

**UNIFIED PARAMETRIZATION**  
**– MORE DIAGNOSTICS AND INTERPRETATIONS –**

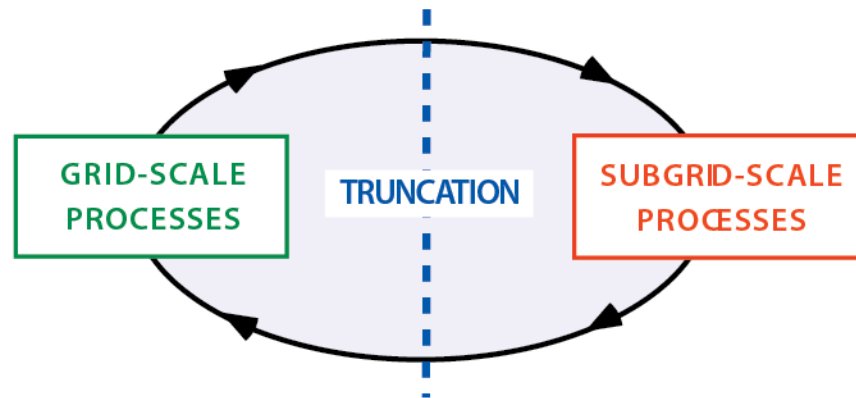
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## THE PARAMETERIZATION PROBLEM IN NUMERICAL MODELING

The need for parameterization arises from the *artificial* truncation of atmospheric processes.




Parameterization in numerical modeling is an inherently resolution-dependent problem.

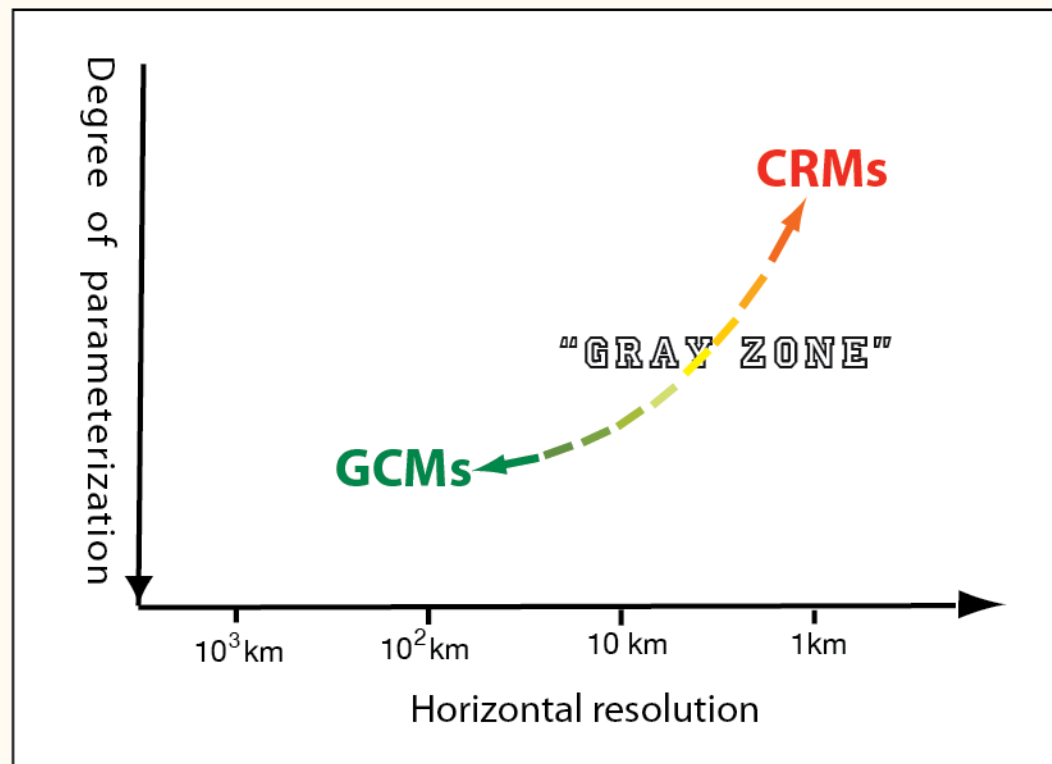
## UNIFIED PARAMETERIZATION

- An attempt to break through the "GRAY ZONE" -

Deep convection  
*explicitly simulated*



Deep convection  
*highly parameterized*



## JOINT USE OF PARAMETERIZATION AND EXPLICIT PREDICTION

- In mesoscale modeling, the importance of jointly using parameterization and explicit prediction of hydrometeors has been well recognized :

e.g.,

Full physics approach (Zhang et al. 1988)

Hybrid approach (Molinari and Dudek 1992)

Cascading approach (Gerard 2007)

- Approaches similar to these are now often taken even in GCMs for selected species of hydrometeors.

Resolution-dependent formulation of the subgrid dynamical response to cloud microphysics remains challenging.

## TWO CRM SIMULATIONS USED IN THIS STUDY

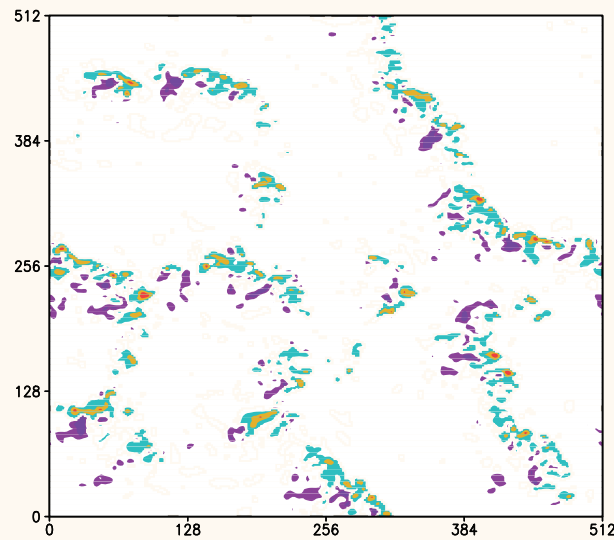
Model : The vorticity equation model of Jung and Arakawa (2008)

Horizontal domain size : 512 km      Horizontal grid size : 2km

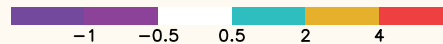
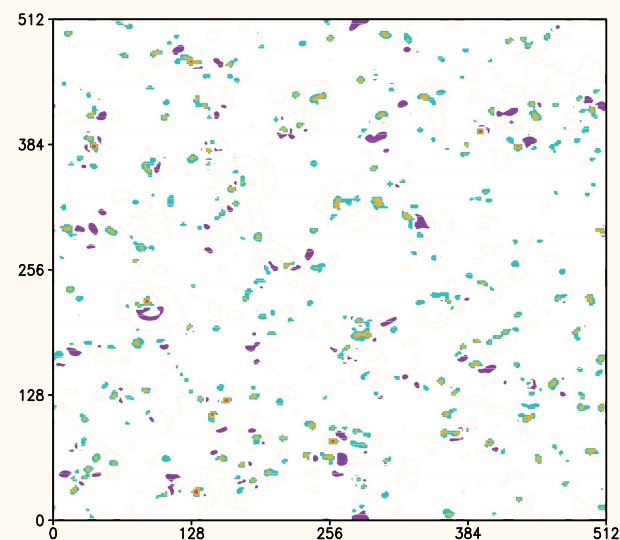
Data used : last 2 or 12 hrs of two 24-hr simulations with 20-min intervals

### Snapshots of vertical velocity $w$ at 3 km height

With Shear



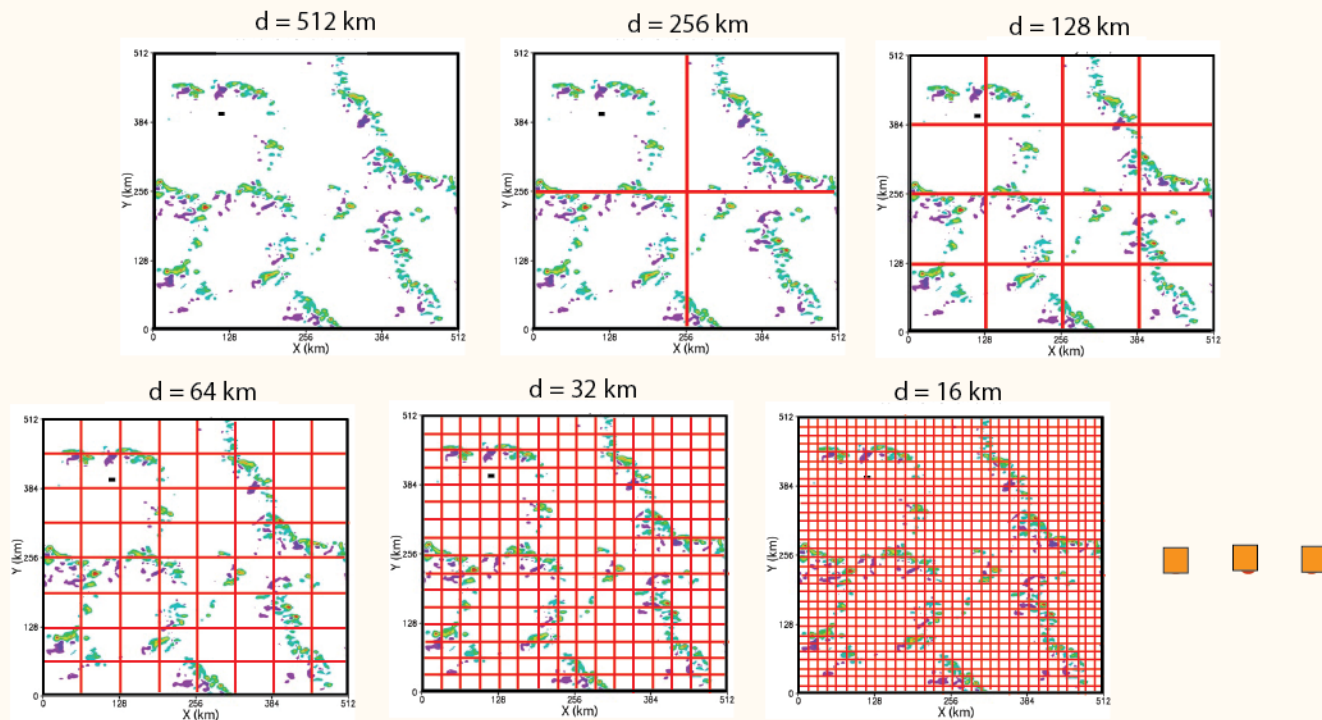
Without Shear



# ANALYSIS OF THE RESOLUTION-DEPENDENT STATISTICS OF THE CRM-SIMULATED DATA

The original domain (512 km) used for CRM simulations is divided into sub-domains of same size.

## Examples

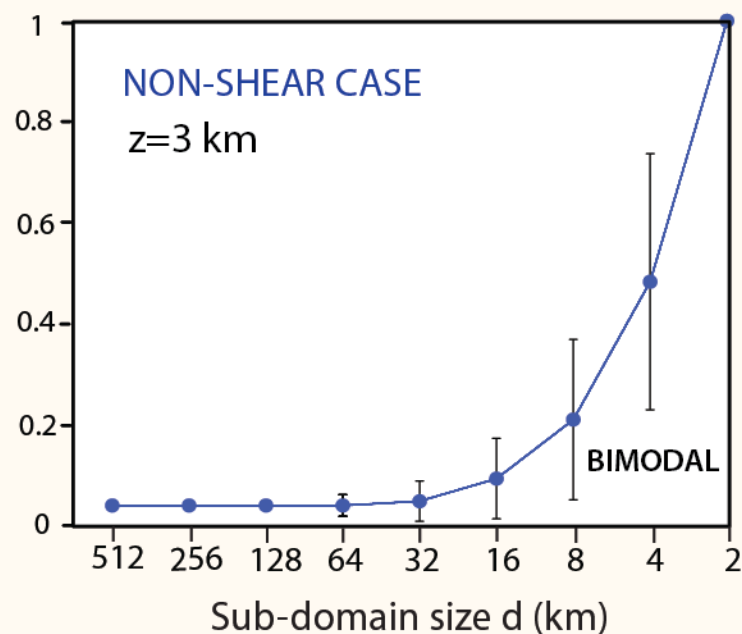
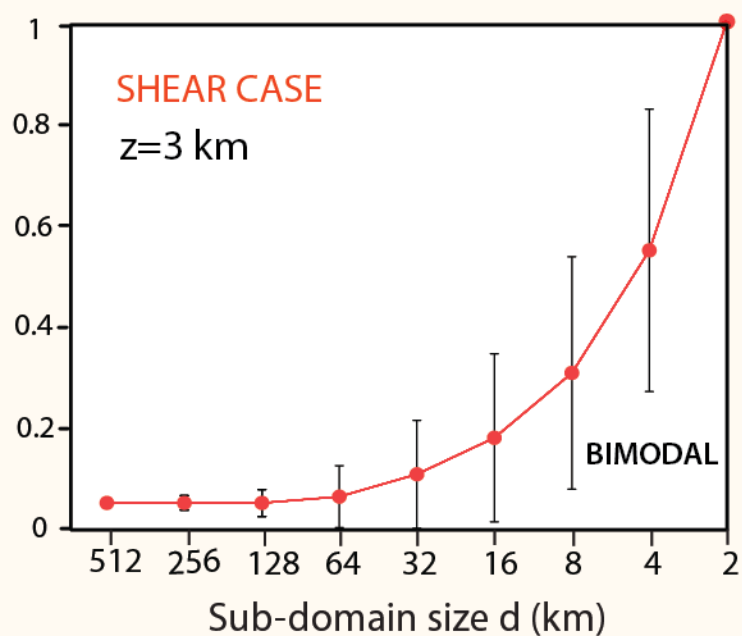


The size of subdomains is interpreted as the GCM grid size.

## FRACTIONAL AREA COVERED BY CONVECTIVE UPDRAFTS, $\sigma$

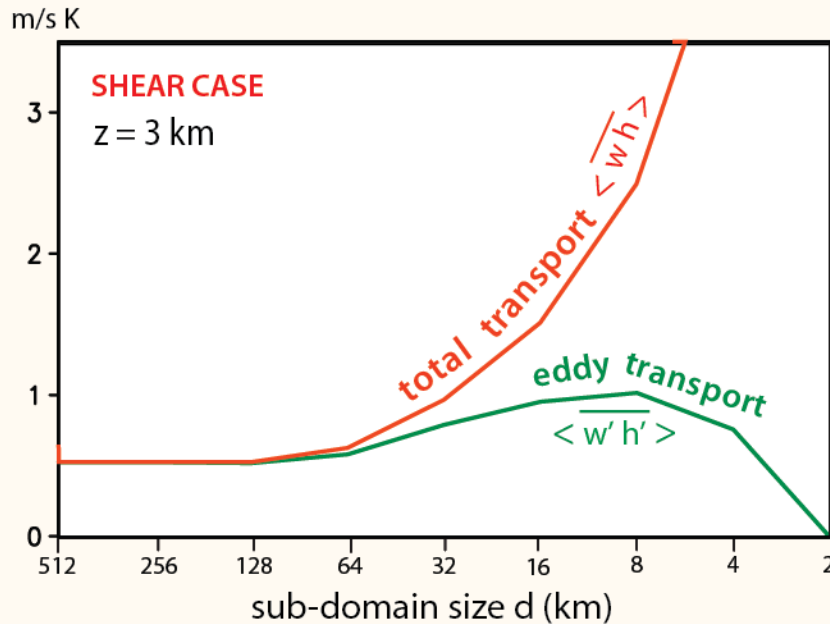
Measured by the fractional number of grid points in a sub-domain that satisfy  $w > 0.5$  m/s.

Ensemble average of  $\sigma$  over all sub-domains with  $\sigma > 0$



$\sigma \ll 1$  can be a good approximation *ONLY* for low resolutions.

# RESOLUTION DEPENDENCE OF ENSEMBLE-AVERAGE VERTICAL TRANSPORT OF MOIST STATIC ENERGY



$h$  : Deviation of moist static energy from a reference state

$\overline{(\ )}$  : Average over all grid points in the sub-domain

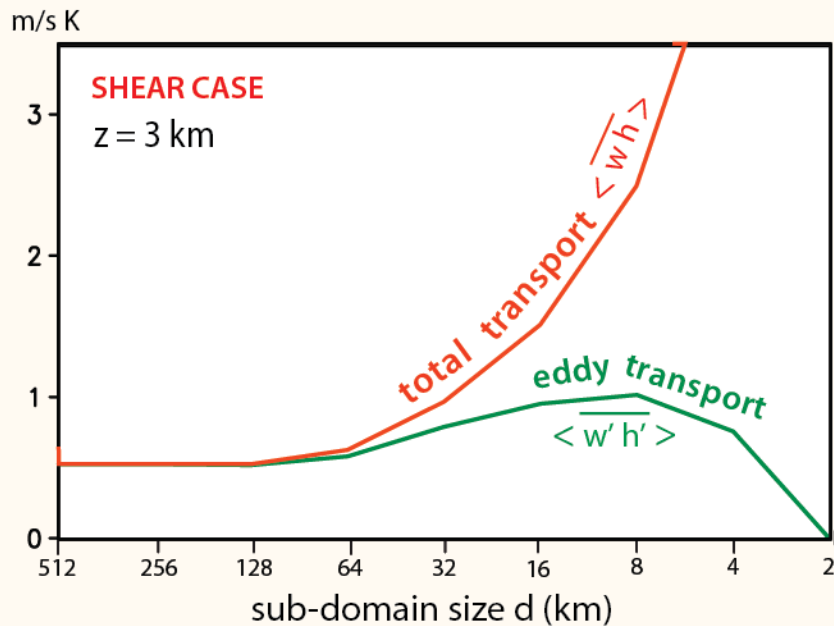
$\langle \rangle$  : Ensemble average over all sub-domains with  $\sigma > 0$ .

$(\ )'$  :  $(\ ) - \overline{(\ )}$

As the resolution increases, the total transport tends to increase while the eddy transport for small d tends to decrease.



# RESOLUTION DEPENDENCE OF ENSEMBLE-AVERAGE VERTICAL TRANSPORT OF MOIST STATIC ENERGY



$h$  : Deviation of moist static energy from a reference state

$\overline{(\ )}$  : Average over all grid points in the sub-domain

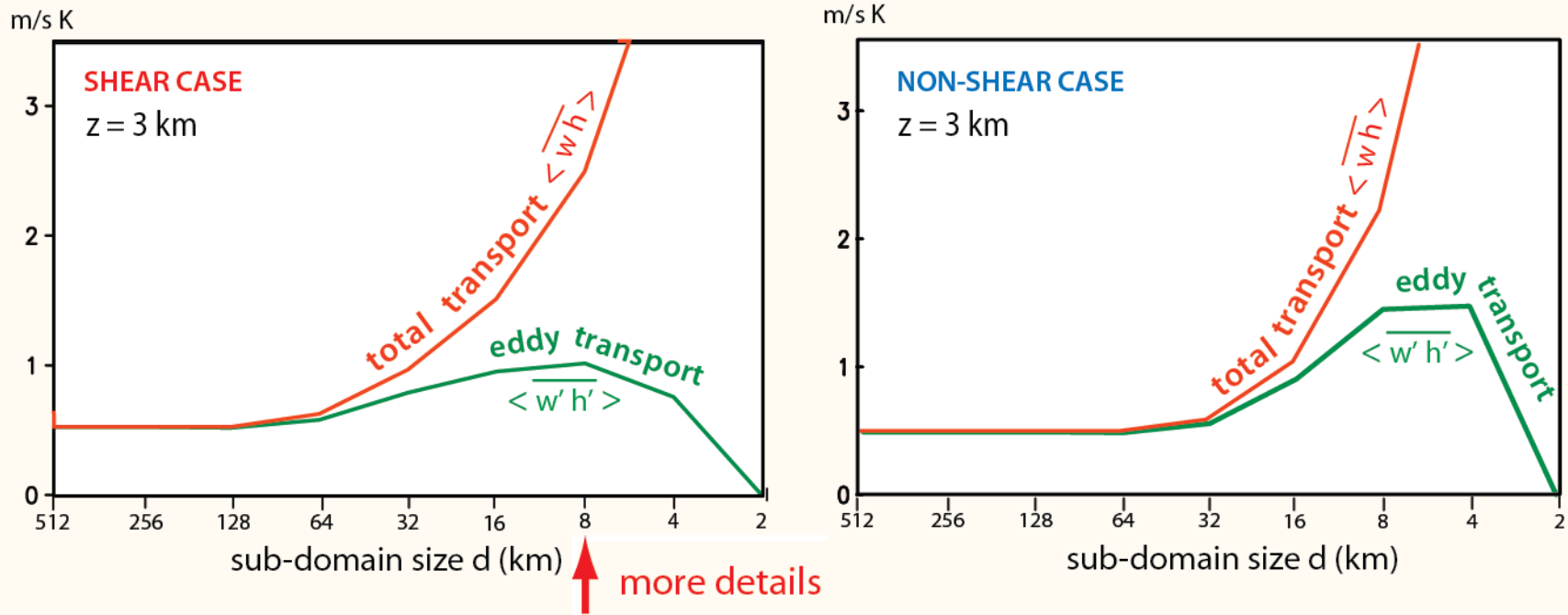
$\langle \rangle$  : Ensemble average over all sub-domains with  $\sigma > 0$ .

$(\ )'$  :  $(\ ) - \overline{(\ )}$

## IMPORTANT !

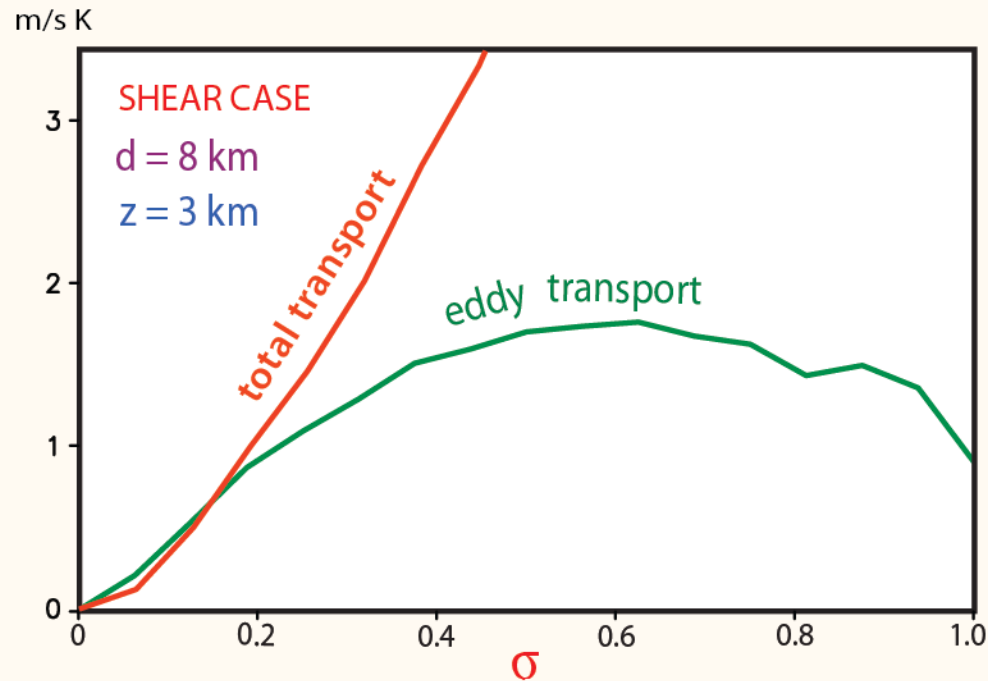
Parameterization is a formulation of the eddy transport,  
NOT that of the total transport.

# RESOLUTION DEPENDENCE OF ENSEMBLE-AVERAGE VERTICAL TRANSPORT OF MOIST STATIC ENERGY



There is no qualitative difference between the shear and non-shear cases.

# THE $\sigma$ -DEPENDENCE OF ENSEMBLE-AVERAGE VERTICAL TRANSPORT OF MOIST STATIC ENERGY



Even with the same resolution,  
the relative importance of eddy transport strongly depends on  $\sigma$ .

## VERTICAL EDDY TRANSPORT BY HOMOGENEOUS CLOUDS/ENVIRONMENT

Most conventional parameterizations assume that clouds and the environment are horizontally homogeneous.

Continue to use this assumption to start with.

For a thermodynamic variable  $\psi$ , we can derive

$$\overline{w'\psi'} = \sigma(1 - \sigma)\Delta w \Delta\psi$$

$\Delta( )$ : cloud-environment difference

If  $\Delta w \Delta\psi$  is independent of  $\sigma$ ,  
the  $\sigma$ -dependence of  $\overline{w'\psi'}$  is through  $\sigma(1 - \sigma)$ .

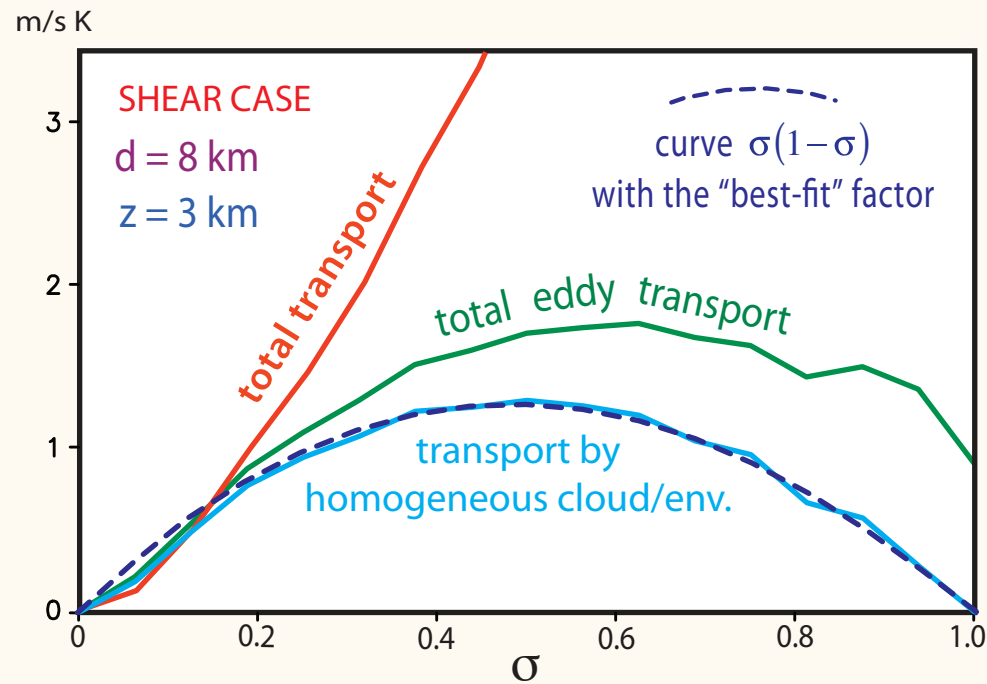
# SIMULATED VERTICAL EDDY TRANSPORT BY HOMOGENEOUS CLOUDS/ENVIRONMENT

For each sub-domain,

replace all  $w_c$  with  $\overline{w_c}$ ,

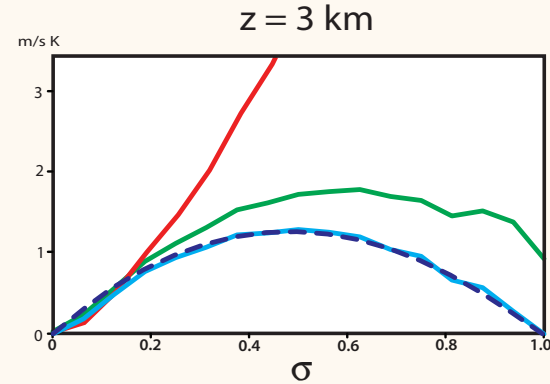
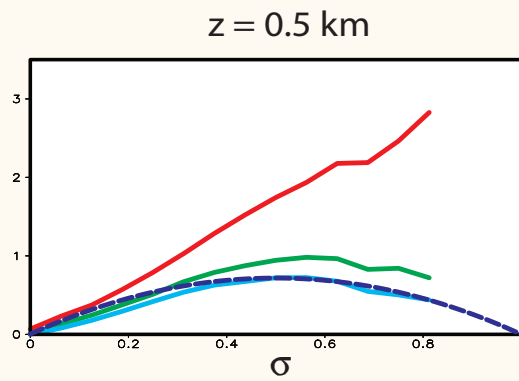
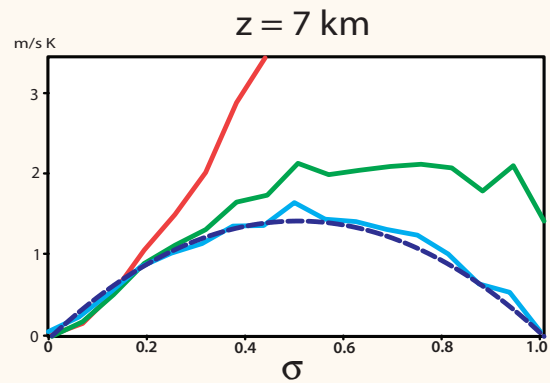
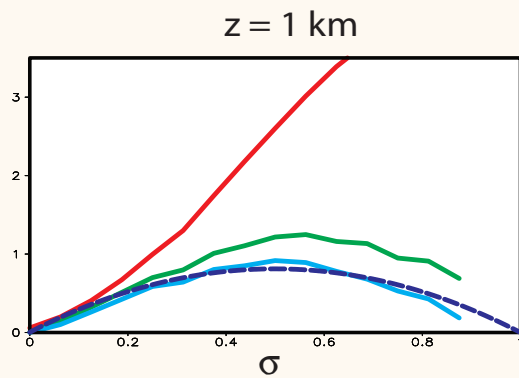
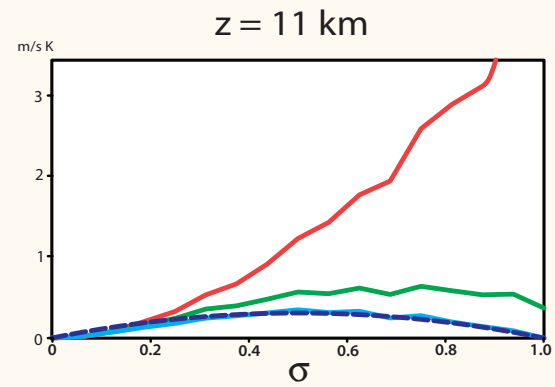
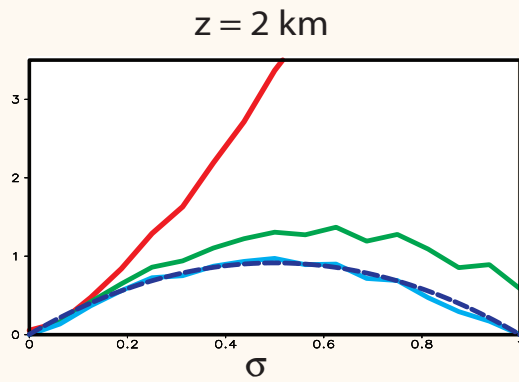
replace all  $h_c$  with  $\overline{h_c}$ ,

the same for the environment.

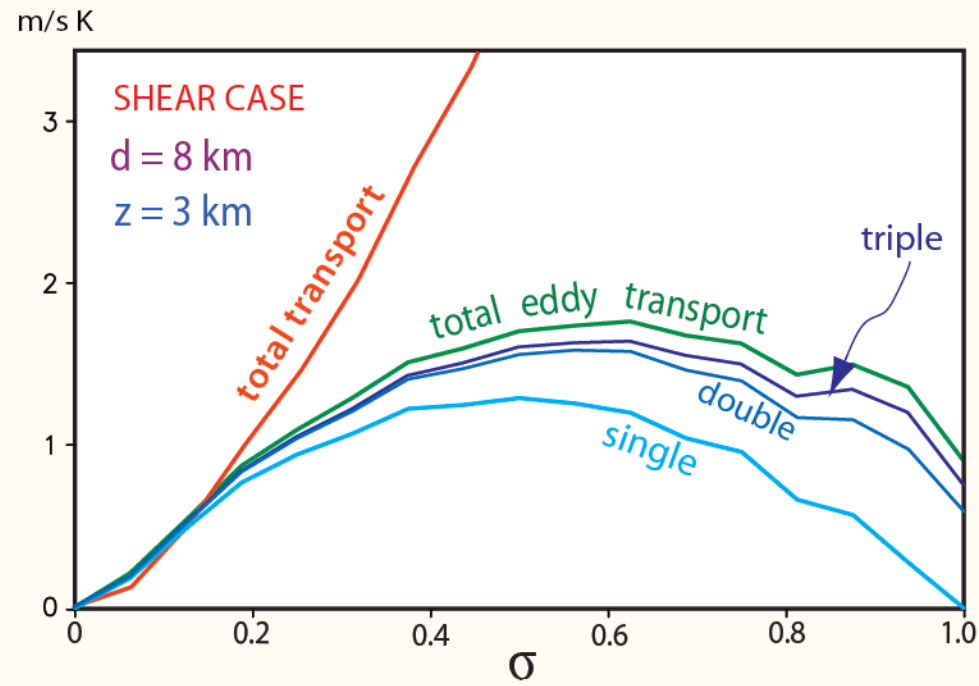


The dependence on  $\sigma$   
through  $\sigma(1 - \sigma)$   
is well supported.

# COMPARISONS OF EDDY TRANSPORT OF $h$ AT DIFFERENT LEVELS



# THE EFFECT OF MULTIPLE CLOUD-STRUCTURE / CLOUD-TYPE



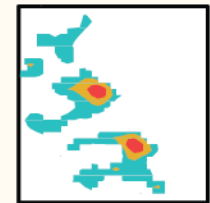
single  
 $0.5 \text{ m/s} < w$



double  
 $0.5 \text{ m/s} < w < 2 \text{ m/s}$   
 $2 \text{ m/s} < w$



triple  
 $0.5 \text{ m/s} < w < 2 \text{ m/s}$   
 $2 \text{ m/s} < w < 4 \text{ m/s}$   
 $4 \text{ m/s} < w$



# CLOSURE ASSUMPTION

## CONVENTIONAL ADJUSTMENT SCHEMES

Determine cloud properties  $w_c^*$  and  $h_c^*$   
assuming that grid-point values  
represent the environment (i.e.,  $\sigma \ll 1$ )

Estimate the transport  $(\overline{wh})_{adj}$   
required for the adjustment  
to a neutral state.

Assume that  
the eddy transport estimated with  $\sigma \ll 1$   
is totally responsible for the adjustment.

To be consistent,

$$\sigma = \frac{(\overline{wh})_{adj}}{(w_c^* - \overline{w})(h_c^* - \overline{h})}$$

Not used, but self-contradictory because  
 $\sigma \ll 1$  does not hold for large  $(\overline{wh})_{adj}$ .



## CLOSURE ASSUMPTION

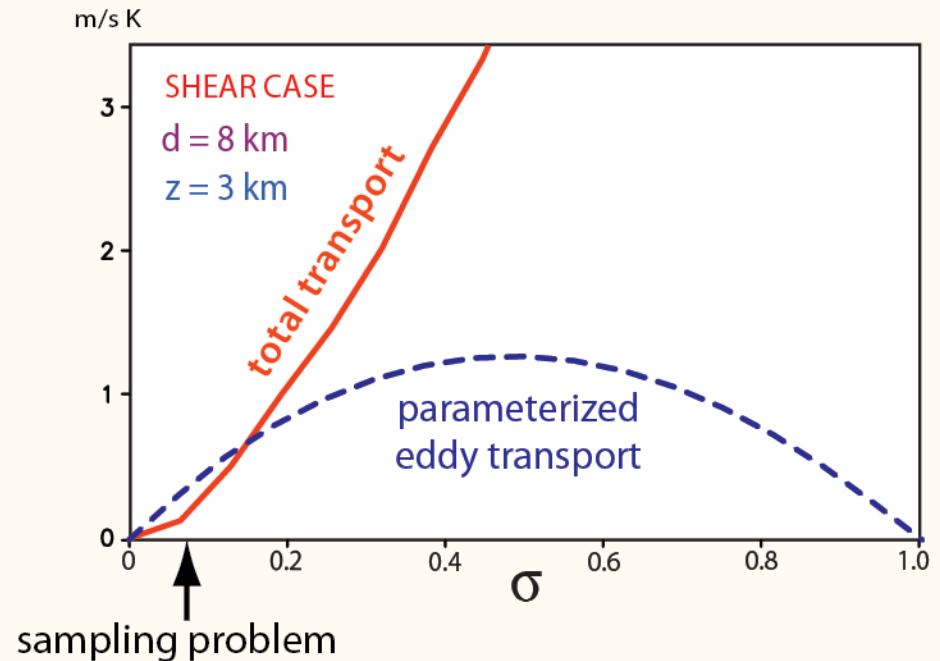
### UNIFIED PARAMETERIZATION (SINGLE CLOUD TYPE)

- When  $\sigma$  is larger,  $w_c - \bar{w}$  and  $h_c - \bar{h}$  are smaller.
- Then the magnitude of the eddy transport is limited.

➔ Relaxed adjustment

We choose

$$\sigma = \frac{(\overline{wh})_{\text{adj}}}{\overline{wh}_{\text{adj}} + (w_c^* - \bar{w})(h_c^* - \bar{h})}$$



This  $\sigma$  automatically satisfies  $0 \leq \sigma \leq 1$   
including  $\sigma \rightarrow 1$  as  $(\overline{wh})_{\text{adj}} \rightarrow \infty$ .

## SPECTRAL REPRESENTATION OF CLOUDS

Suppose that we use  $w$  at cloud base to classify cloud types (as in Chikira 2010).

We can drive

$$\overline{w'\psi'} = \sum_i (\Delta w_i \Delta \psi_i) \sigma_i - \sum_i \Delta w_i \sigma_i \sum_i \Delta \psi_i \sigma_i$$

A generalization of  $\overline{w'\psi'} = \sigma(1-\sigma)\Delta w \Delta \psi$

$\Delta$ : cloud-env. difference  
 $i$ : cloud type

We have to consider possible overlap of clouds.



internal structure

is more likely than



different cloud types

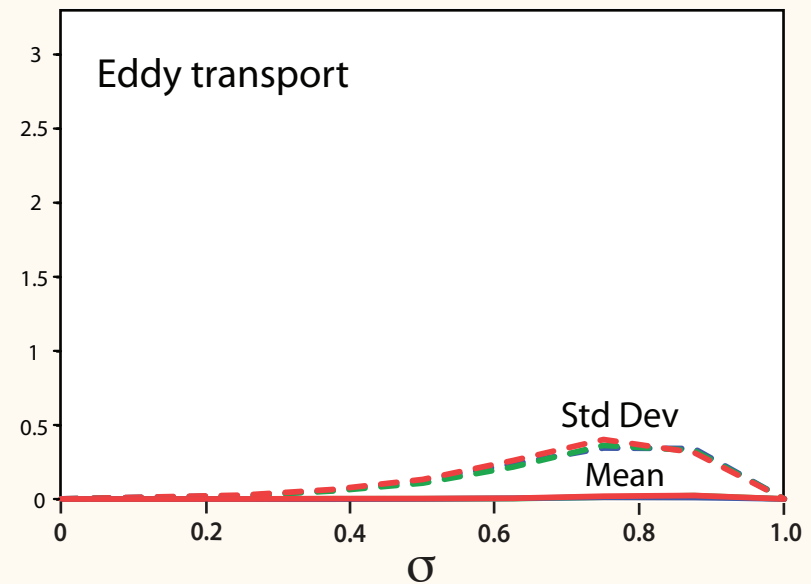
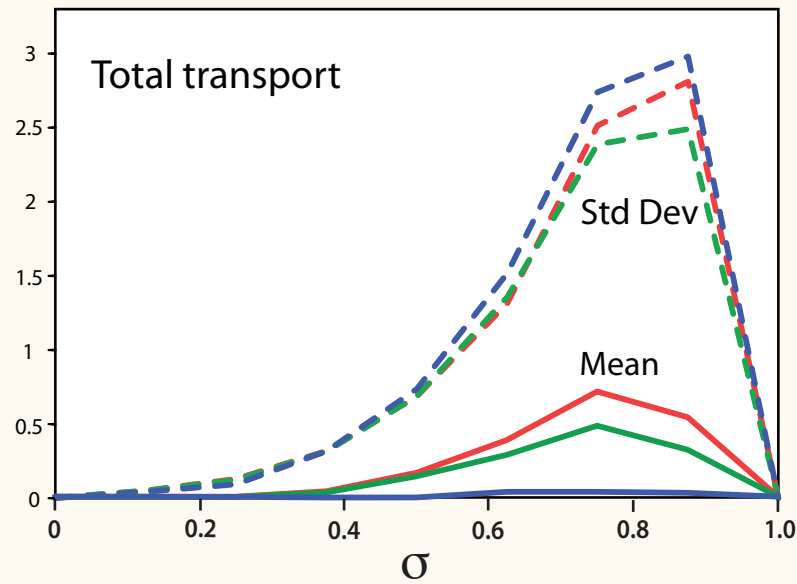


The problem of  
cloud organization

A challenge!

# DIVERGENCE OF THE HORIZONTAL TRANSPORT OF $h$

Shear case  $d = 8$  km



—  $z = 0.5$  km    - -  $z = 1$  km    - -  $z = 2$  km

Divrgence of the eddy transport is much smaller than that of the total transport in both means and standard deviations.

## SUMMARY AND CONCLUSIONS

The unified parameterization (UP) *generalizes* conventional parameterization including the transition to explicit simulation of cloud processes.

UP eliminates the assumption of  $\sigma \ll 1$ , distinguishing the cloud environment from the grid-cell mean.

Eddy transport in UP decreases as  $\sigma \rightarrow 1$  and, therefore, the adjustment to a neutral state is relaxed for large  $\sigma$ .

UP determines  $\sigma$  for each realization.

Outstanding problems in conventional parameterization (e.g., determination of cloud properties, cloud spectrum, cloud organization, . . .) remain important in UP.