km, 2/day

Meteorological observations include radiosonde, satellite, ships etc: examples

Zonal wind within 500hPa and 600hPa

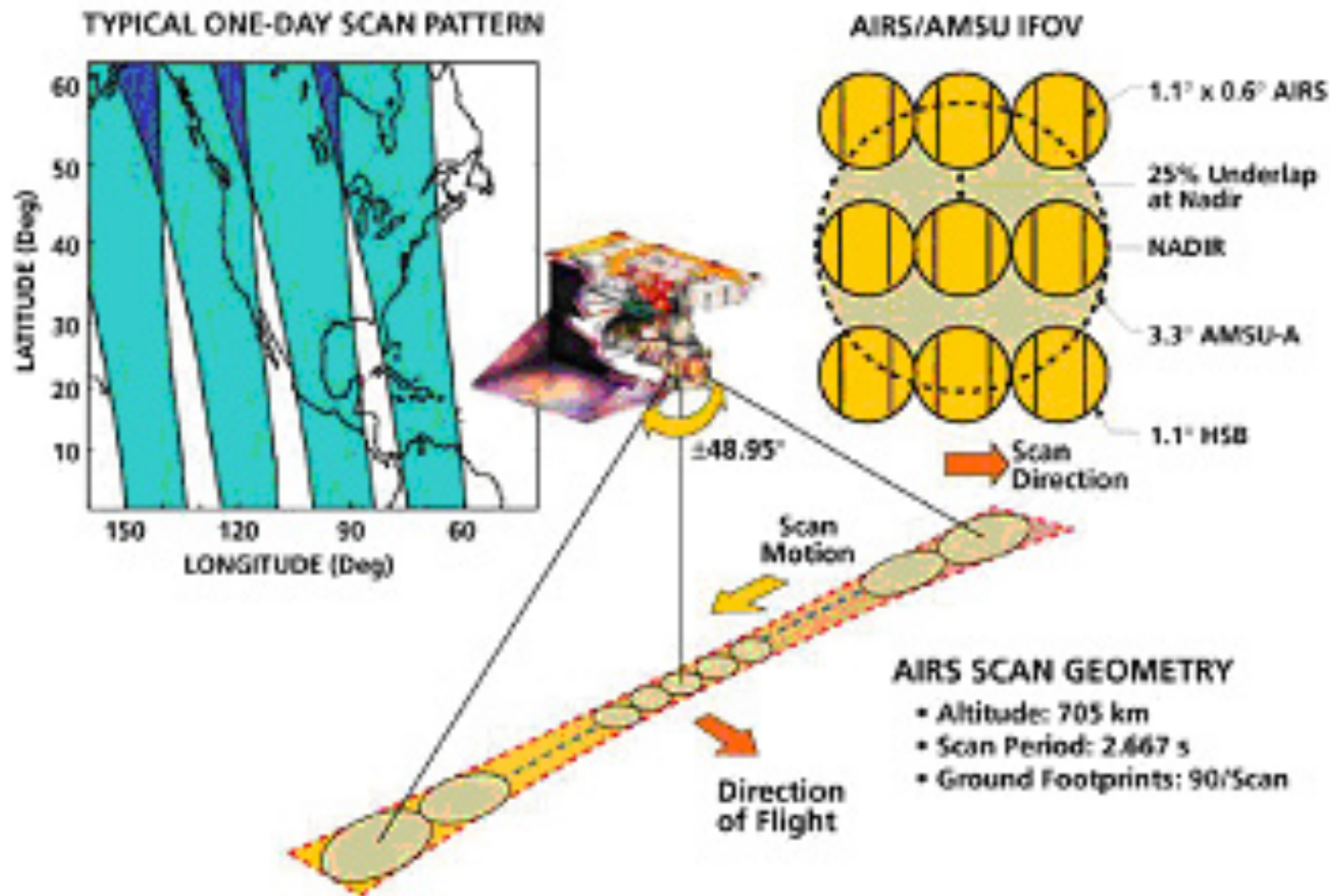


Surface pressure



- Assimilate all the quality-controlled meteorological observations assimilated in the DOE/NCEP Reanalysis 2 products (Kanamitsu et al. (2002).
- 10^6 observations within 6-hour.

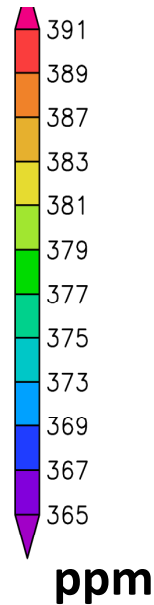
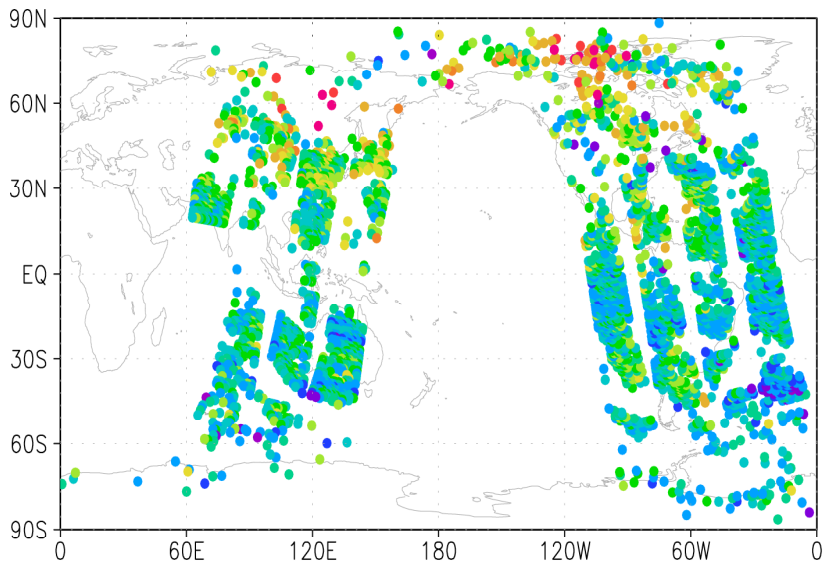
AIRS satellite instrument specification



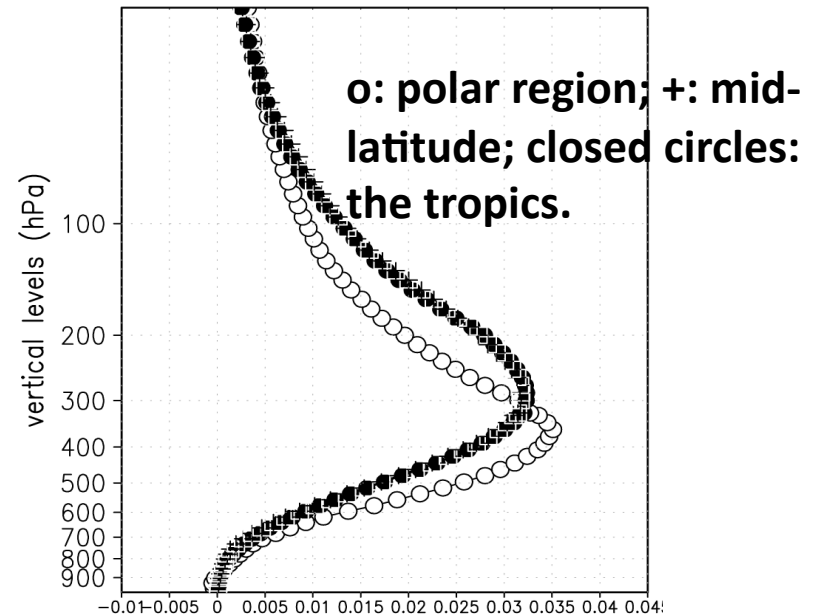
- Overpass the same spot twice per day;
- Footprint is about 100km.

More than 2000 AIRS CO2 within 6 hours; more sensitive in the middle troposphere

AIRS CO2 at 18Z01May2003 (+/-3hour)



AIRS averaging kernel

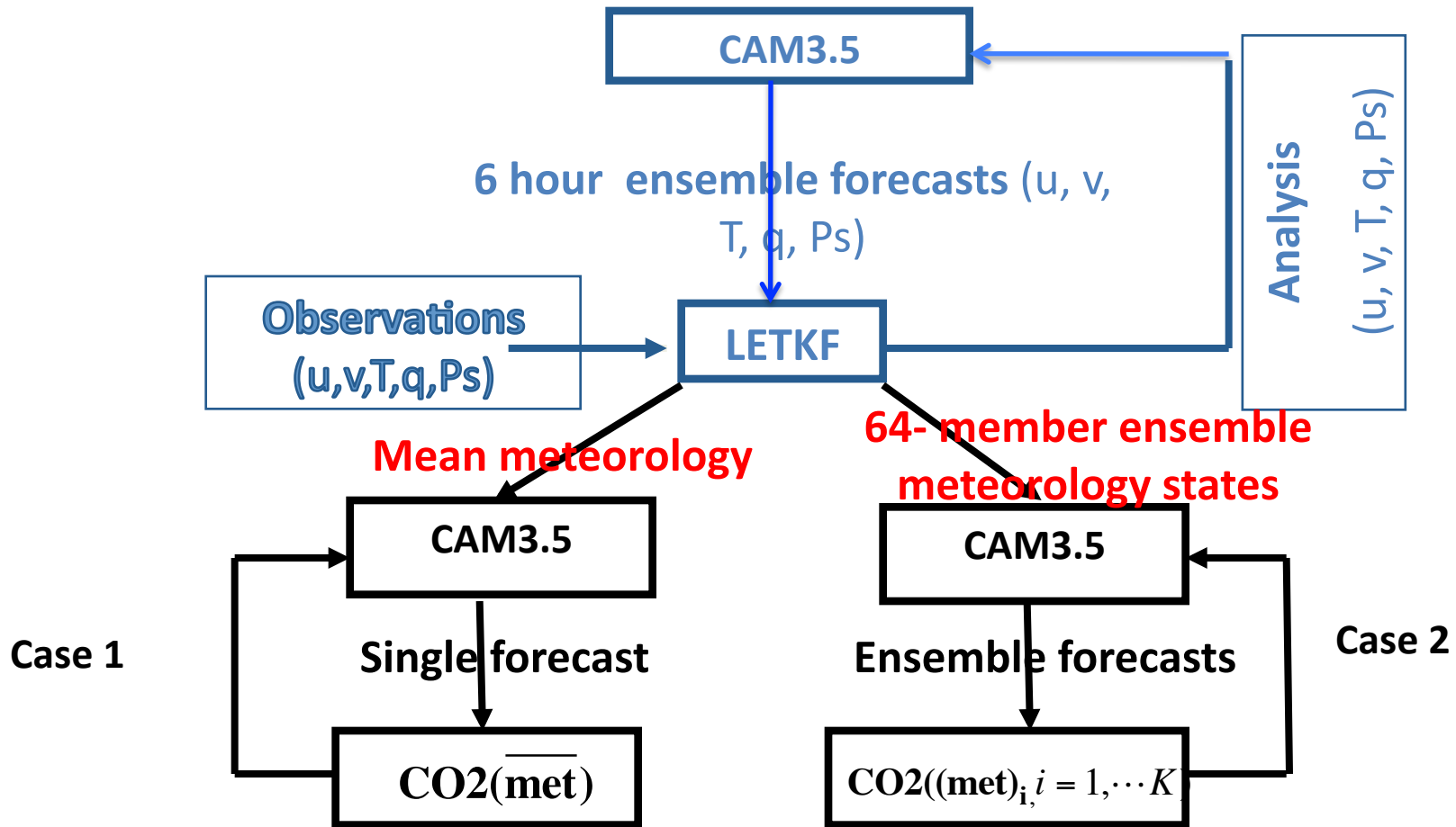


- Averaging kernel: the sensitivity of AIRS CO2 to the CO2 at each vertical level.

Assimilation Expts (64 ensemble members)

- **Free run. No assim. CO2 flux prior; CO2 as inert tracer**
- **Met run: assim meteorology only. CO2 flux prior; CO2 is inert tracer**
 - **Compare with free run**
 - **Compare bias in CO2 if use mean of meteorology**
- **Assimilate Met+CO2; CO2 flux prior (not updated)**
- **Assim Met+CO2; update CO2 flux**

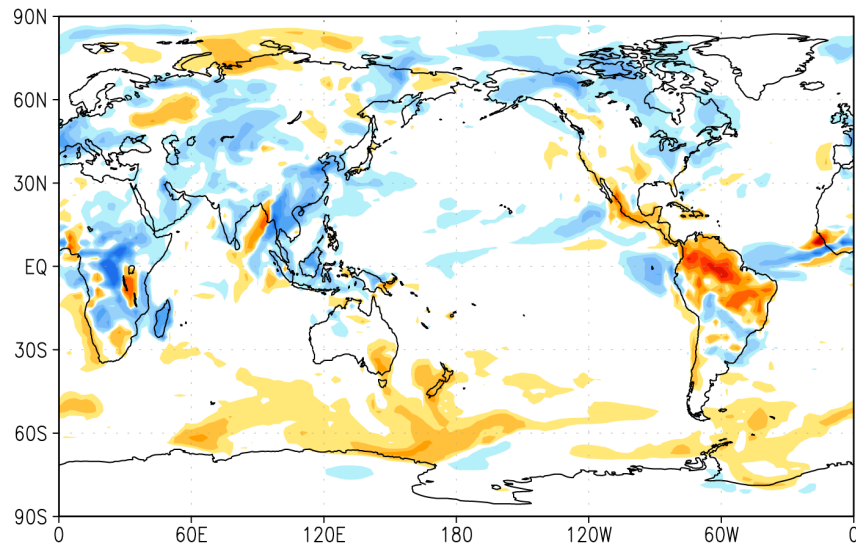
The impact of single and multiple meteorological states on CO₂ forecast



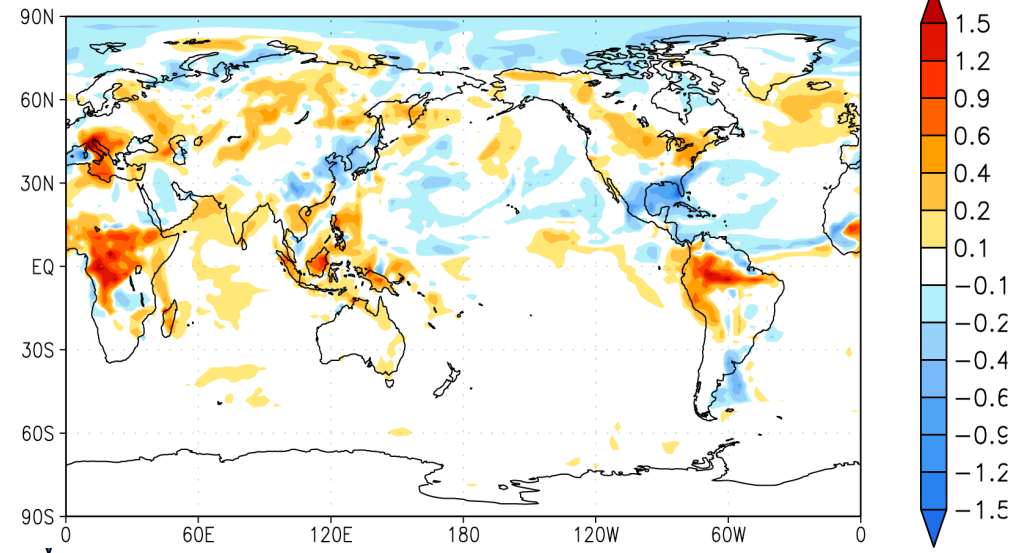
BIAS from transport

$$[\overline{\text{CO}_2(\text{met})} - \frac{1}{K} \sum_{i=1}^K \text{CO}_2((\text{met})_i)] \text{ at surface}$$

January 02-15



June 02-15

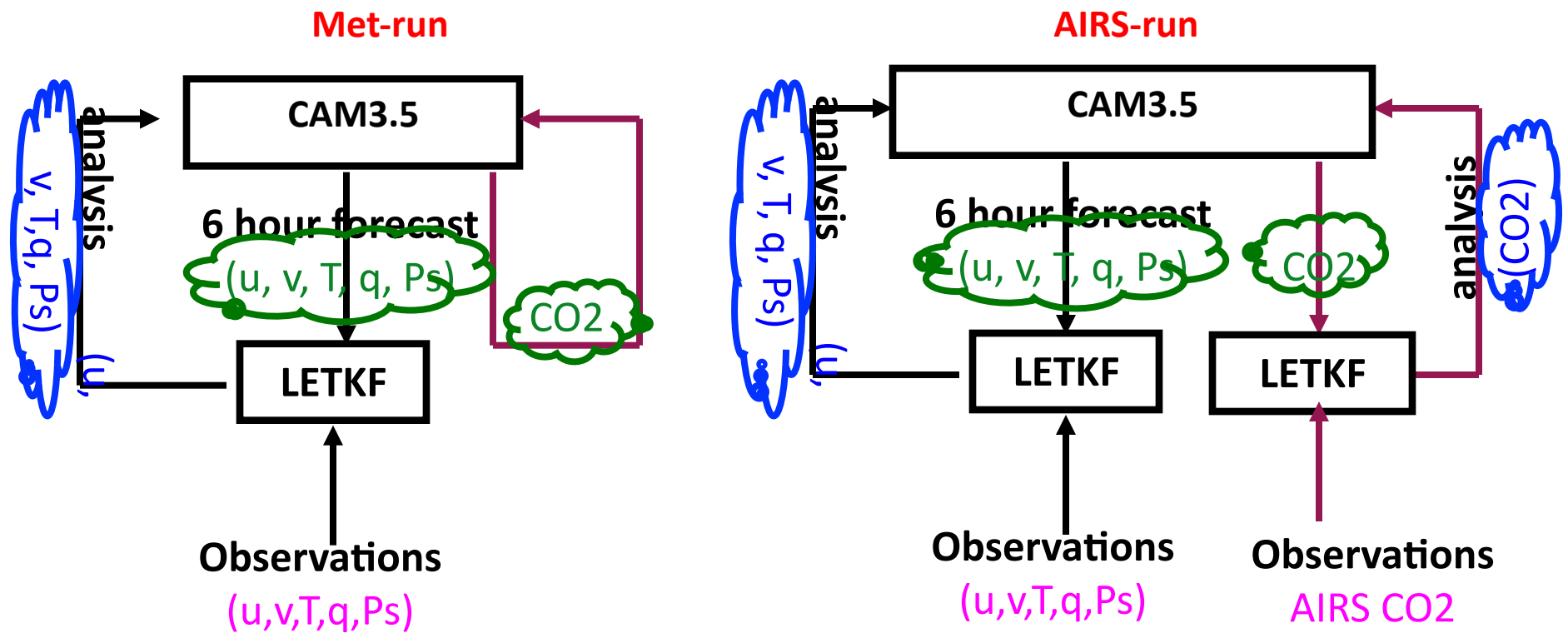


- **Non-uniform in both space and time, with the difference as large as $\pm 1.5\text{ppm}$.**
- **The difference is due to the **nonlinear interaction** in the model alone.**

Assimilation Expts (64 ensemble members)

- **Free run. No assim. CO2 flux prior; CO2 as inert tracer**
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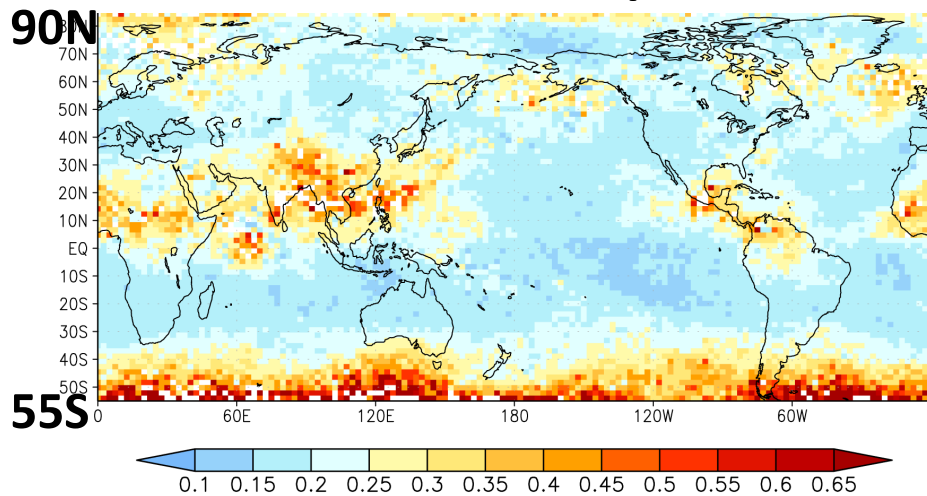
The impact of AIRS CO₂ assimilation on 6-hourly CO₂ 3D (x, y, z) fields



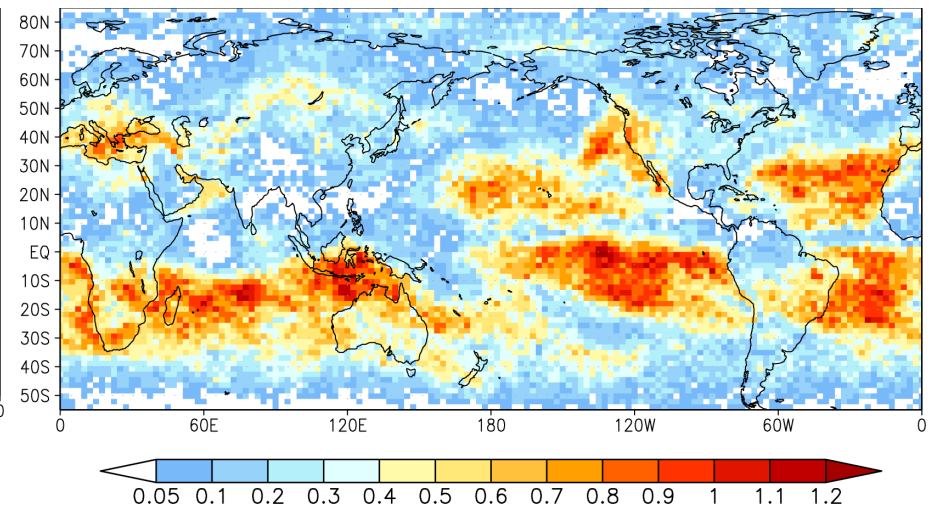
- AIRS-run: AIRS CO₂+met obs; Met-run: only met obs.
- The first half year of 2003.
- Prescribed surface carbon flux forcing.

Relationship Between Analysis Ensemble Spread and Observation Coverage

CO₂ analysis ensemble spread at observation space



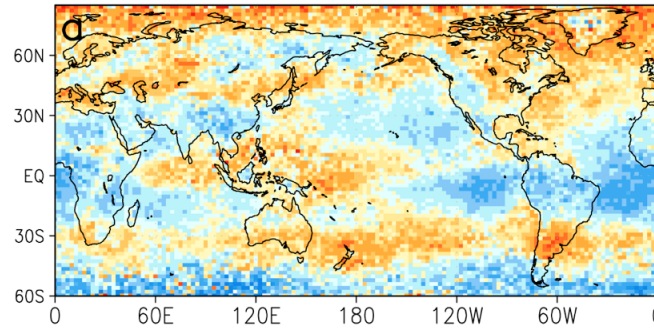
Average number of AIRS CO₂ observations within 6-hour



- Analysis ensemble spread is anti-correlated with the the CO₂ observation coverage

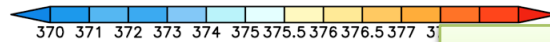
CO2 at ~500hPa

Monthly average AIRS CO2 (ppm):Sep

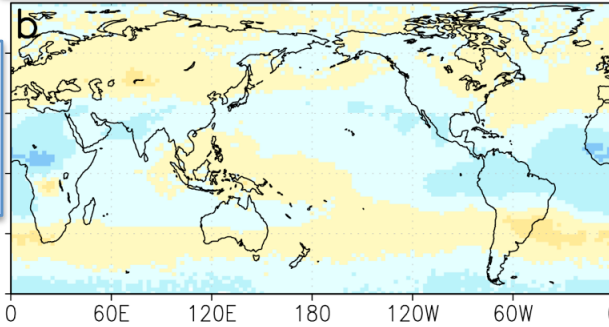


AIRS obs

Column CO2

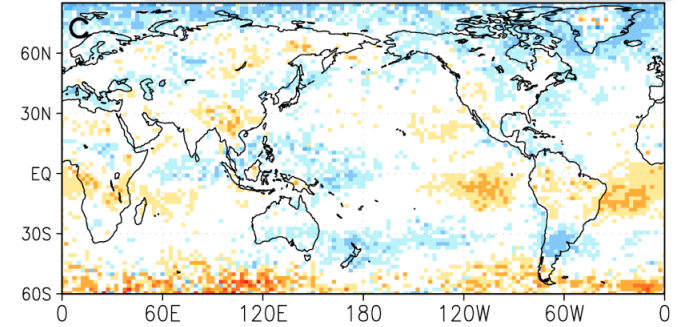


Column CO2 from AIRS-run

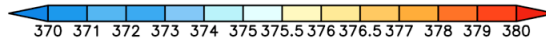


Column CO2 minus AIRS

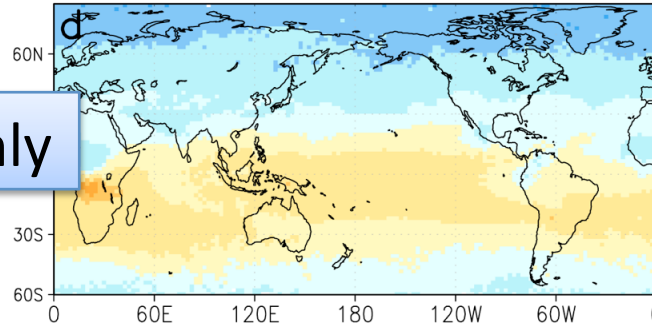
Difference



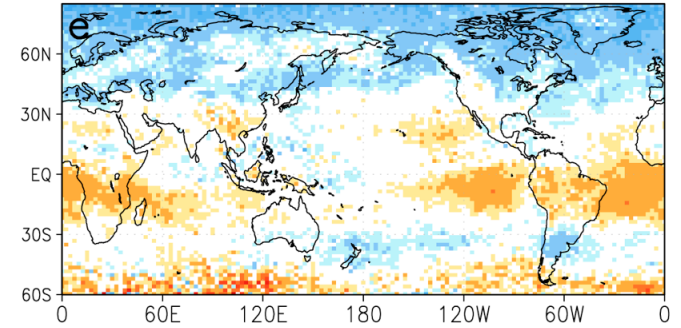
Assim Meteorology +AIRS



Column-integrated CO2 from meteo-run



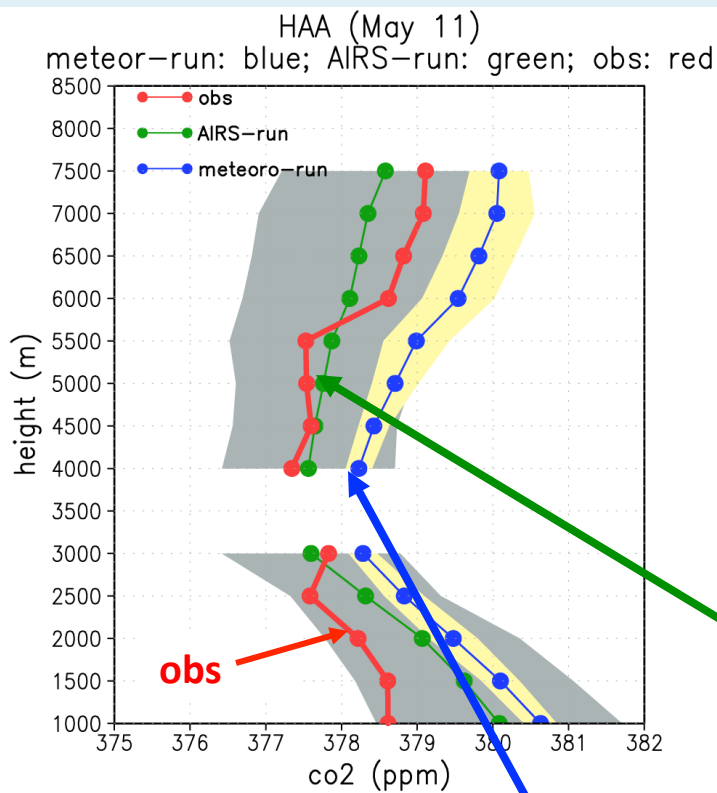
Difference between meteo-run and AIRS



Assim Meteorology only

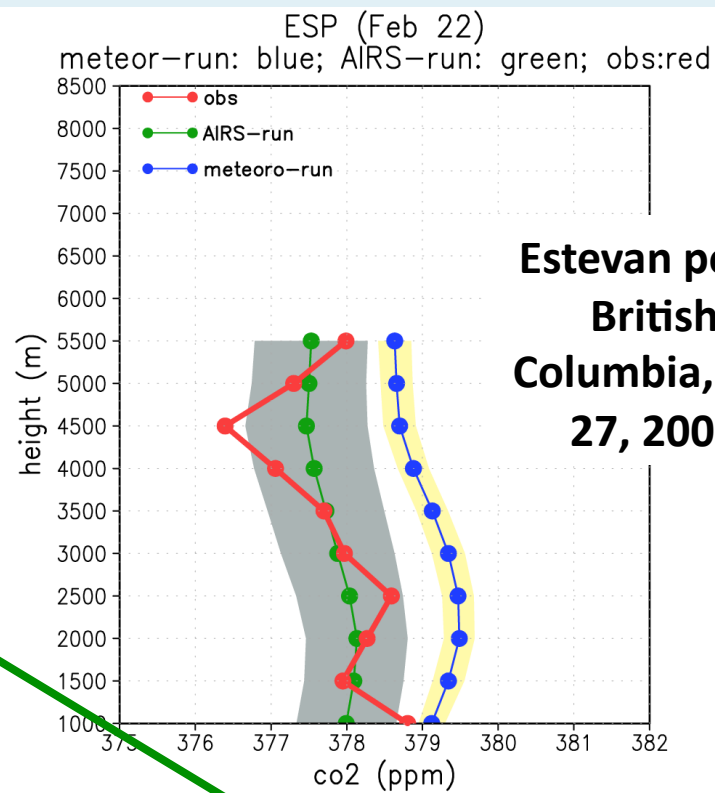
Ensemble CO2 analyses bracket aircraft obs

**Molokai
Island,
Hawaii.
May 11,
2003**



- **Meteor-run: CO2 tracer transported by 64-member ensemble meteorological analyses generated every 6hr --> "precision" of CO2 "forecast" by model**

**Estevan point,
British
Columbia, Feb
27, 2003**

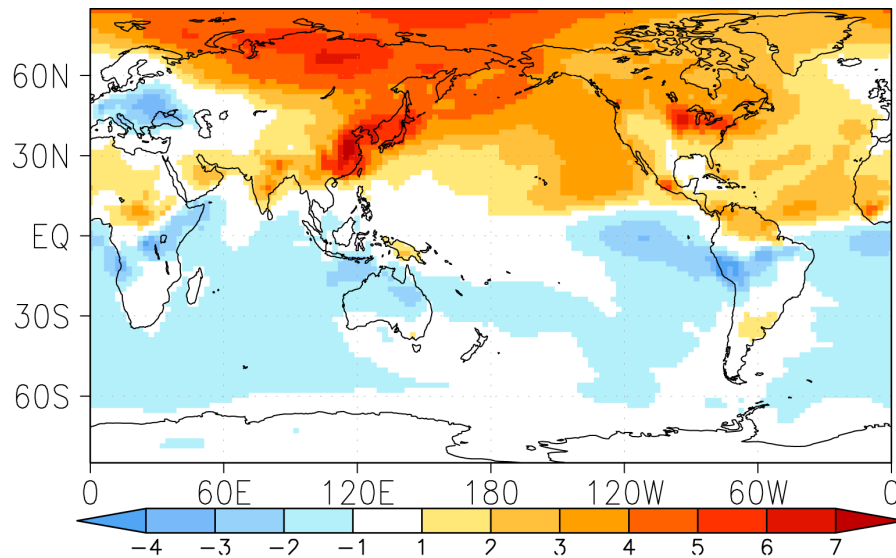


- **AIRS-run: CO2 assimilated along with meteorological obs.**

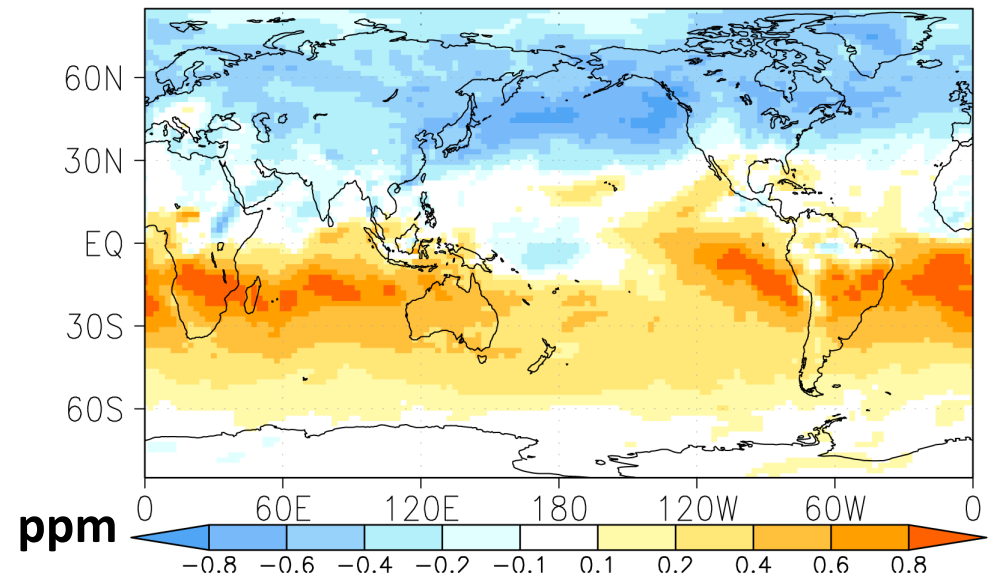
Known: models underestimate vertical mixing

May 2003: CO₂(925hPa)-CO₂(500hPa)

Met-run



(AIRS-run)-(Met-run)



- In the NH, CO₂(925hPa)>CO₂(500hPa): fossil fuel+ land carbon source;
- In the SH, CO₂(925hPa)<CO₂(500hPa): transported from the NH.

Assimilating AIRS CO₂ decreases vertical gradient

Atmosphere

momentum $\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} + 2\Omega \times \vec{u} = -\frac{1}{\rho} \nabla p + g\hat{k} + \vec{F} + \mathfrak{S}(\vec{u})$

energy $\frac{\partial T}{\partial t} + \vec{u} \cdot \nabla T = SW \updownarrow + LW \updownarrow + SH + LH + \mathfrak{S}(T)$

water vapor $\frac{\partial q}{\partial t} + \vec{u} \cdot \nabla q = Evap - Condensation + \mathfrak{S}(q)$

CO2 $\frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = SfcFlux + \mathfrak{S}(C)$

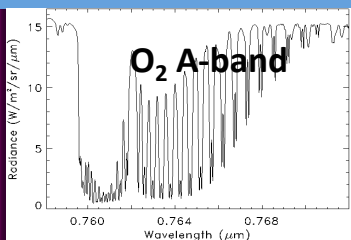
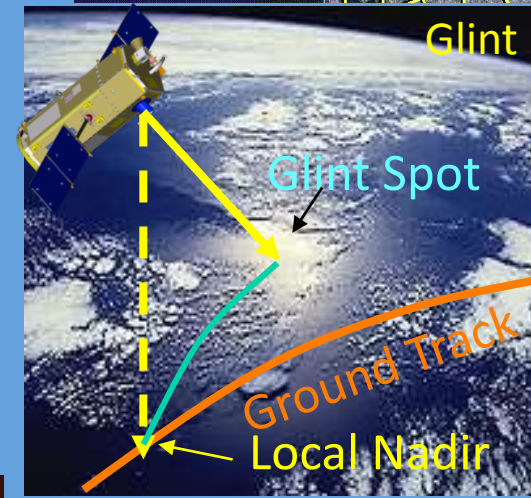
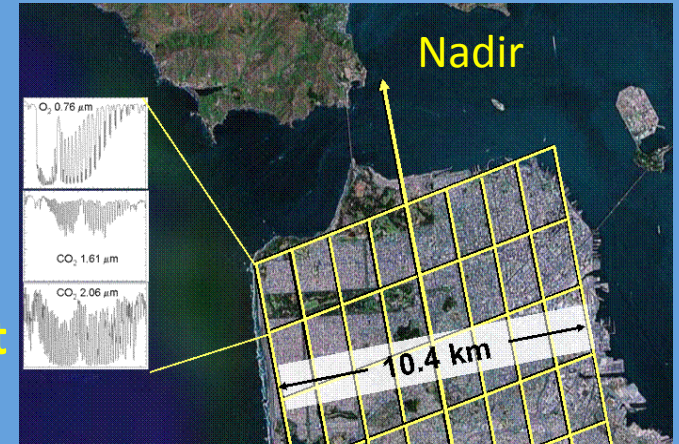
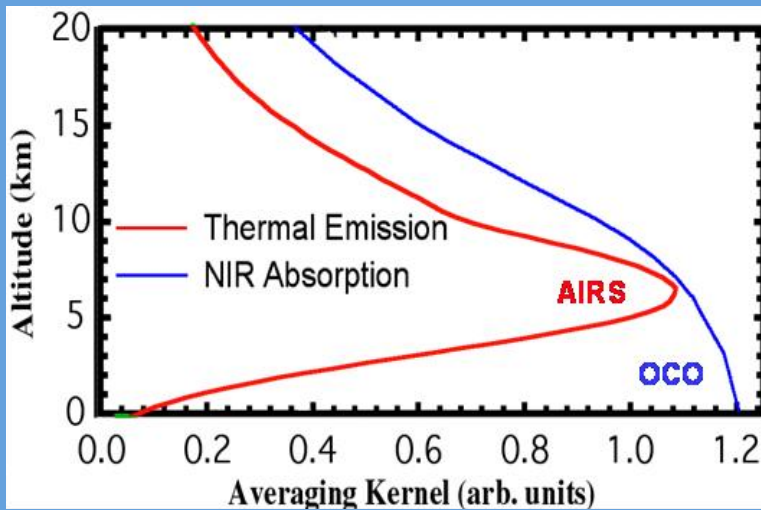
\mathfrak{S} convective mixing

Sub-grid Scale Vertical Mixing

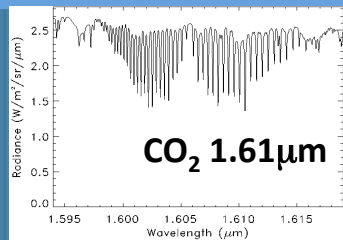
- **T(z), q(z) from meteorological assimilation \approx best approx to obs**
- **Convective mixing working terms on RHS of equations (in-situ source/sink terms) to produce “best” T(z), q(z)**
- **CO₂ has no in-situ source/sink terms**
- **CO₂(z) is a cleaner diagnostic of sub-grid scale vertical mixing**
- **CO₂ is the only inert (in atm) tracer with repeating obs in the vertical**

Outlook 1: Orbiting Carbon Observatory (OCO-2)

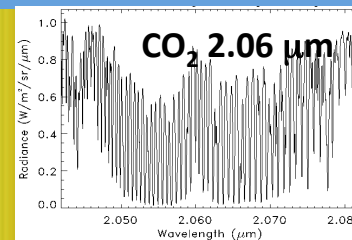
- High resolution spectra of reflected sunlight in near IR CO₂ and O₂ bands
- 3 km² footprint at nadir
- 3 Hz
- Sun-Synchronous Orbit (7km/s): 16-day repeat



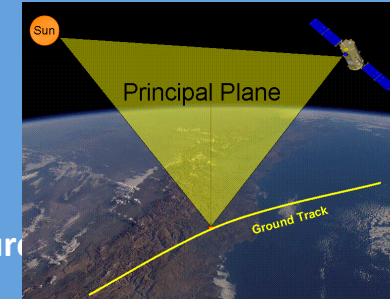
Clouds/Aerosols,
Surface Pressure



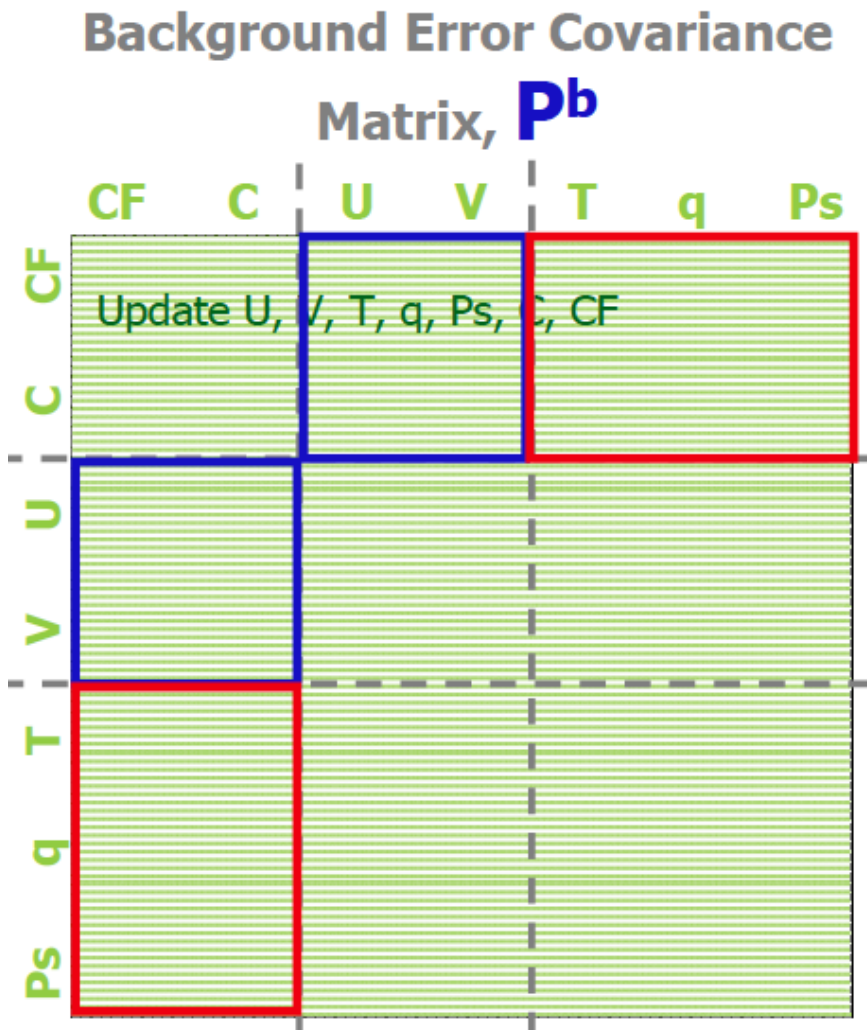
Column CO₂



Clouds/Aerosols, H₂O, Temperature



Outlook 2: Multi-variate Assimilation



$$\mathbf{X}^b = \begin{bmatrix} \mathbf{X}^* \\ \text{CF} \end{bmatrix} \quad \begin{array}{l} \mathbf{X}^* = (\text{U}, \text{V}, \text{T}, \text{q}, \text{Ps}, \text{C}) \\ \text{CF} = \text{surface carbon flux} \end{array}$$

- **Errors of all variables are coupled**
 - **Errors of CO₂ variables correlated with errors of all atmospheric variables (U, V, T, q, Ps)**
- This includes the error correlation between CO₂ variables and (T, q, Ps), which is not physical and introduces sampling errors

