

A landscape photograph showing a golden field in the foreground, a line of green trees in the middle ground, and a bright blue sky with scattered white clouds. The text is overlaid on the sky and trees.

Whistlestop Tour: Land-Surface Modeling & the Global Carbon Cycle

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Energy Budget Concept

- **Energy In – Energy Out = Change in Energy**
- **For the land surface,**
 - **Energy in = Radiation**
 - **Energy Out = Radiation + Turbulent fluxes of “sensible” and “latent” heat**
 - **Change in energy = changes in temperature of soil, plants, water, & air**

Land Surface Energy Budget

- Very little of the energy gained by net radiation is stored in the ground (**G**)
- Most is emitted as LW IR and turbulent fluxes of sensible (**H**) and latent heat (**LE**)
- Latent energy is then **released into atmosphere when vapor condenses**

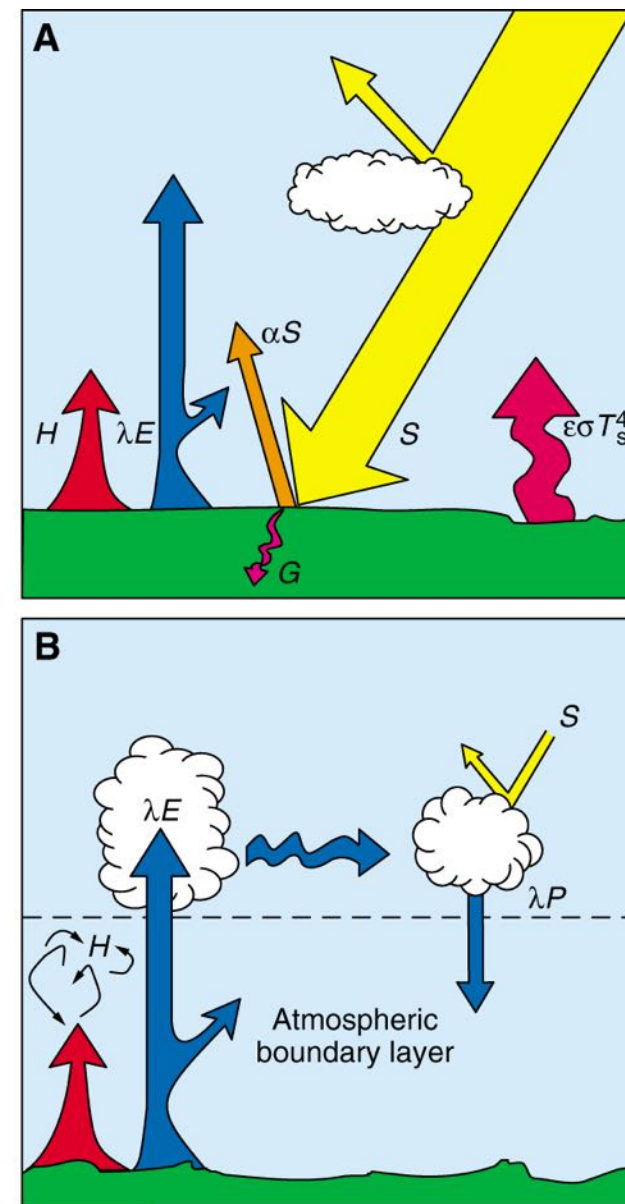


Fig. 1. Interactions between the land surface and the atmosphere that have direct impacts on the physical climate system. **(A)** Surface radiation budget. **(B)** Effect of heat fluxes on the atmosphere.

Surface Energy Budget

Storage change = Energy in – energy out

$$\rho c \frac{\Delta T}{\Delta t} \Delta z = (S \downarrow - S \uparrow + L \downarrow - L \uparrow) - H + \lambda E = G$$

$$R_{net} = (S \downarrow - S \uparrow) + (L \downarrow - L \uparrow) = H + \lambda E + G$$

net SW

net LW

*sensible
heat flux*

*Latent heat
of vaporization*

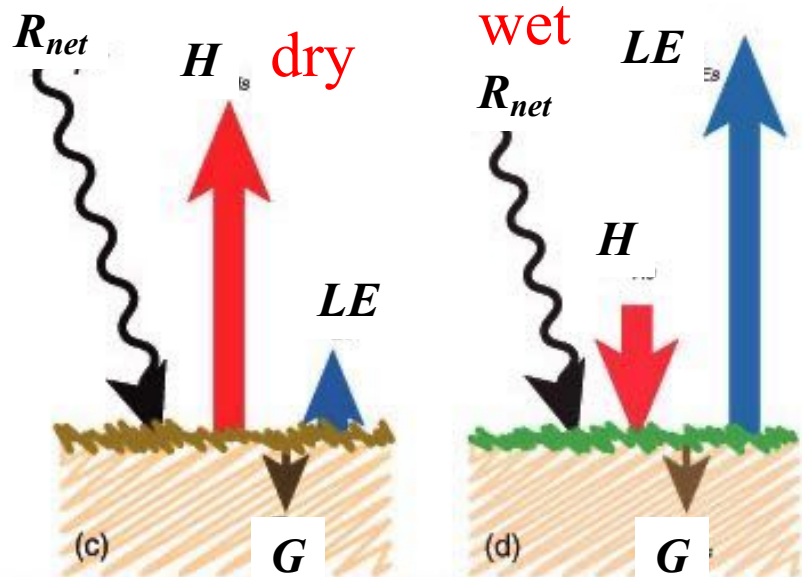
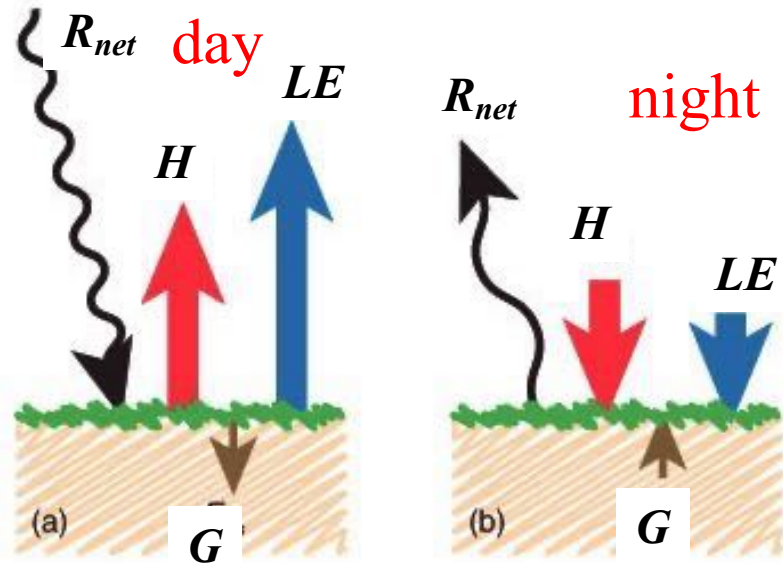
evap

*ground
heat
flux*

Role of the land surface:

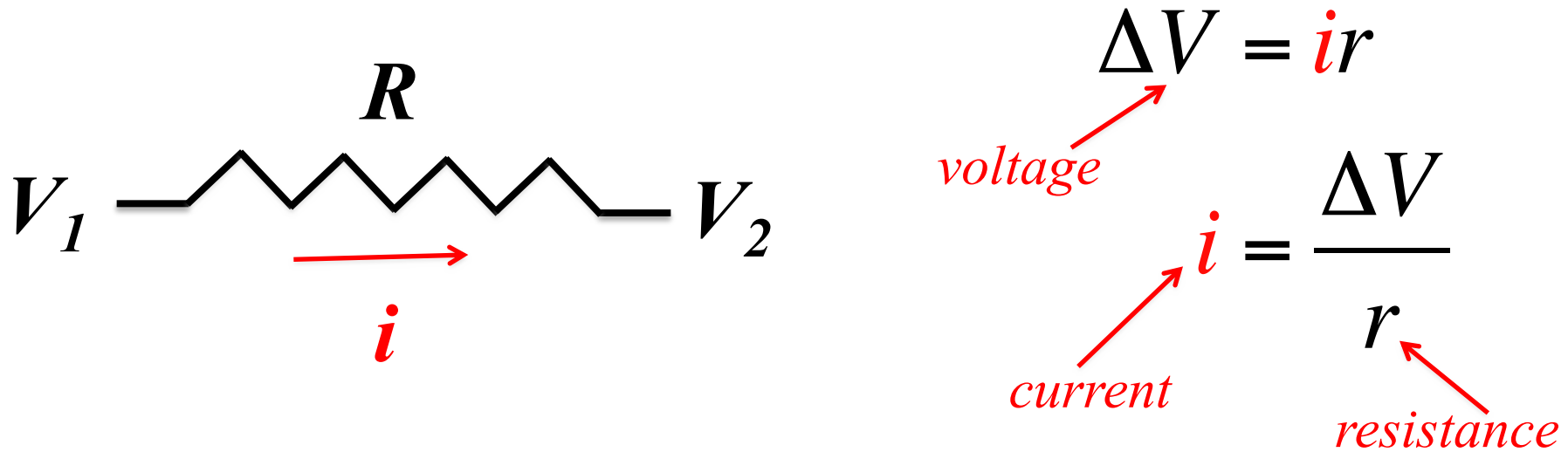
**Partition of net radiation into
turbulent fluxes & storage**

Surface Energy Budgets



- $R_{net} = H + LE + G$
 $\sim H + LE$
- Daytime turbulent fluxes upward
- Night: turbulent fluxes downward (dew or frost!)
- Dry surfaces
 $R_{net} \sim H$
- Wet surfaces
 $R_{net} \sim LE$

Heat Fluxes ~ Currents



- **Sensible heat flux**
 - Driving potential is a difference in temperature
 - **H** is proportional to ΔT
- **Latent heat flux**
 - Driving potential is a difference in vapor pressure
 - **LE** is proportional to Δe

Sensible Heat Flux

- Driving potential is a difference in temperature
- **H** is proportional to ΔT

$$H = \rho c_p \frac{\Delta T}{r} = \rho c_p \frac{T_s - T_a}{r}$$

Watts m⁻² density kg m⁻³ heat capacity 1004 J K⁻¹ kg⁻¹ aerodynamic resistance s m⁻¹

$$\frac{(\text{kg m}^{-3})(\text{J K}^{-1} \text{kg}^{-1})(\text{K})}{(\text{s m}^{-1})} = \frac{(\cancel{\text{kg}} \text{ m}^{-3})(\cancel{\text{J}} \cancel{\text{K}^{-1}} \cancel{\text{kg}^{-1}})(\cancel{\text{K}})}{(\text{s m}^{-1})} = \frac{\text{J s}^{-1}}{\text{m}^2} = \text{W m}^{-2}$$

Latent Heat Flux

- Driving potential is a difference in water vapor pressure
- **LE** is proportional to Δe

$$LE = \frac{\rho c_p}{\gamma} \frac{\Delta e}{r} = \frac{\rho c_p}{\gamma} \frac{e_s - e_a}{r}$$

Watts m⁻²

“Psychrometric constant”

$$\gamma = (C_p P) / (0.622 \lambda)$$

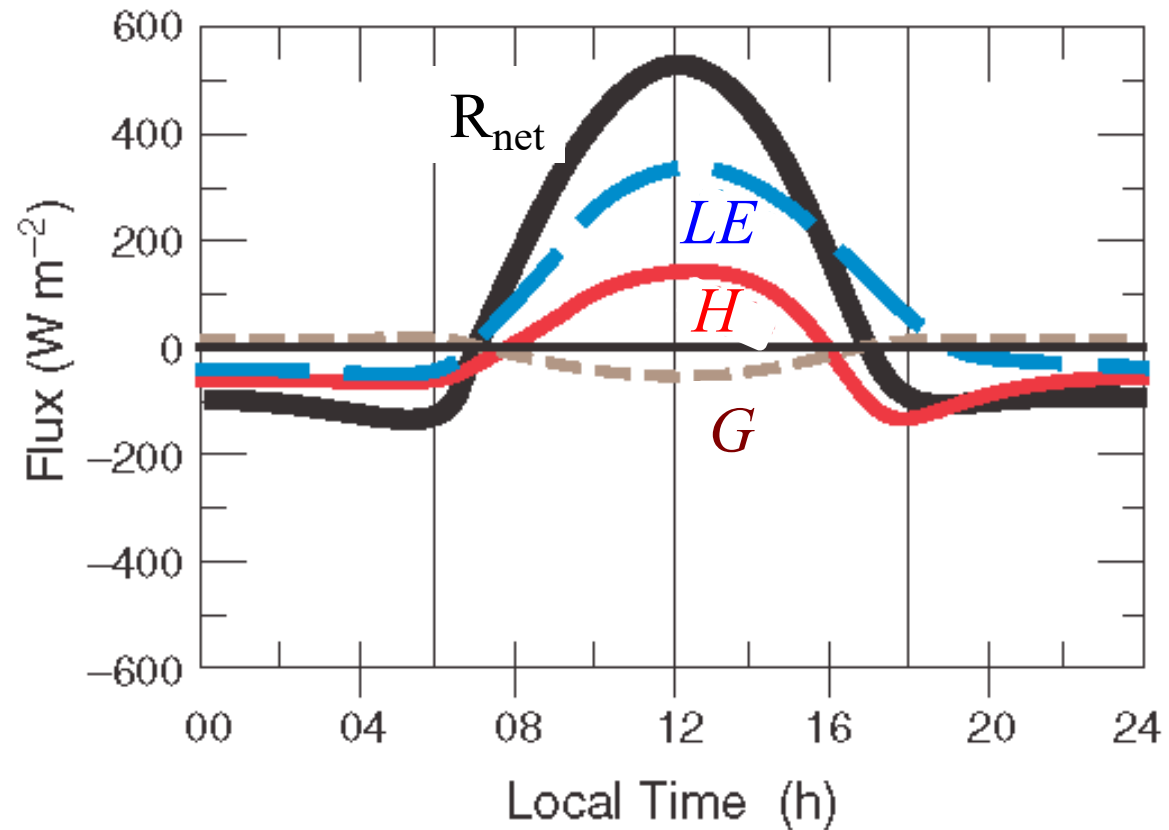
$$66.5 \text{ Pa } ^\circ\text{C}^{-1}$$

aerodynamic
resistance

$$\text{s m}^{-1}$$

Idealized Diurnal Cycle

- R_{net} follows $\cos(z)$ during day, negative at night (LW cooling)
- Downward turbulent fluxes at night
- Ground heat flux smaller: downward during day and up at night



$$R_{\text{net}} = H + LE + G$$
$$\sim H + LE$$

Partition of Net Radiation

Ground heat flux

$$G = k(T_s - T_g)/\Delta z$$

$$R_{net} = (S \downarrow - S \uparrow) + (L \downarrow - L \uparrow) = H + \lambda E + G$$

$$H = -\rho C_p \frac{(T_a - T_s)}{r_H}$$

*Sensible flux
driven by ΔT*

*Latent flux
driven by VPD*

$$\lambda E = -\frac{\rho C_p (e_a - e_*[T_s])}{\gamma r_w}$$

$$\gamma = (C_p P)/(0.622\lambda) \quad 66.5 \text{ Pa } ^\circ\text{C}^{-1}$$

“Psychrometric constant”

Surface Energy Budget

Energy in = energy out + storage change

$$(1 - r)S_{\downarrow} + \epsilon L_{\downarrow} = \epsilon \sigma (T_s + 273.15)^4 + H + \lambda E + G$$

$$(1 - r)S_{\downarrow} + \epsilon L_{\downarrow} = \epsilon \sigma (T_s + 273.15)^4 - \rho C_p \frac{(T_a - T_s)}{r_H} - \frac{\rho C_p (e_a - e_s(T_s))}{\gamma r_w} + k \frac{(T_s - T_g)}{\Delta z}$$

- Can solve for surface temperature
- Physical properties: albedo, emissivity, heat capacity, soil conductivity & temperature
- “Resistances” are properties of the turbulence ... **depend sensitively on H!**

Penman-Monteith Equation

“Thermodynamic” energy balance

$$\lambda E = (R_n - G) - H = (R_n - G) + \rho C_p (T_a - T_s) / r_H$$

“Turbulent” energy balance

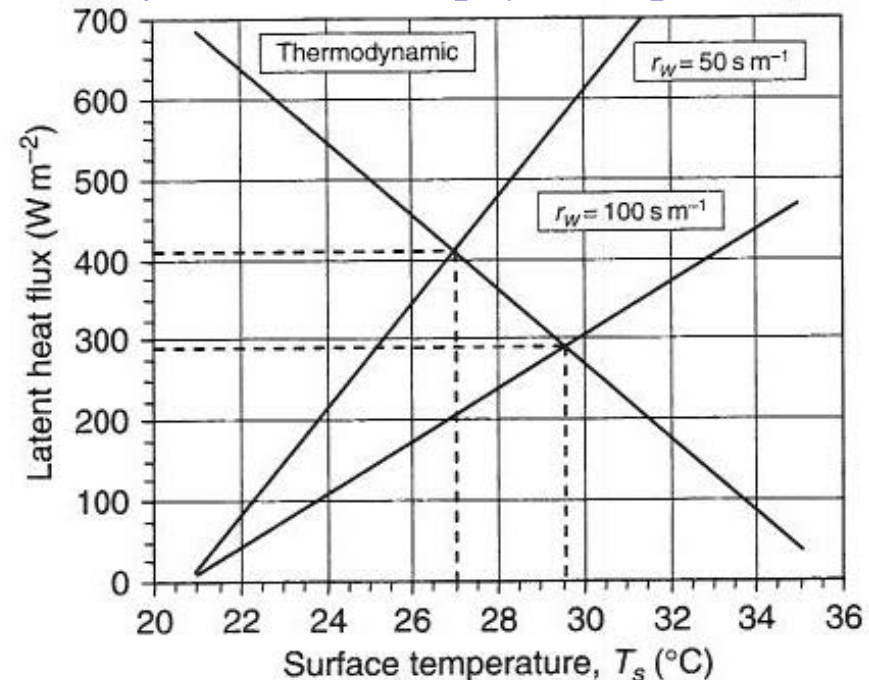
$$\lambda E = \frac{\rho C_p (e_*[T_a] + s(T_s - T_a) - e_a)}{\gamma + r_w}$$

Solve for surface temperature

$$T_s - T_a = (r_H / \rho C_p) (R_n - G - \lambda E)$$

$$e_*[T_s] = e_*[T_a] + s(T_s - T_a)$$

VPD approximated by linearization of Clausius-Clapeyron equation



Solutions to P-M Equation

Latent heat flux

$$\lambda E = \frac{s(R_n - G) + \rho C_p (e_*[T_a] - e_a)/r_H}{s + \gamma(r_W/r_H)}$$

Sensible heat flux

$$H = \frac{(R_n - G)\gamma^* - \rho C_p (e_*[T_a] - e_a)/r_H}{s + \gamma^*}$$

Surface temperature

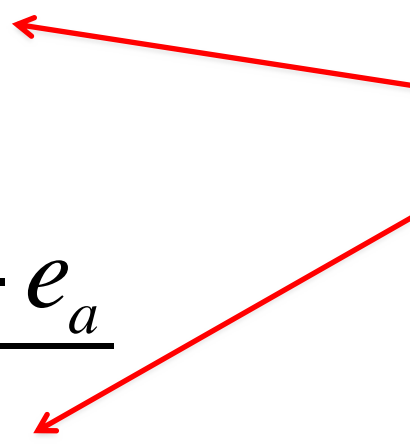
$$T_s = T_a + \frac{(R_n - G)\gamma^* r_H / \rho C_p - (e_*[T_a] - e_a)}{s + \gamma^*}$$

Turbulent Fluxes

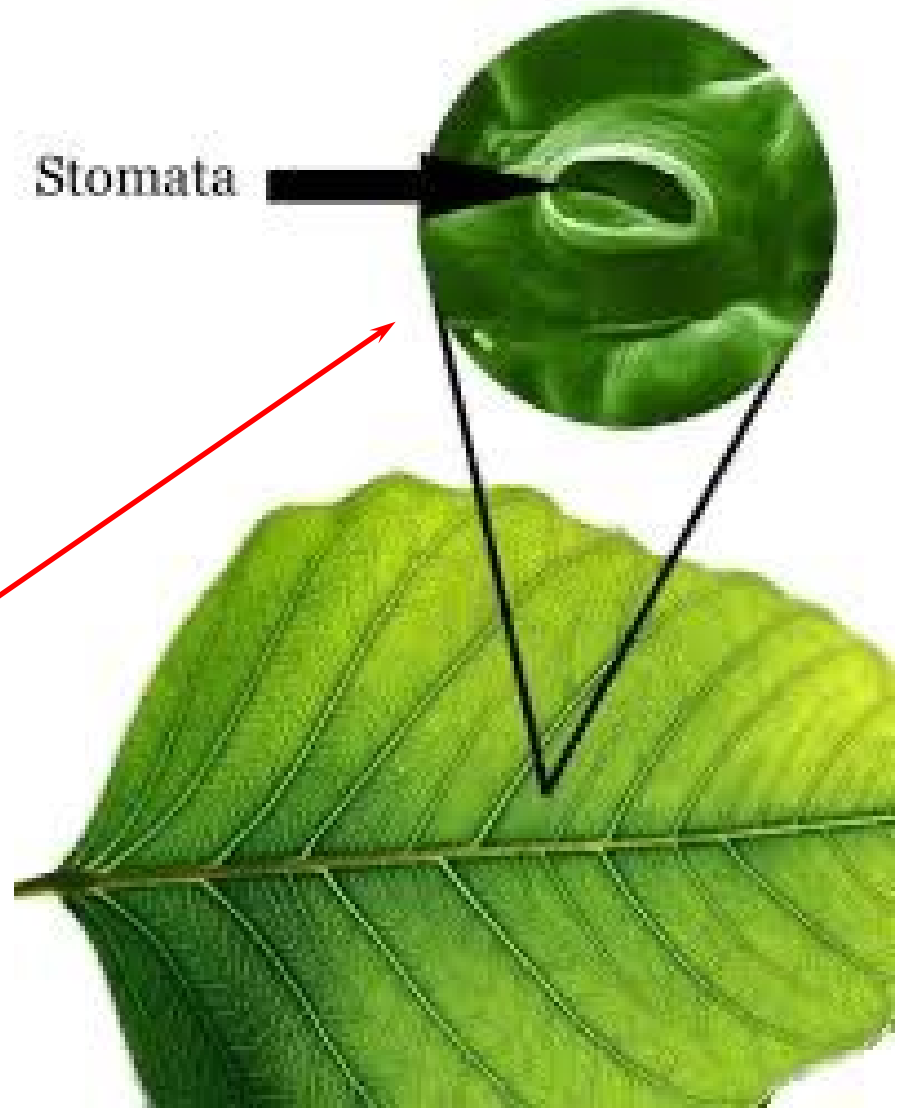
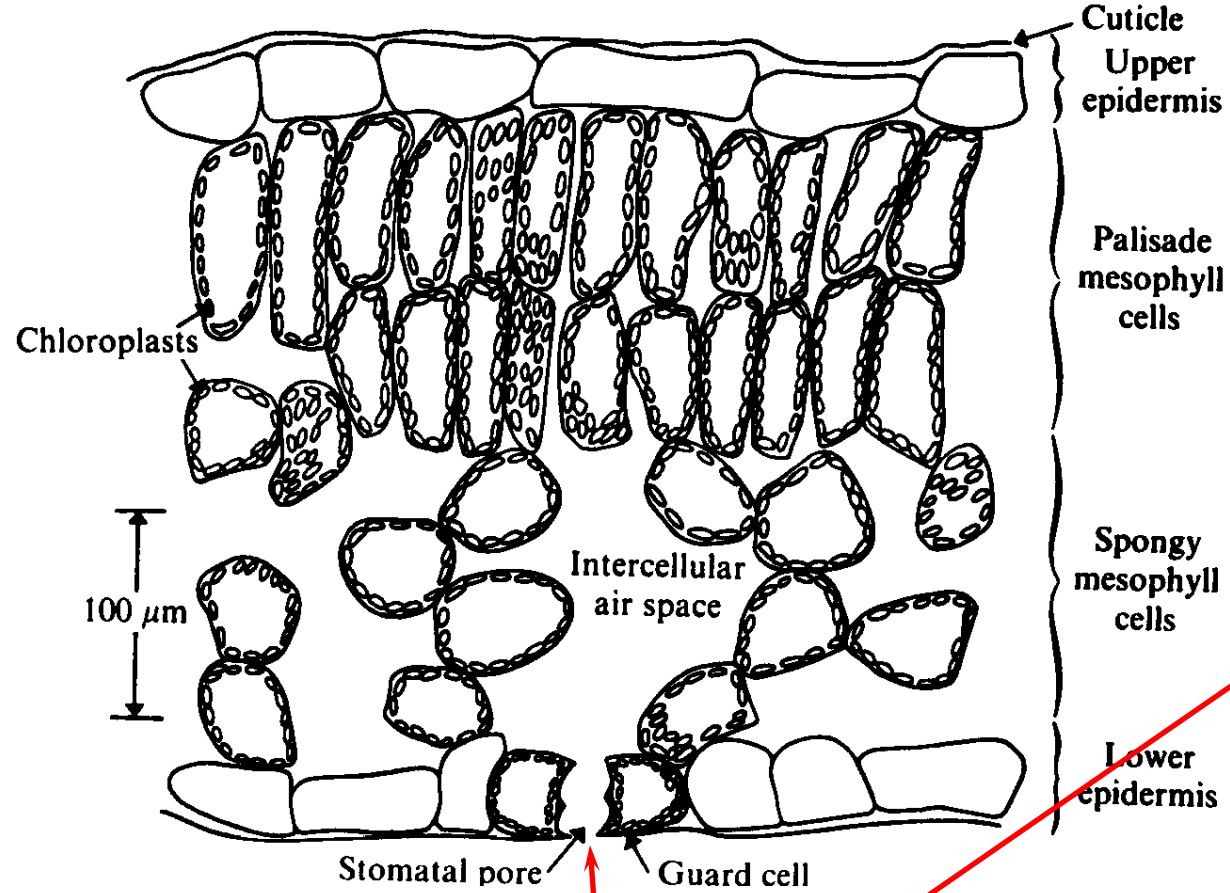
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$$LE = \frac{\rho c_p}{\gamma} \frac{\Delta e}{r} = \frac{\rho c_p}{\gamma} \frac{e_s - e_a}{r}$$

aerodynamic
resistance
 s m^{-1}

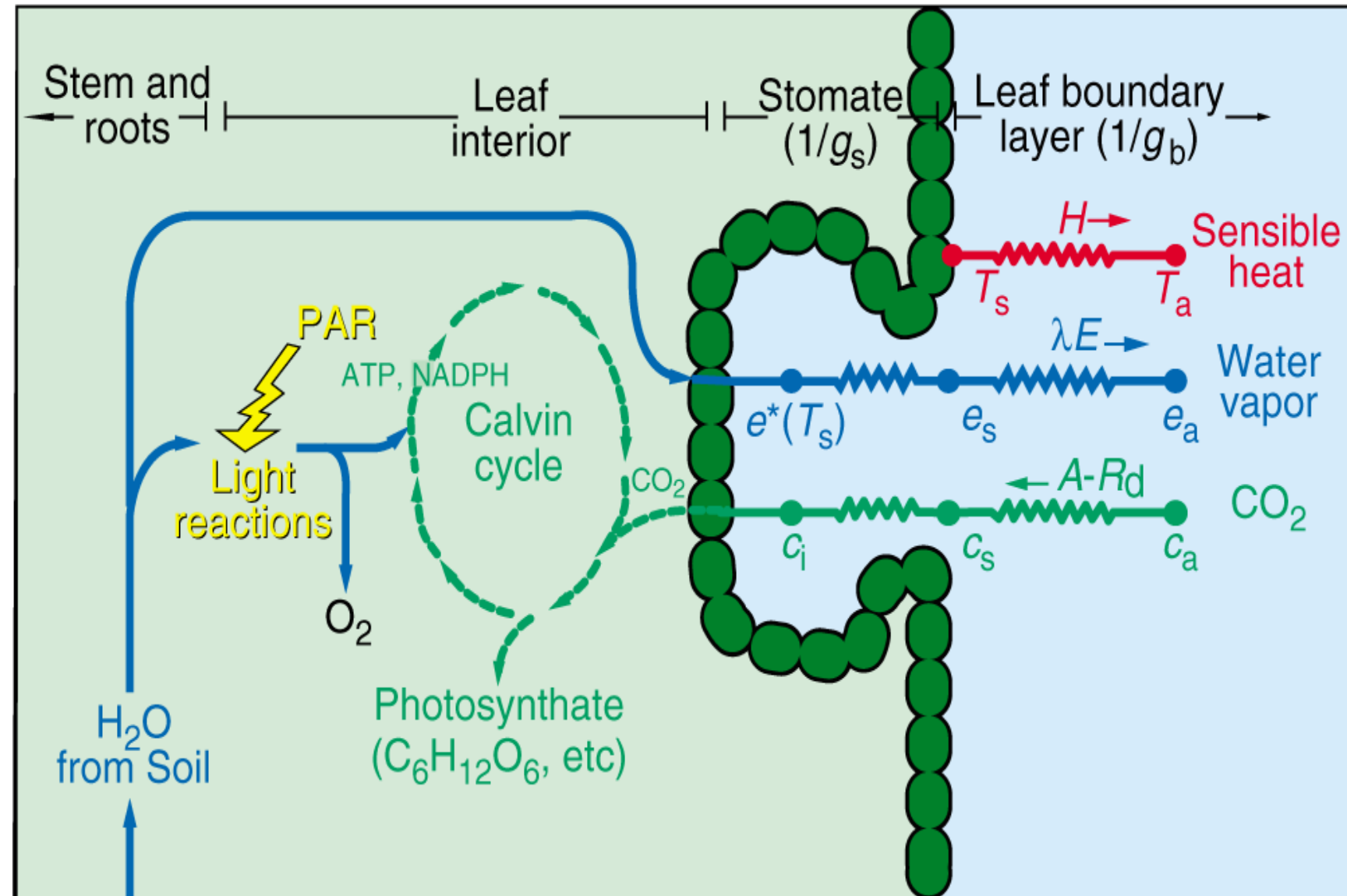


Leaf Anatomy



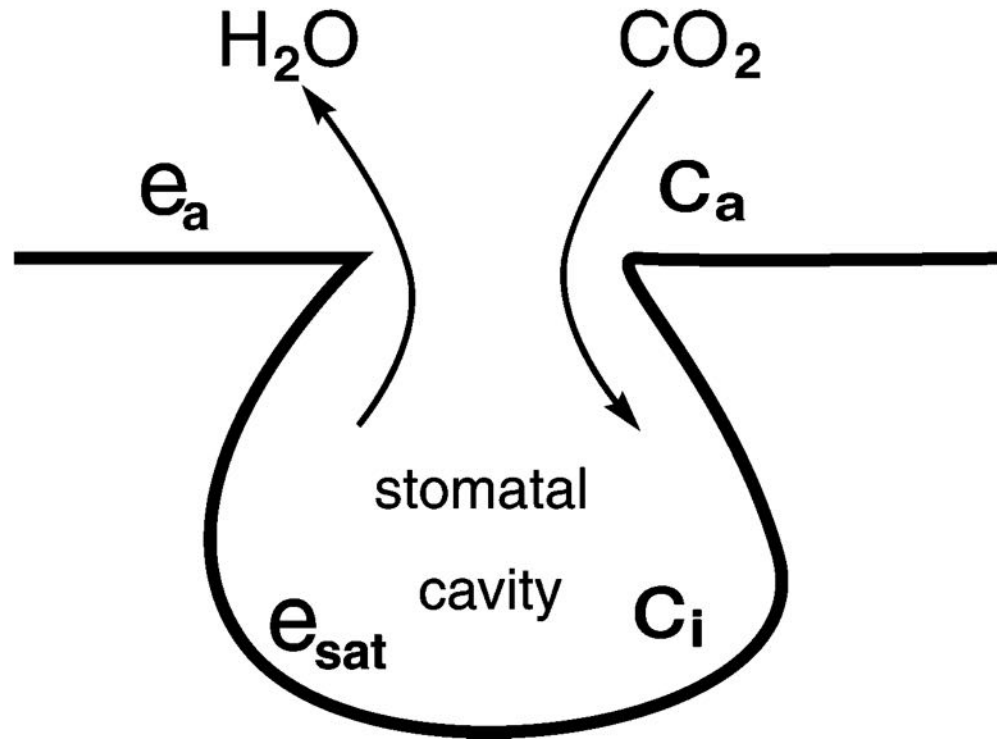
Stomate
(pl. stomata)

Stomatal Physiology



- Heat, water, and carbon fluxes are coupled by physiology
- Scaling to canopy and landscape fluxes based on resource allocation

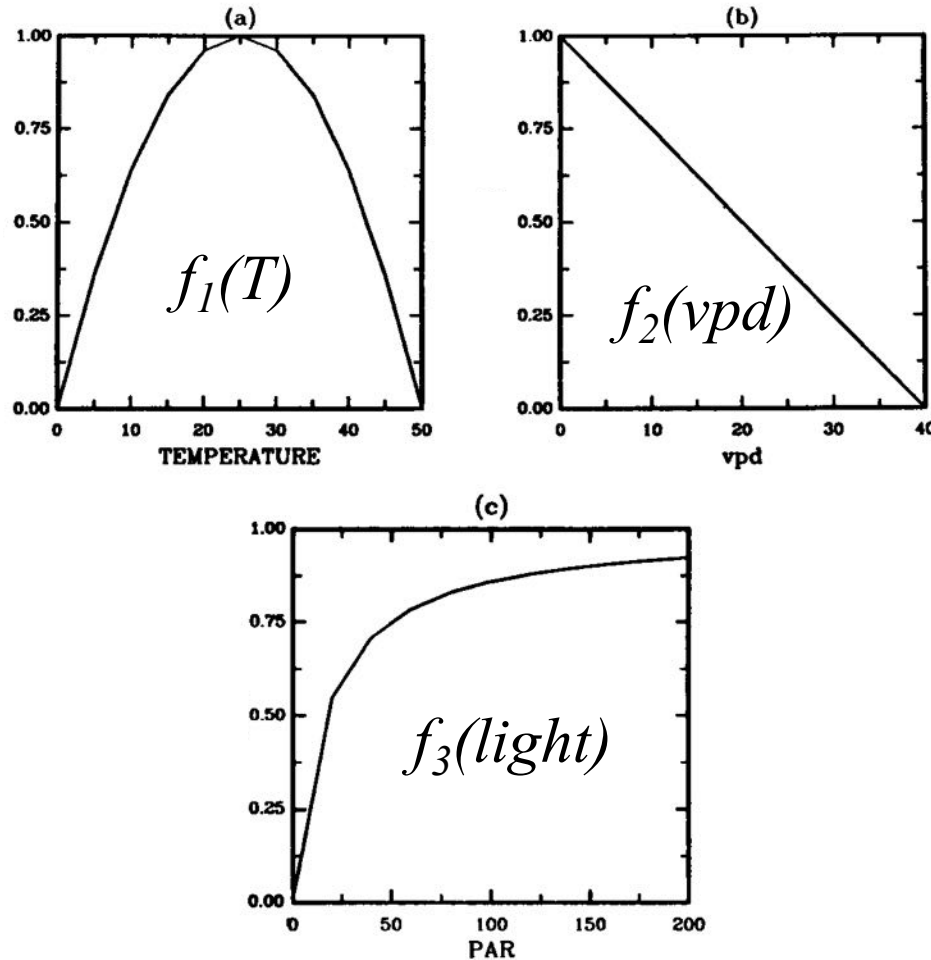
Carbon and Water



- Plants eat CO_2 for a living
- They open their stomata to let CO_2 in
- Water gets out as an (unfortunate?) consequence
- For every CO_2 molecule fixed about 400 H_2O molecules are lost

Canopy Conductance, c. 1990

$$g_s = g_{s,\max} f_1(T) f_2(vpd) f_3(PAR)$$

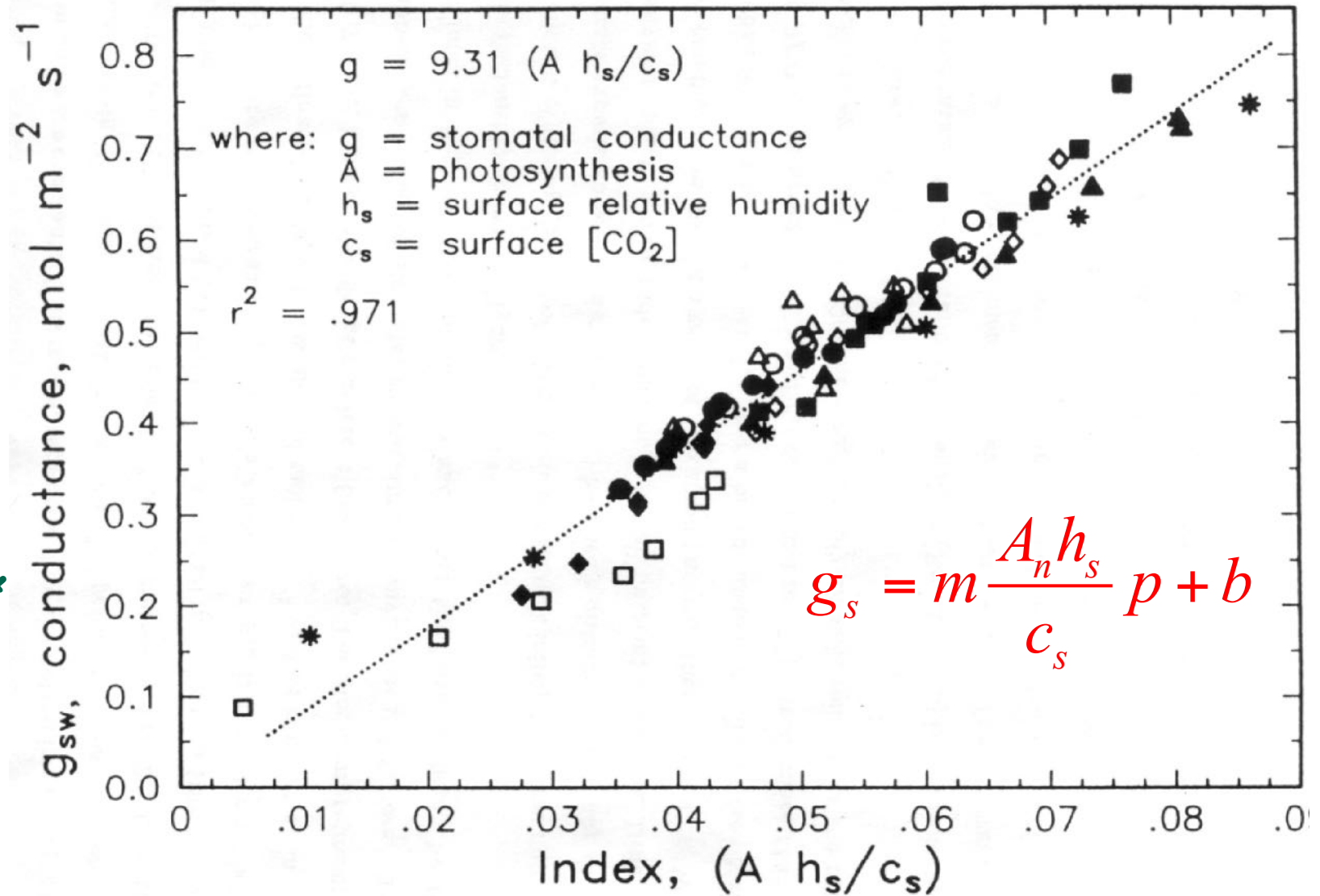
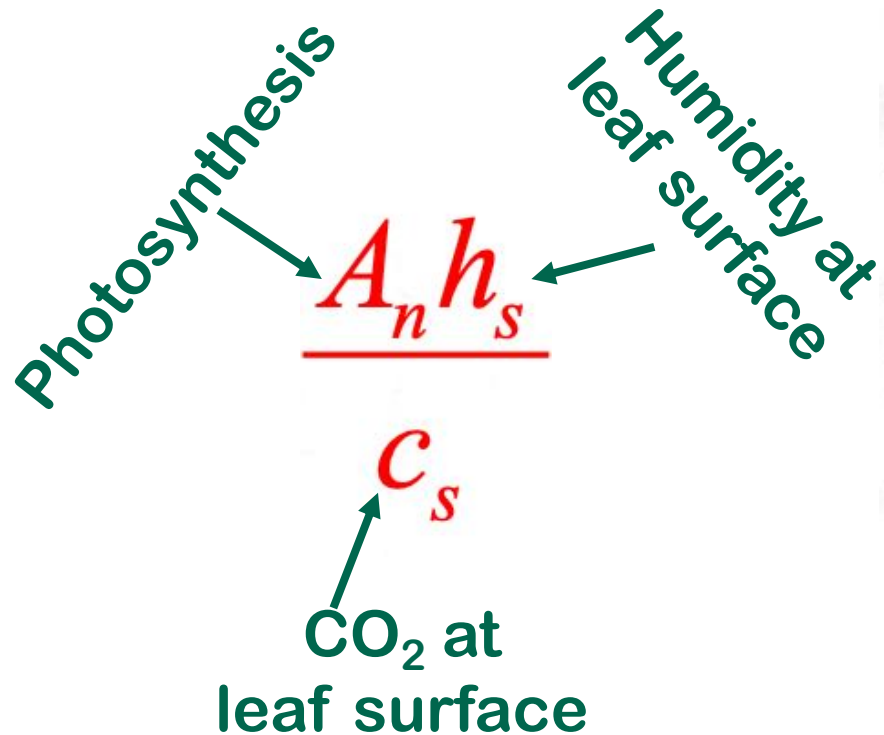


$$\lambda E = \beta \left[\frac{e^*(T_s) - e_r}{r_a + r_c} \right] \frac{\rho c_p}{\gamma}$$

- Maximum conductance scaled down by empirically-derived factors
- Assumed independence of limitations

Ball-Berry Relationship

- Stomatal conductance is linear w/ an index that **reflects plants physiological strategy**
- Light, vpd, leaf temperature effects all collapse among **multiple different species**



Photosynthesis and Conductance

Stomatal conductance is linearly related to photosynthesis:
(The “Ball-Berry-Collatz” parameterization)

$$g_s = m \frac{A_n h_s}{c_s} p + b$$

Diagram illustrating the Ball-Berry-Collatz parameterization for stomatal conductance (g_s). The equation is annotated with red arrows and text:

- g_s : stomatal conductance
- A_n : photosynthesis
- h_s : RH at leaf sfc
- c_s : CO2 at leaf sfc

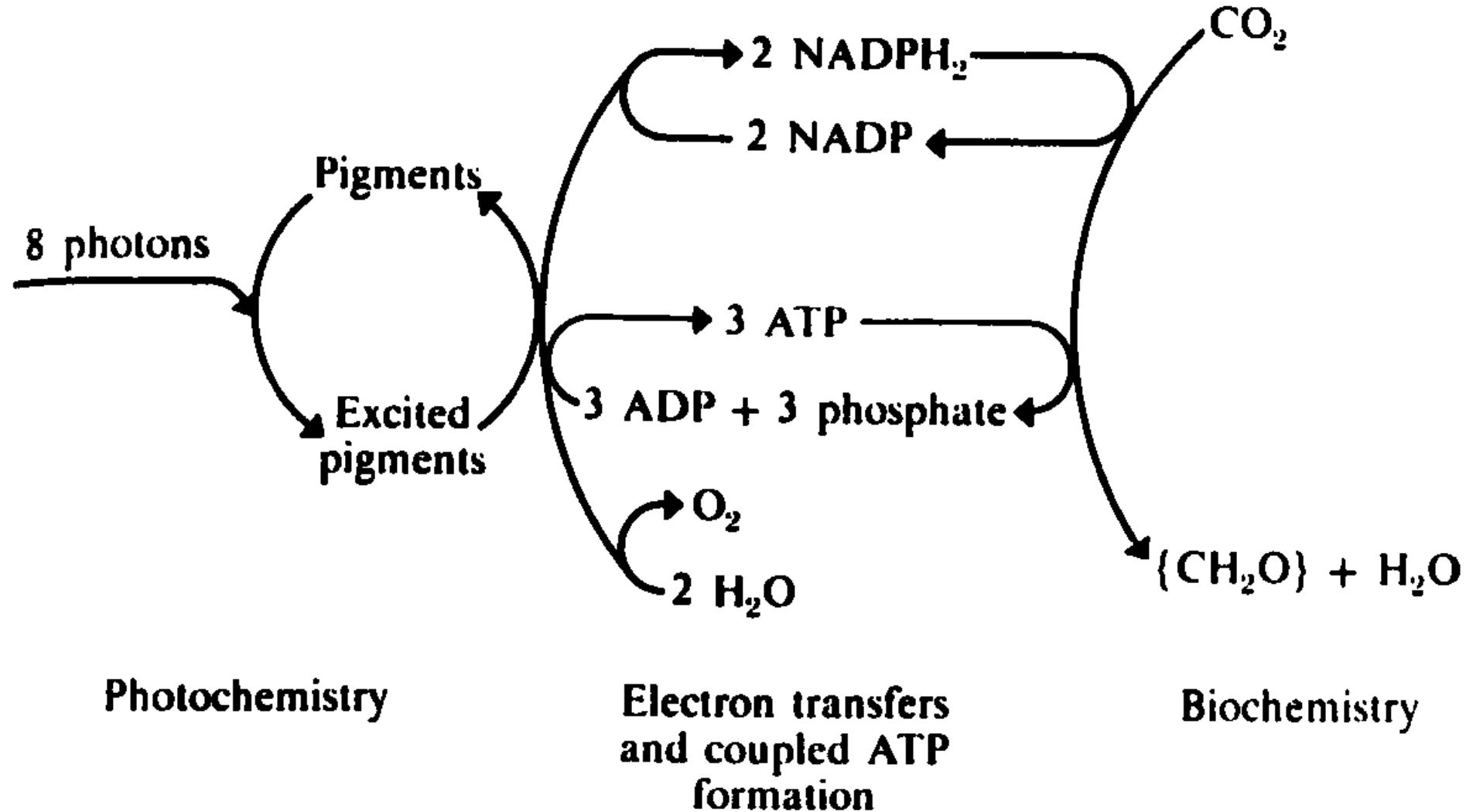
Photosynthesis is controlled by three limitations
(The Farquahar-Berry model):

$$A_n = \min(A_C, A_L, A_S) - R_d$$

Diagram illustrating the Farquahar-Berry model for photosynthesis (A_n). The equation is annotated with red arrows and text:

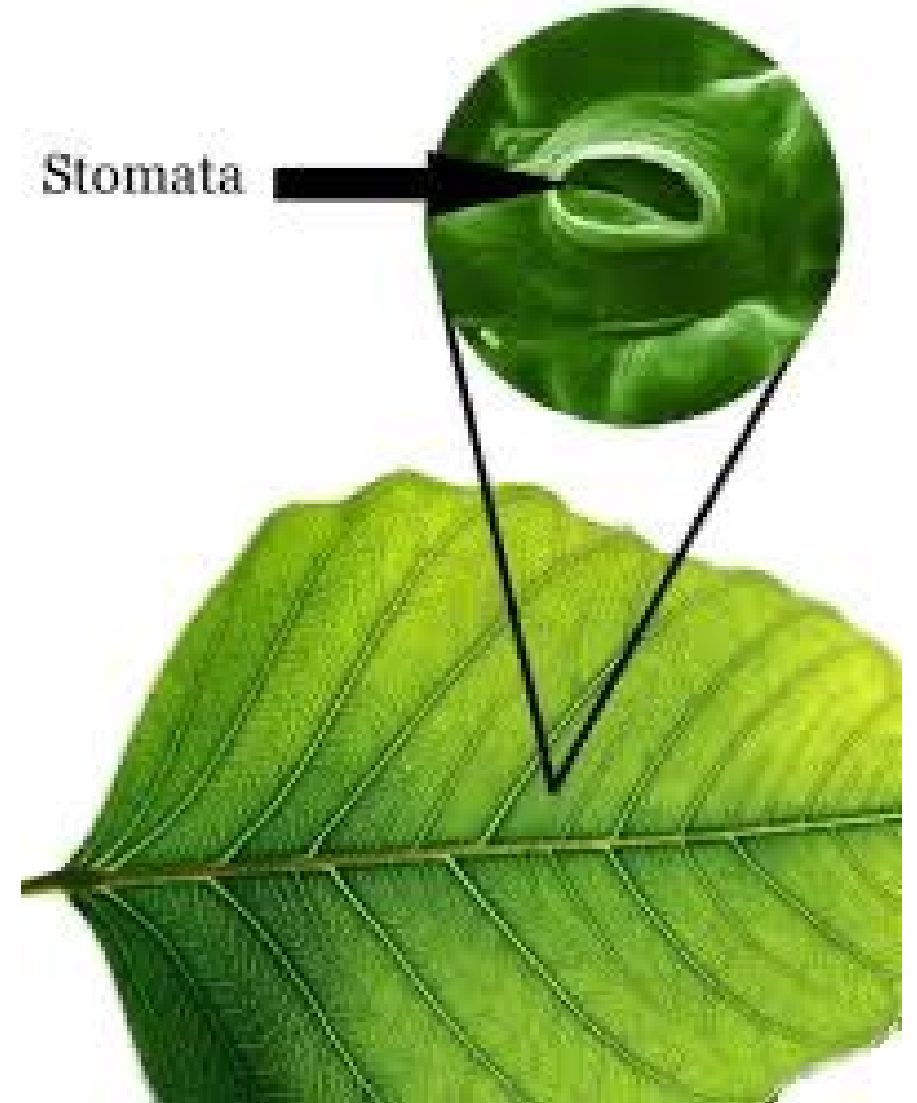
- A_C : Enzyme kinetics (“rubisco”)
- A_L : Light
- A_S : Starch

Light and Dark



Canopy Integration

- Photosynthesis and transpiration are linked via stomatal conductance
- Mechanistic understanding of biophysics for **leaf-level fluxes**
- How to **integrate to entire canopy?**
 - Could multiply fluxes ($\text{mol m}^{-2} \text{s}^{-1}$) at leaf level by **total leaf-area index**
 - That would **assume all leaves have same properties and physical environment**
 - What about **shading** inside canopy?
 - **How does a plant respond to shading over time?**





to
Boldy Go



Canopy Integration

$$\frac{I(L)}{I_0} = e^{-kL}$$

L = "cumulative LAI"
(vertical coordinate)

$$k = \frac{G(\mu)}{\mu}$$

$G(\mu)$ = projected LAI
normal to beam

$$A_{canopy} = A_{sun-leaf} \int_0^{L_T} e^{-kL} dL$$
$$= A_{sun-leaf} \left[\frac{-(e^{-kL_T} - 1)}{k} \right]$$

$$= A_{sun-leaf} \Pi$$

$$\Pi \equiv \frac{1 - e^{-kL_T}}{k} = \frac{FPAR}{k}$$

- How to efficiently integrate leaf-level equations across all **leaf angles and light levels?**
- Assume light levels drop off inside canopy according to **Beer's Law**
- Maximum photosynthesis rate (V_{max}) depends on **Rubisco**, an enzyme used to catalyze C fixation
- Rubisco is mostly **nitrogen** (most abundant protein on Earth)
- Assume **plant allocates scarce N where it will yield the most C gain (following time-mean light!)**

Canopy scaling factor $\Pi \sim FPAR$... get by remote sensing

C₃ and C₄ Photosynthesis

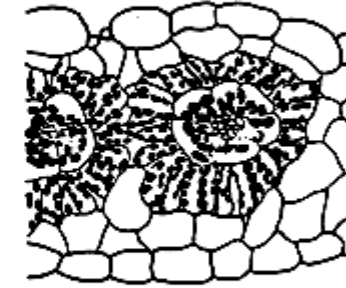
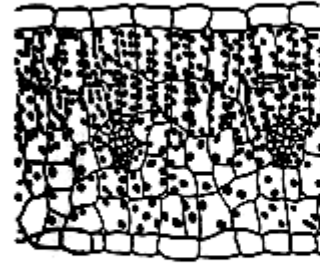
- Most plants produce sugars by the pathway outlined above, in which the first organic compounds have three carbon atoms (C₃)
- Some tropical and subtropical plants have evolved a separate mechanism in which the first products have four carbon atoms (C₄)
- C₄ photosynthesis is a **mechanism to overcome photorespiration** (high O₂/CO₂ ratio, high T)
- Involves **active transport** of dissolved CO₂ to specialized “bundle-sheath” cells to overwhelm O₂ at Rubisco active sites
- Uses energy to do this ... **only “pays off” when photorespiration is a big problem**
- Evolved only ~ 10 My ago, when CO₂ levels dropped



C₃ vs C₄ Differences

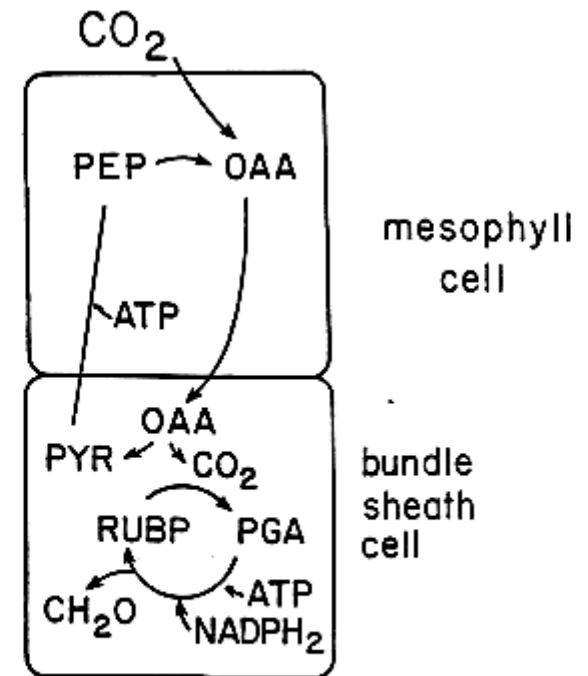
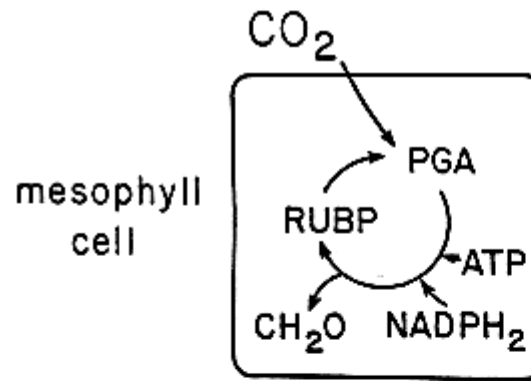
Physiology

distributed chloroplasts



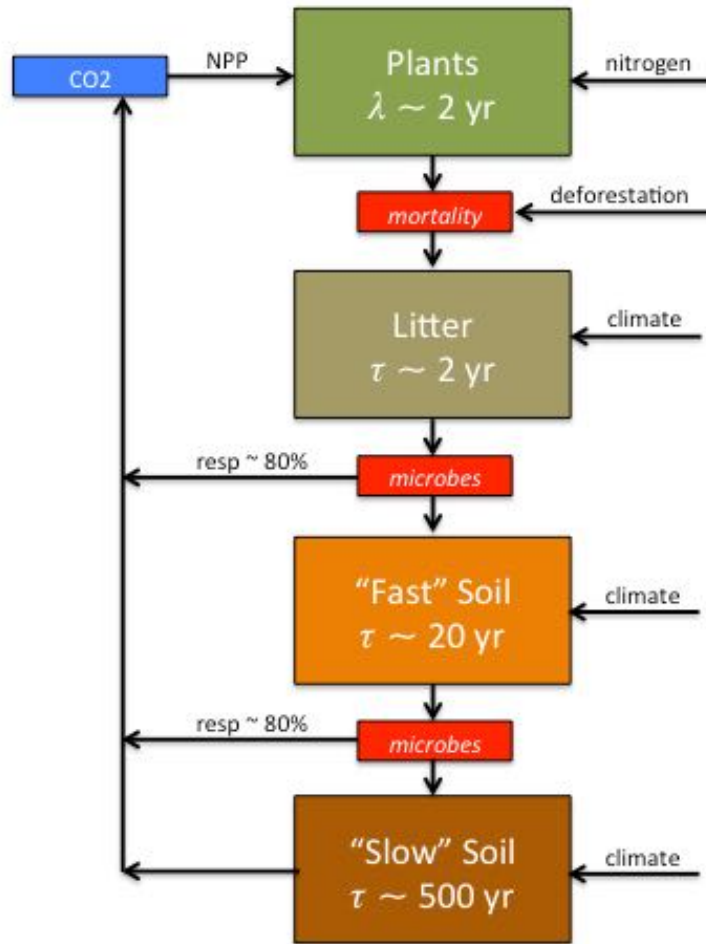
bundle sheath

Biochemistry



Cascading Carbon Pools

Conceptual Model



Mathematical Model

$$\frac{dP}{dt} = NPP - MORT$$

$$\frac{dL}{dt} = MORT - \frac{L}{\tau_L} Q_{10}^{\frac{T-T_0}{10}}$$

$$\frac{dF}{dt} = \left[\frac{L}{\tau_L} (1 - \epsilon) - \frac{F}{\tau_F} \right] Q_{10}^{\frac{T-T_0}{10}}$$

$$\frac{dS}{dt} = \left[\frac{F}{\tau_F} (1 - \epsilon) - \frac{S}{\tau_S} \right] Q_{10}^{\frac{T-T_0}{10}}$$

Symbols used:

- NPP = Net primary production (photosynthesis minus plant respiration, in GtC/yr)
- MORT = plant mortality (transfers carbon from live plants to dead litter, GtC/yr)
- τ_L, τ_F, τ_S = turnover time for carbon in litter, fast, and slow soil pools (years)
- ϵ = efficiency of microbial respiration (fraction of what they "eat" that turns into CO₂)
- Q_{10} = fractional increase in decomposition rates per 10 degrees of warming
- T = temperature (Celsius), prescribed from a [simple climate model](#) using the IPCC SRES A2 emissions scenario.

- Plants grow logistically limited by nutrients
- Carbon from dead plants becomes litter
- Litter decomposes quickly into fast and then slow soil organic matter



The Oceans

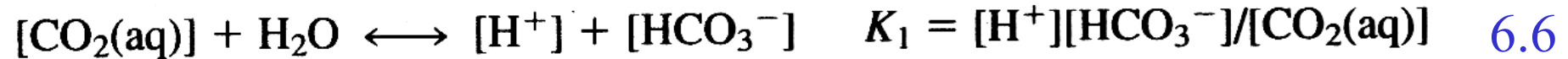
Carbonation



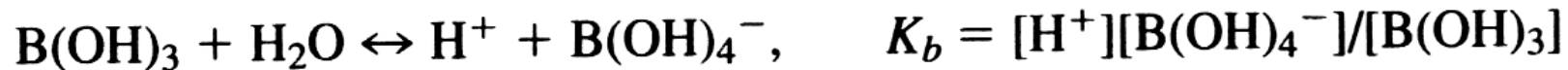
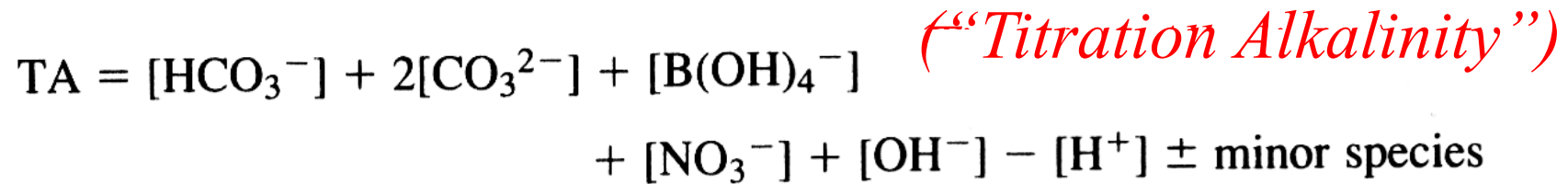
- CO_2 dissolves in water to make carbonic acid
- That's why beer goes with pizza and Chardonnay goes with Brie
- Dissolves twice as well in cold water as warm water
- That's why beer & soda go flat when they warm up
- Cold polar ocean soaks up CO_2 , warm tropical oceans release it

Carbonate Equilibria

Three equations (equilibria) in five unknowns



Add two more constraints

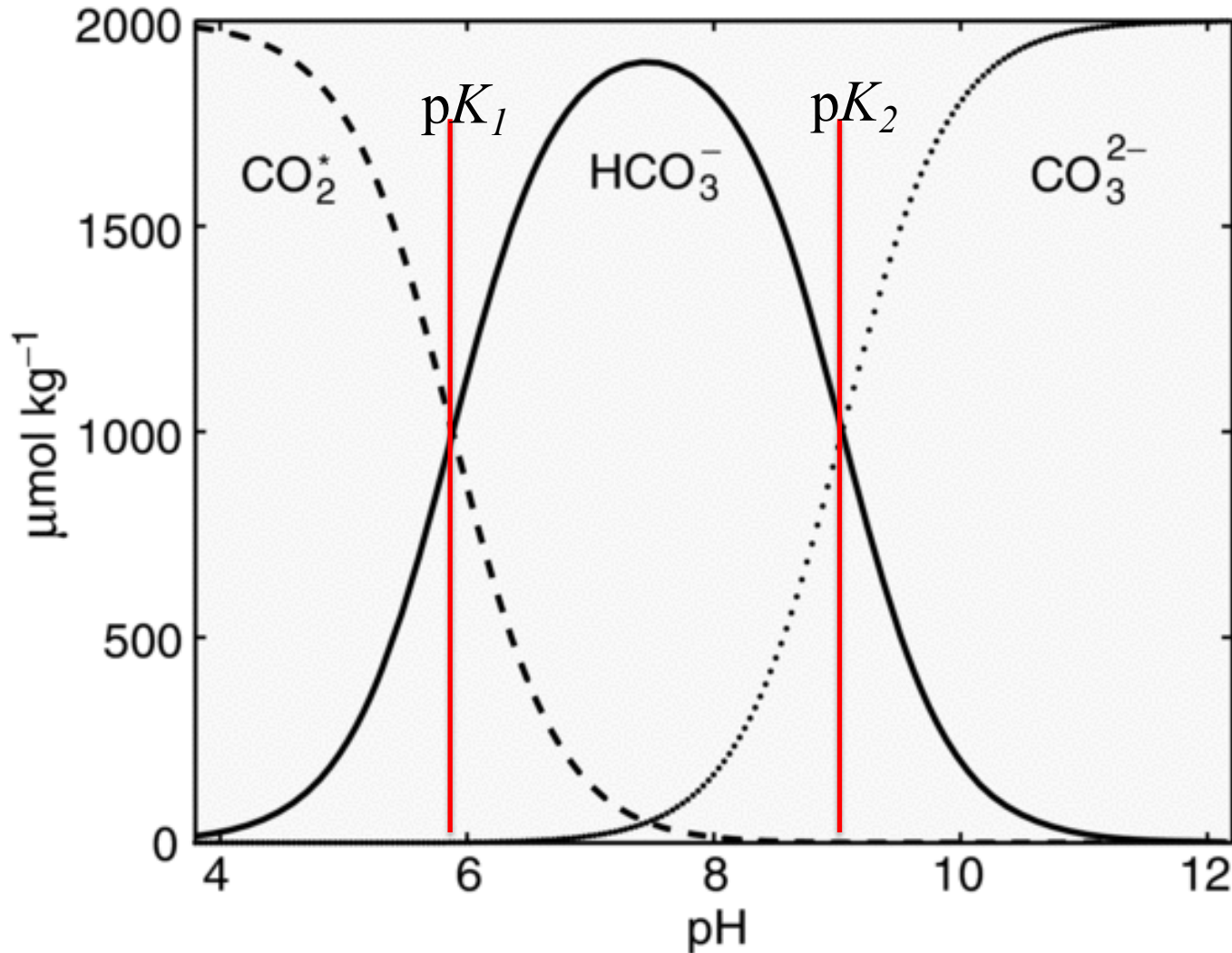


(Boric acid dissociation)

$$\Sigma B = 1.179 \times 10^{-5} S \text{ mol/kg} \\ (\text{S} = \text{Salinity})$$

Speciation vs pH

“Bjerrum Plot”



Williams_Fig. 6.7

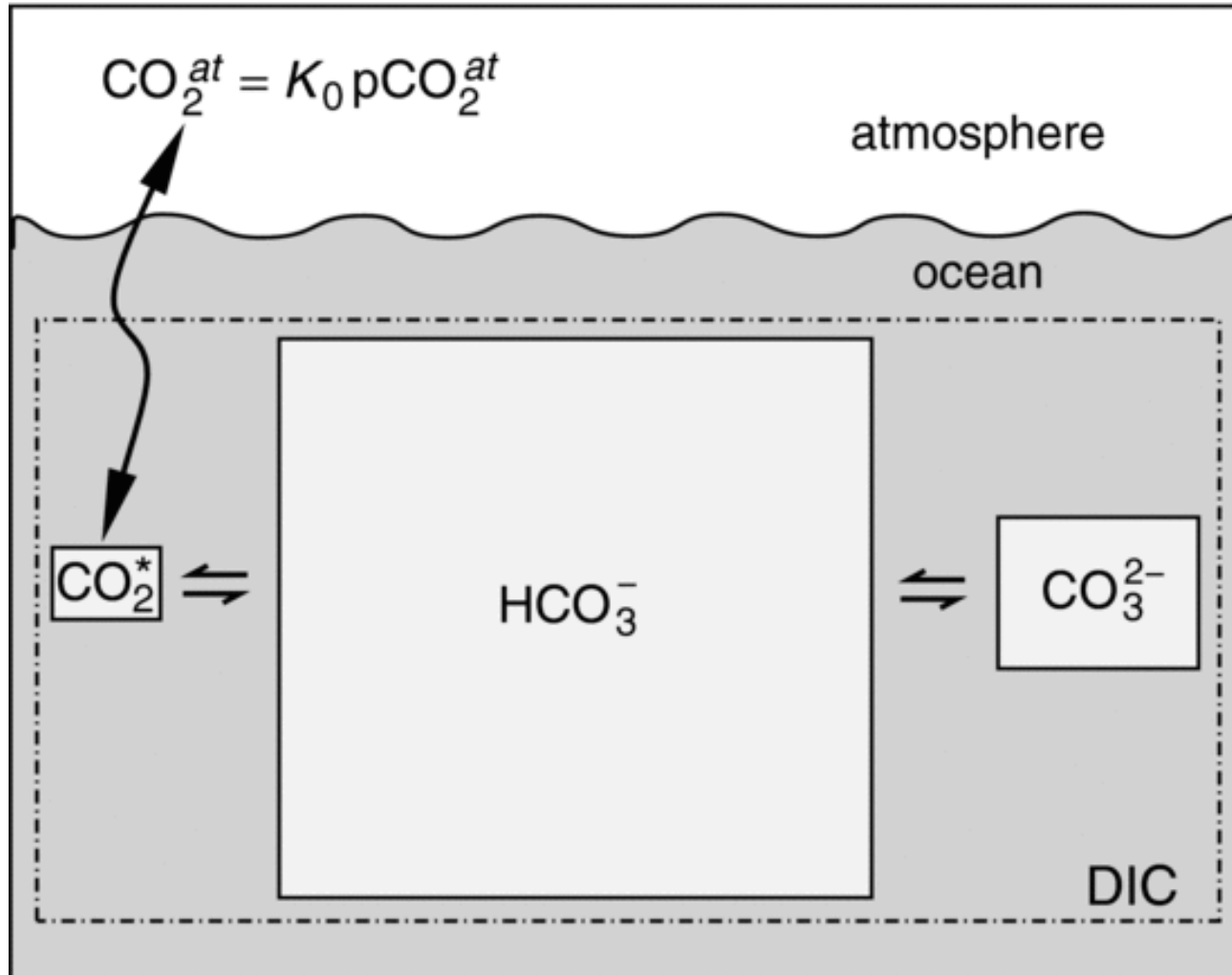
$$[\text{CO}_2^*] = 10 \mu\text{Mol kg}^{-1}$$

$$[\text{HCO}_3^-] = 1769 \mu\text{Mol kg}^{-1}$$

$$[\text{CO}_3^{2-}] = 223 \mu\text{Mol kg}^{-1}$$

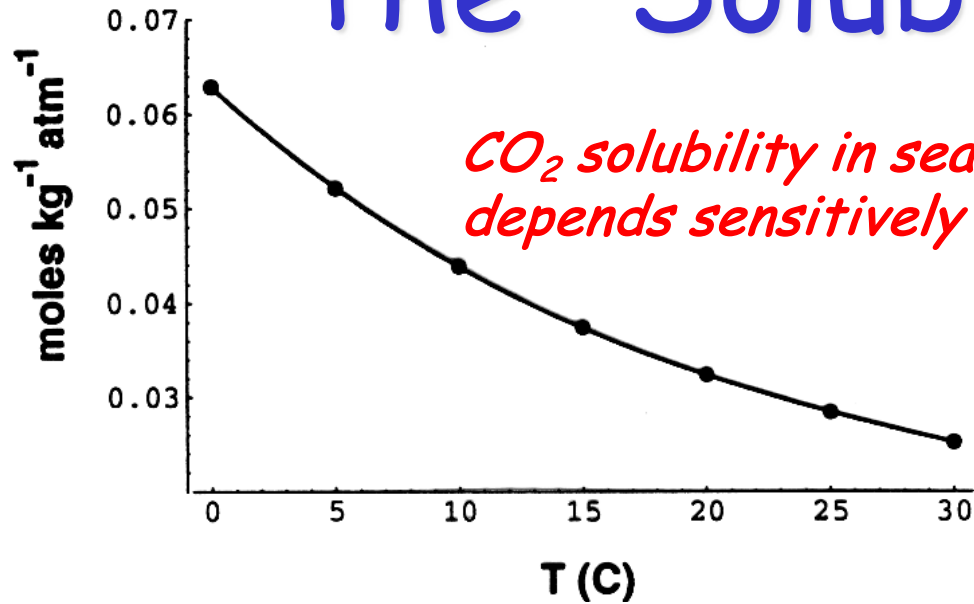
By far most dissolved CO₂ in the oceans is bicarbonate

Buffering of Marine DIC

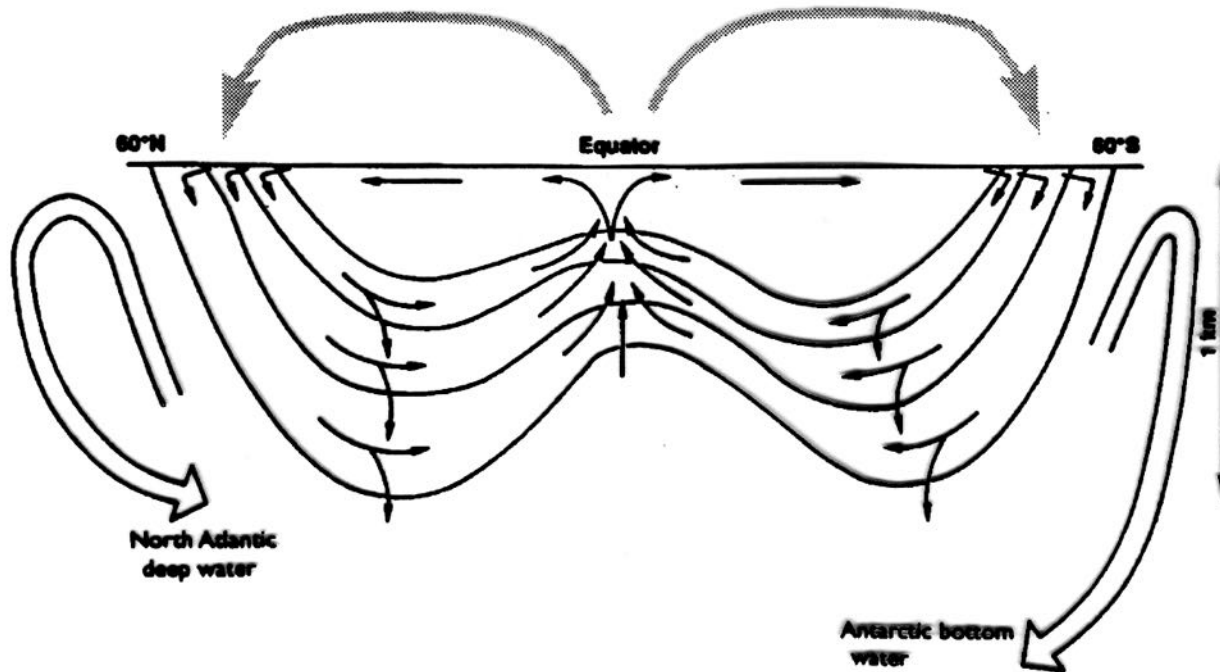


Only a small fraction of DIC (CO_2^*) is in chemical equilibrium with atmospheric CO_2

The “Solubility Pump”

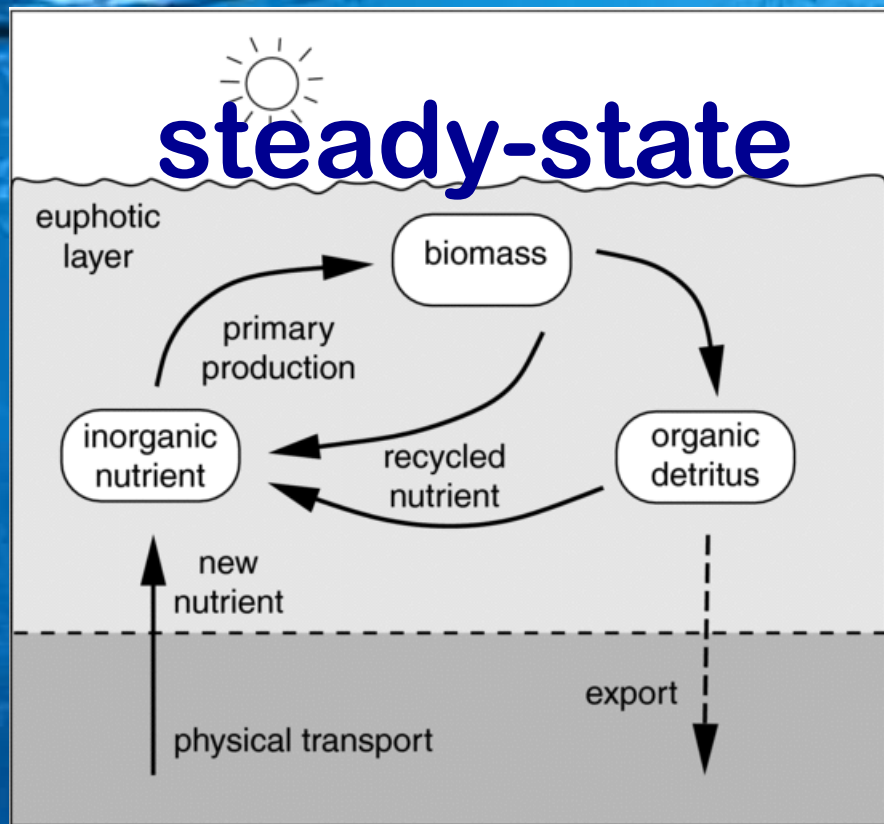


CO₂ solubility in seawater depends sensitively on SST

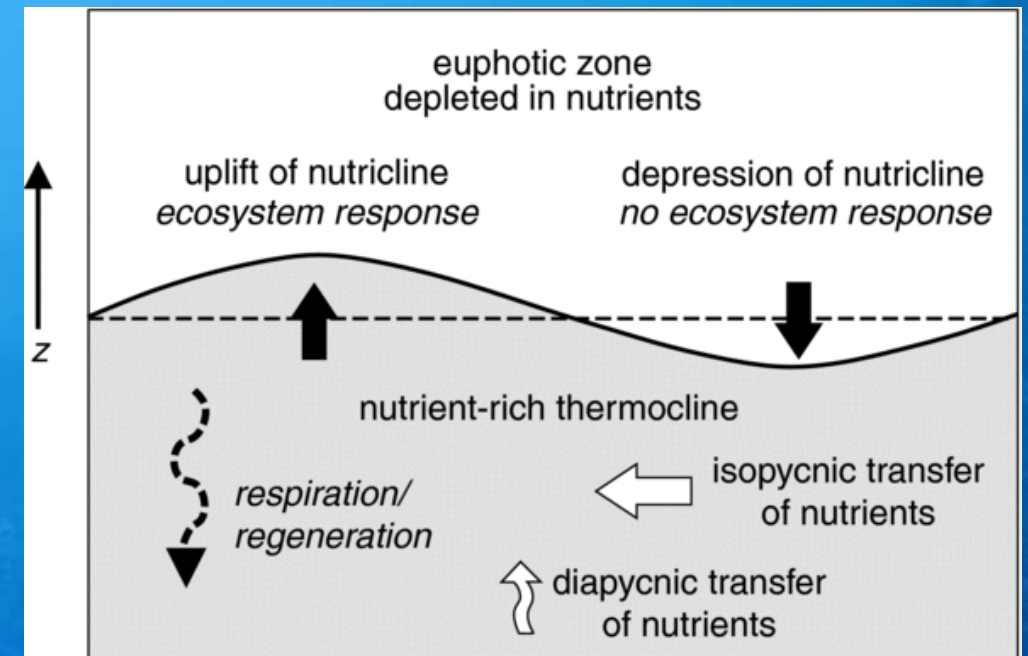


- CO₂ is highly soluble in cold high-lat waters
- Transported to deep ocean by convection and isopycnal mixing
- Dynamically-driven equatorial upwelling brings high-CO₂ water to surface
- Atmospheric transport closes the loop

Nutrient Cycling and the Marine Biological Pump

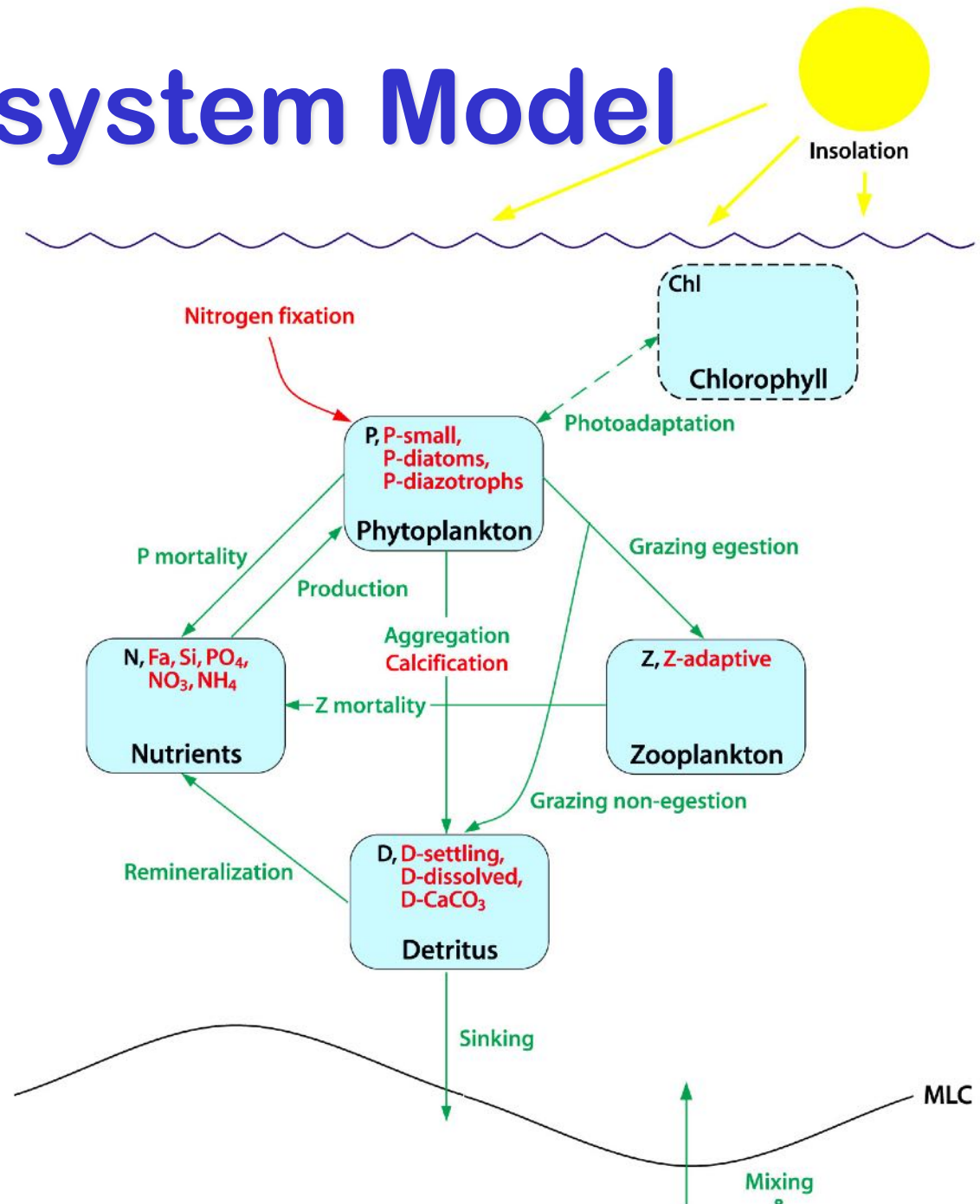


perturbed by wind



Marine Ecosystem Model

- Predict **PZND**, plus Chlorophyll
- Assume a single limiting “currency” (e.g., N) in each pool
- No interactions among individuals, just “pools”
- More recent models (red) include limitation by multiple nutrients, N-fixation, and size classes of organisms



Dark and Deep

- Brightly colored equipment, fish, and corals at snorkel depths (10 – 20 feet)
- Red and orange go first, then yellow and green
- Below 50 feet, everything is progressively dimmer shades of blue

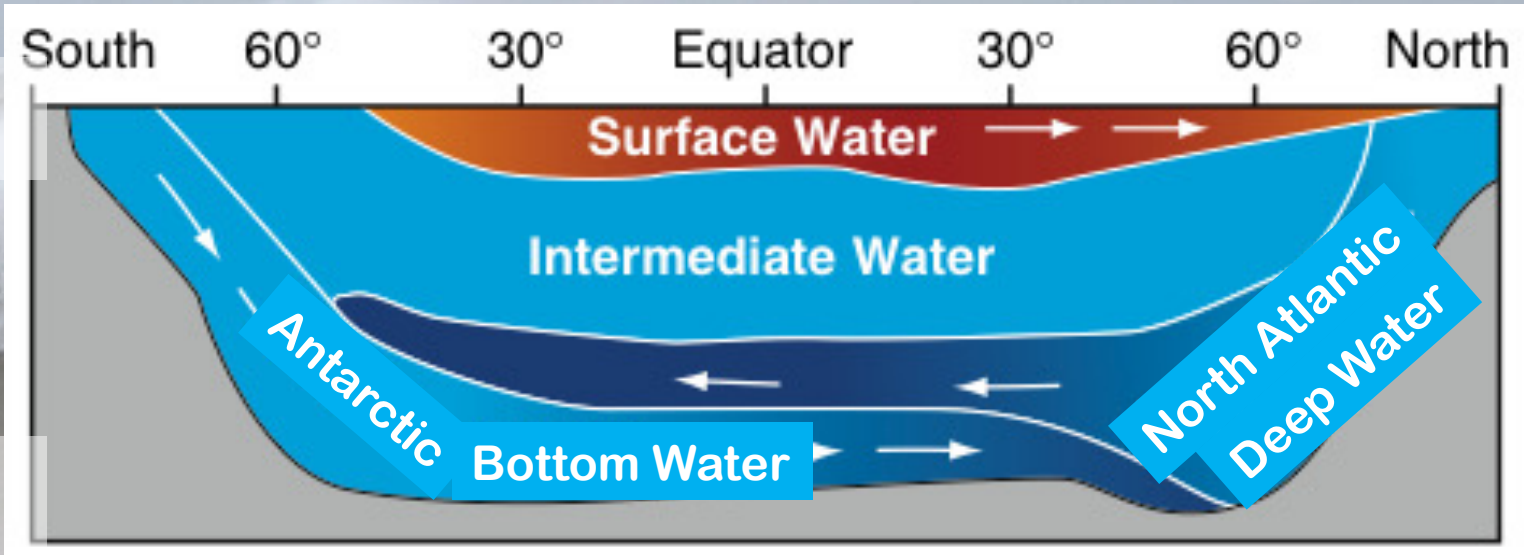
But the oceans are 13,000 feet deep!

really cold too!

Oceans Have Layers

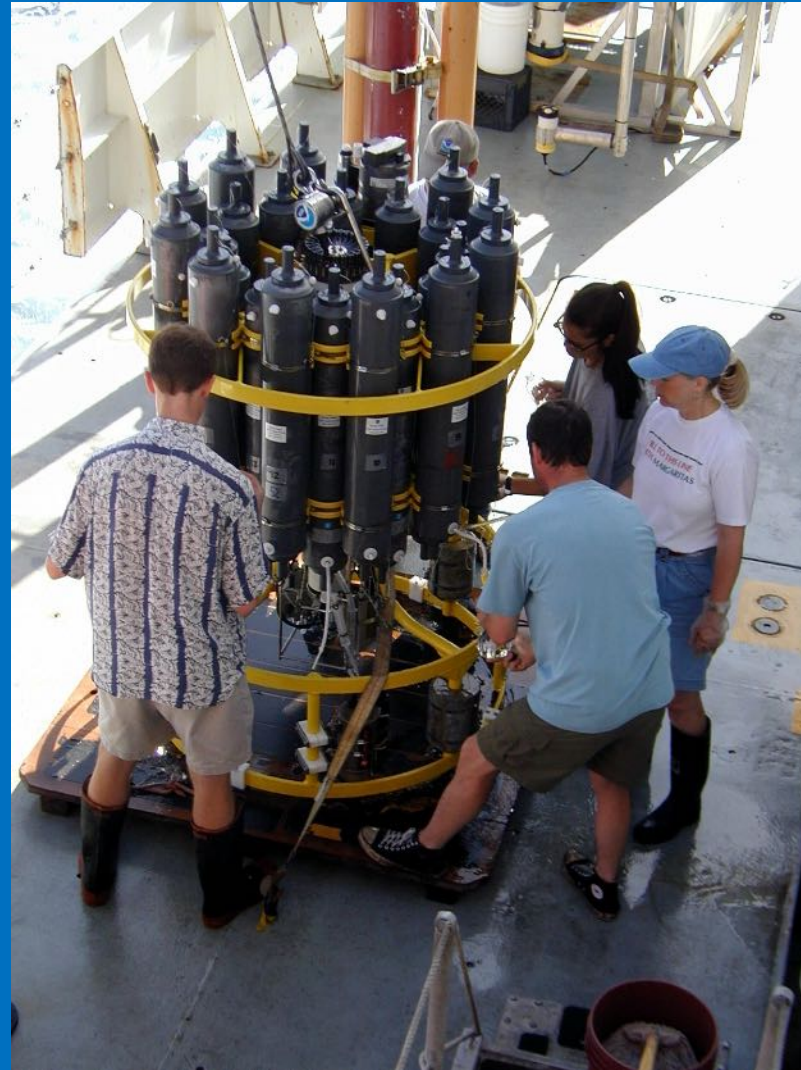
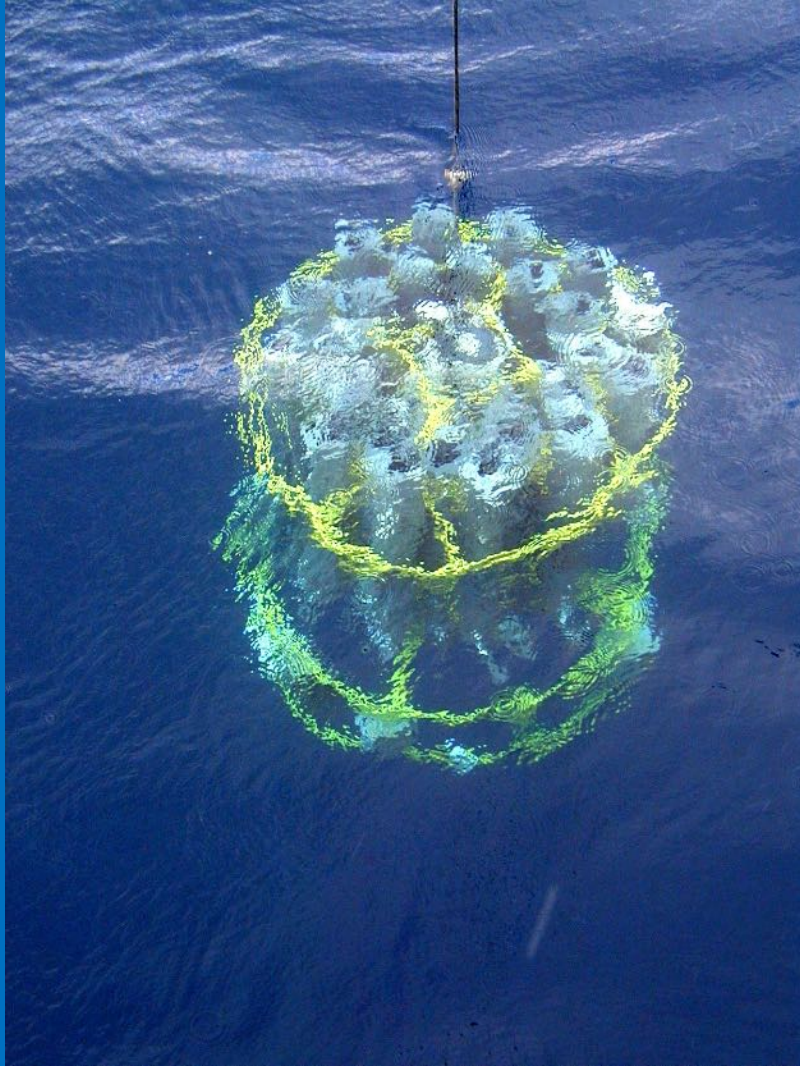
surface

4000 m

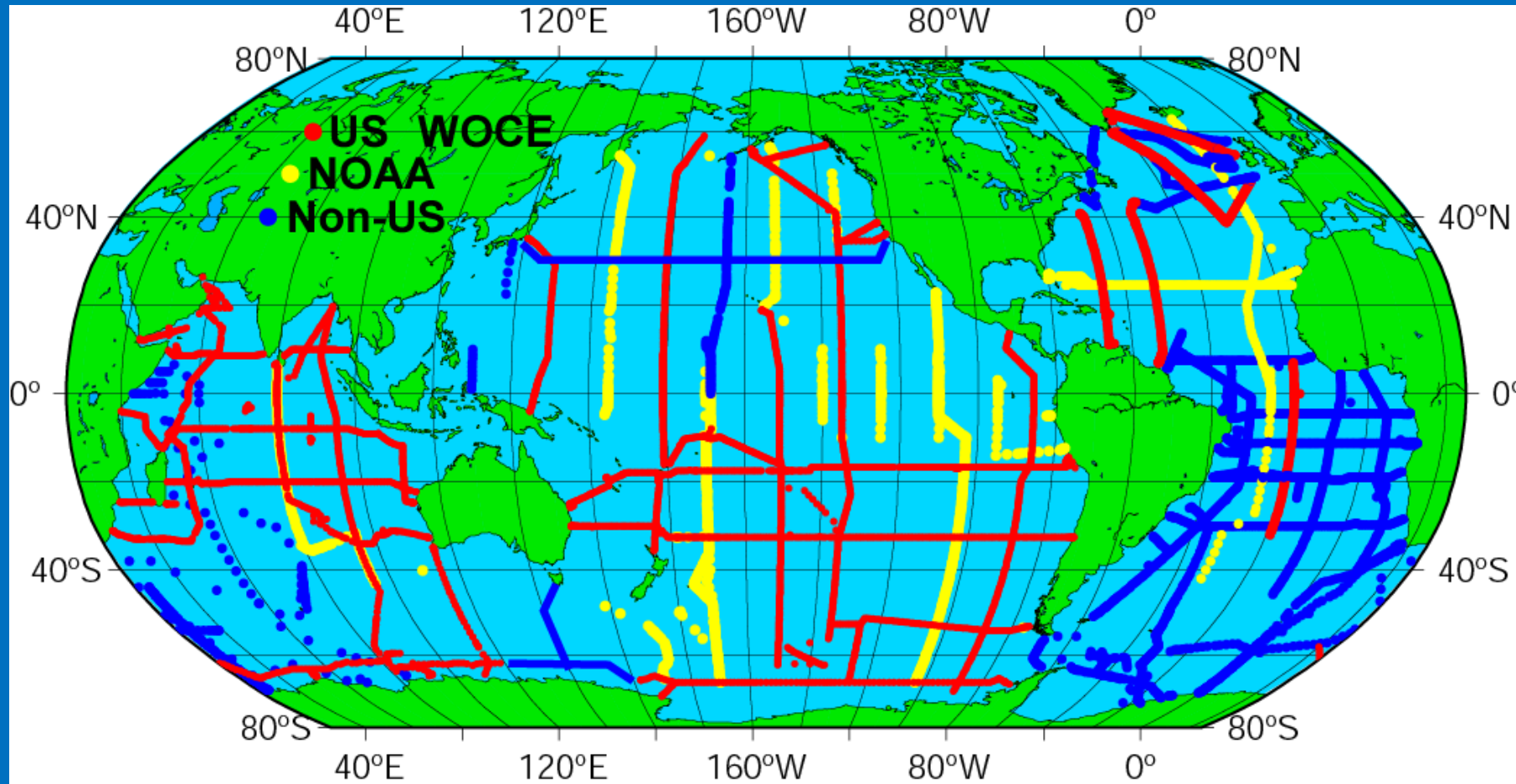


- Warm **buoyant “raft”** floats at surface
- Cold deep water is only “formed” at high latitudes
- Very stable, **hard to mix, takes ~ 1000 years!**
- Icy cold, inky black, most of the ocean **doesn't know we're here yet!**

Observing the Deep Ocean



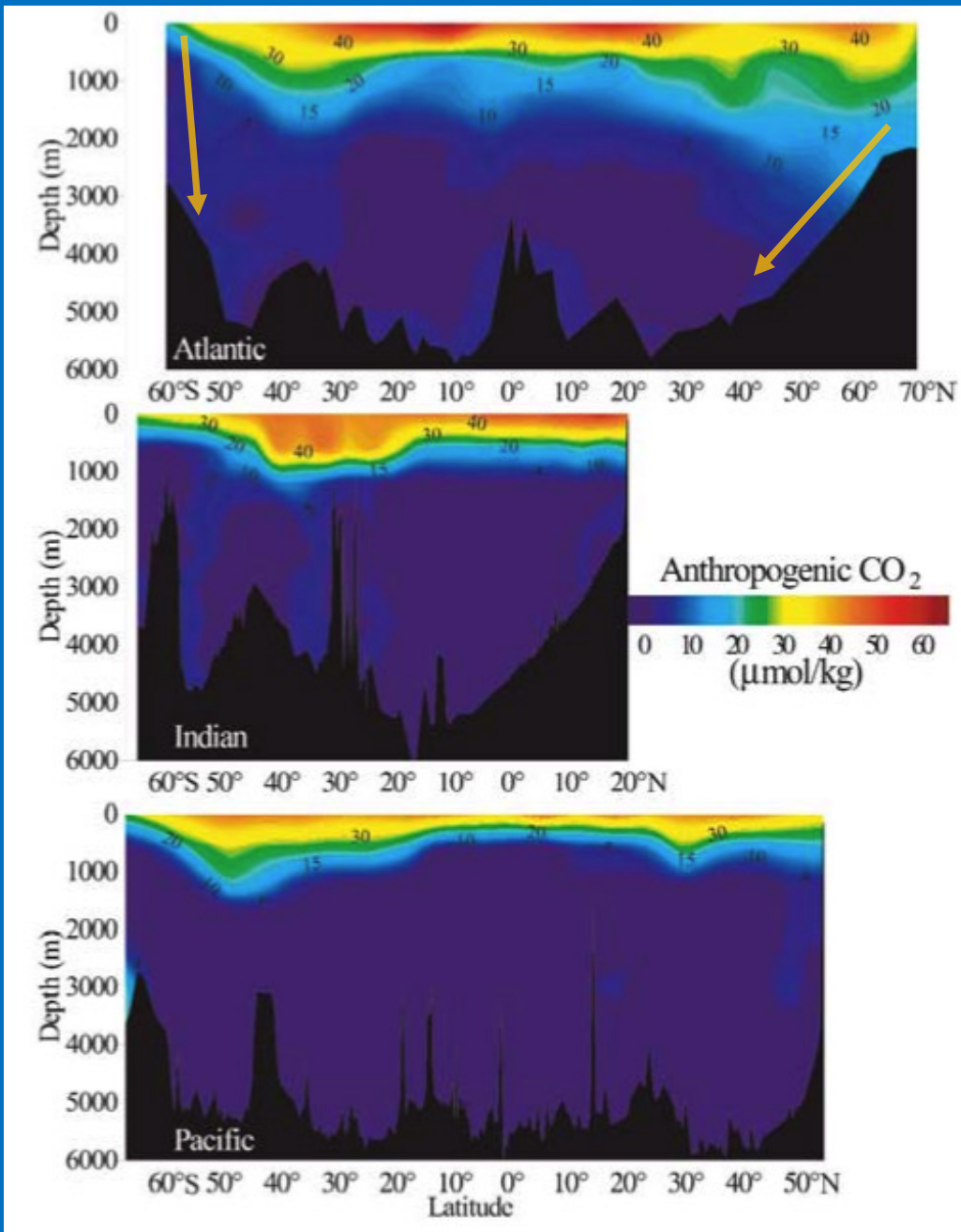
Observing the Deep Ocean



Global Ocean Survey Samples

Dissolved Fossil CO₂

- Millions of direct measurements of dissolved CO₂ in the oceans
- Fossil CO₂ remains trapped near the surface where warm water floats
- *Deep water doesn't know we're here yet!*





Planetary Titration



Where Has All the Carbon Gone?

- Into the **oceans**

- **Solubility** pump (CO₂ very soluble in cold water, but rates are limited by slow physical mixing)
- **Biological** pump (slow “rain” of organic debris)

- Into the **land**

- **CO₂** Fertilization (plants eat CO₂ ... is more better?)
- **Nutrient** fertilization (**N-deposition** and fertilizers)
- **Land-use** change (forest **regrowth**, fire suppression, woody encroachment ... but what about Wal-Mart's?)
- **Response to changing** climate (e.g., **Boreal warming**)

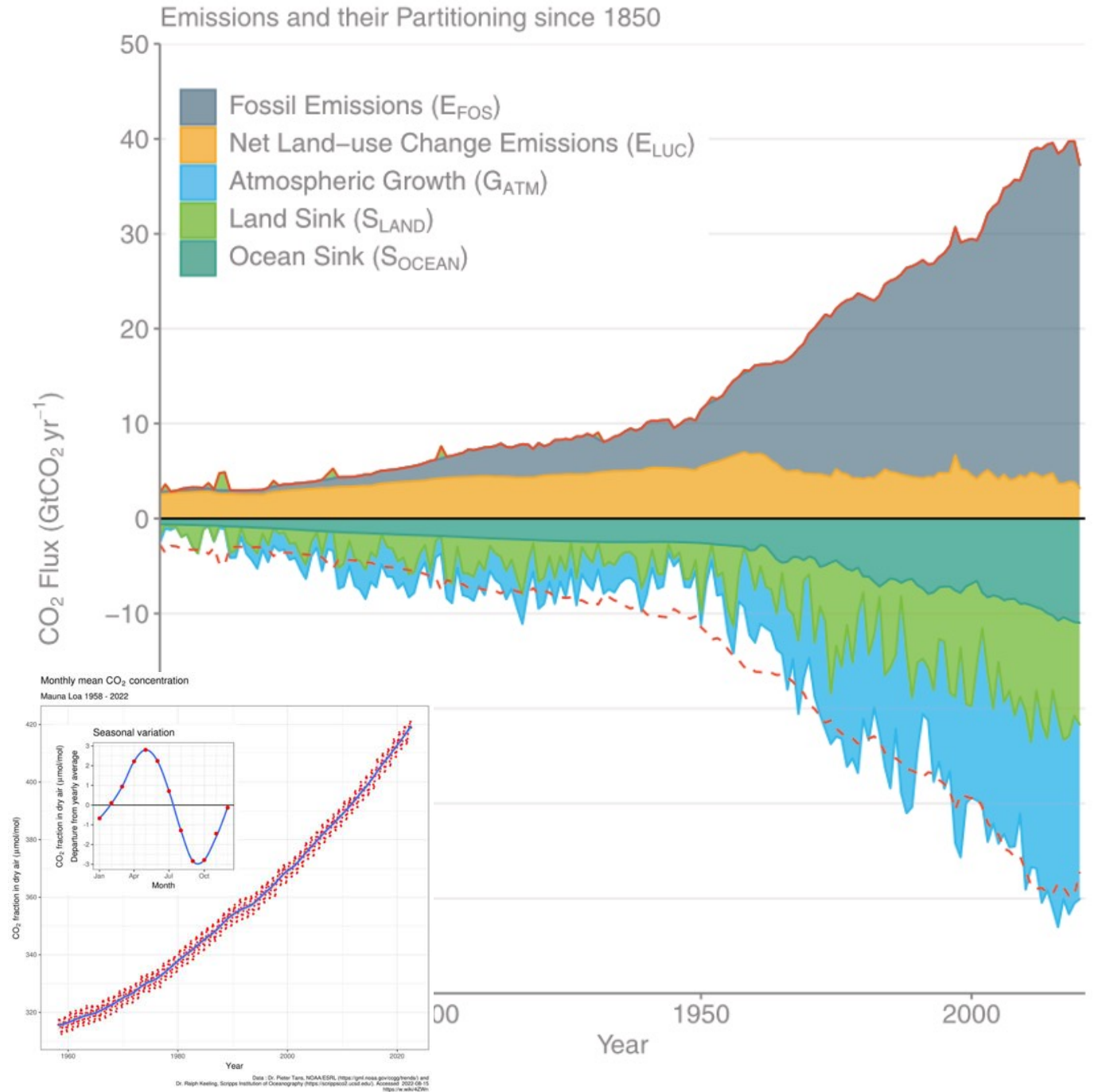


Sink Saturation

- Land – very vulnerable, very uncertain!
 - Only CO₂ fertilization has “legs”
 - N-deposition and Regrowth are transient
 - Boreal warming may switch to a huge source!
- Ocean – slow & safe for near-term, scary for the long term
 - Limited by rate of physical mixing into deep ocean against buoyancy
 - As surface water warms, mixing will slow
 - Thousands of years to reach equilibrium!
 - Acidification chemistry limits total uptake

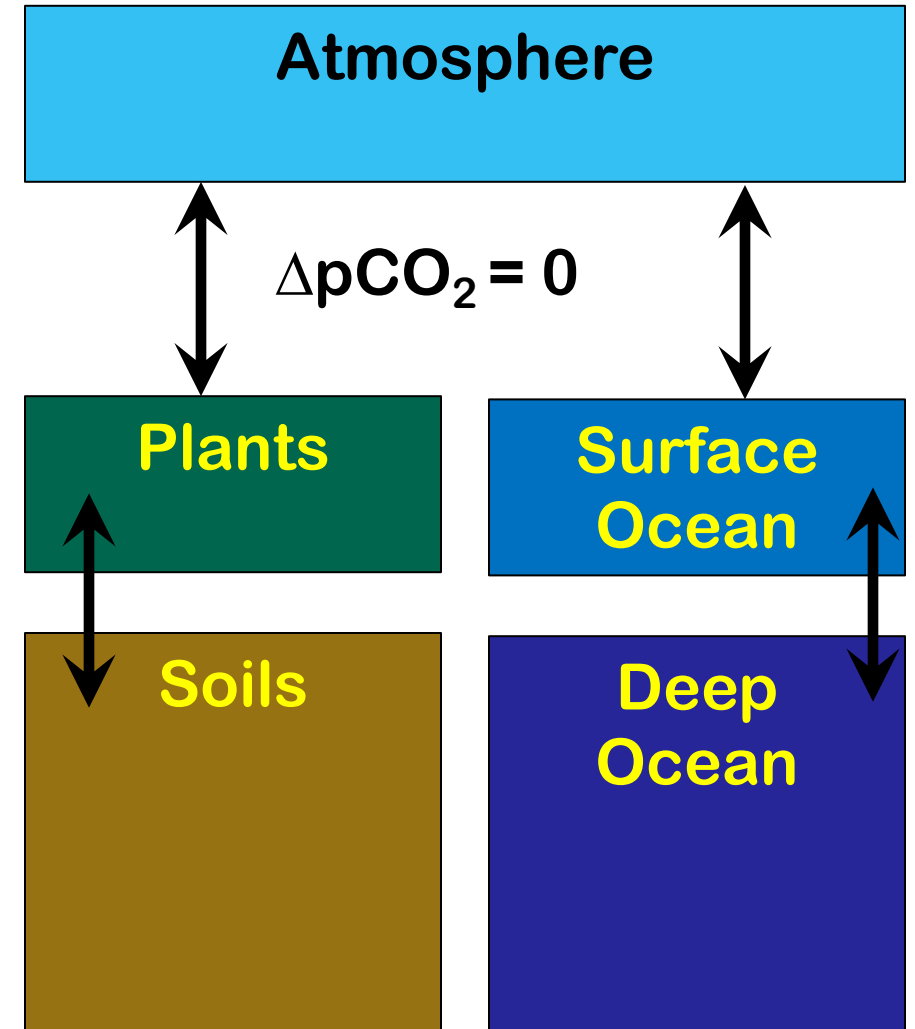
For Our Whole Lives

- CO2 has been increasing
- Growth has exceeded decomposition
- What will happen as emissions fall and CO2 stabilizes or decreases?



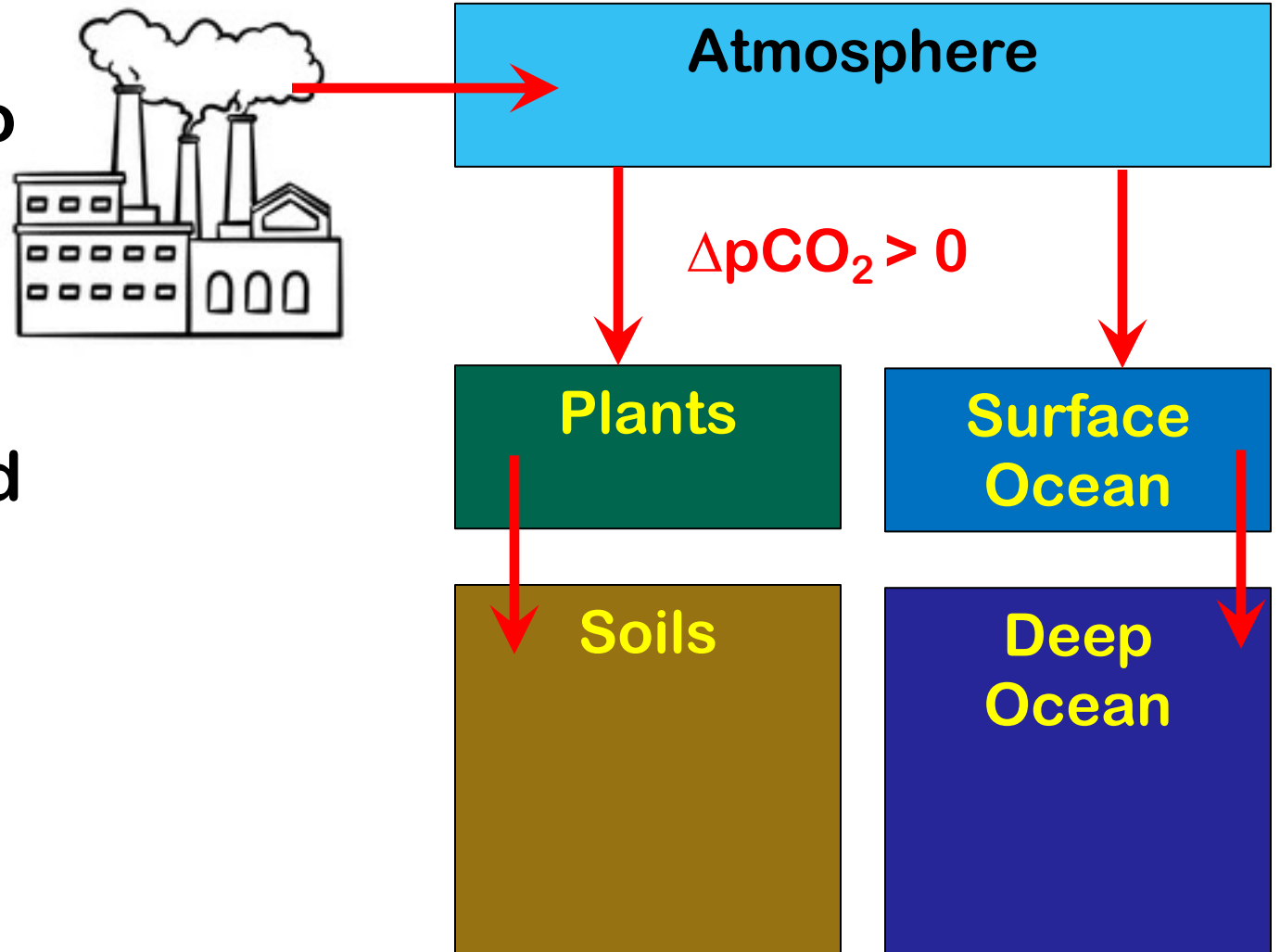
Simple Conceptual Model

- Preindustrial equilibrium:
Historically, there were no carbon sinks



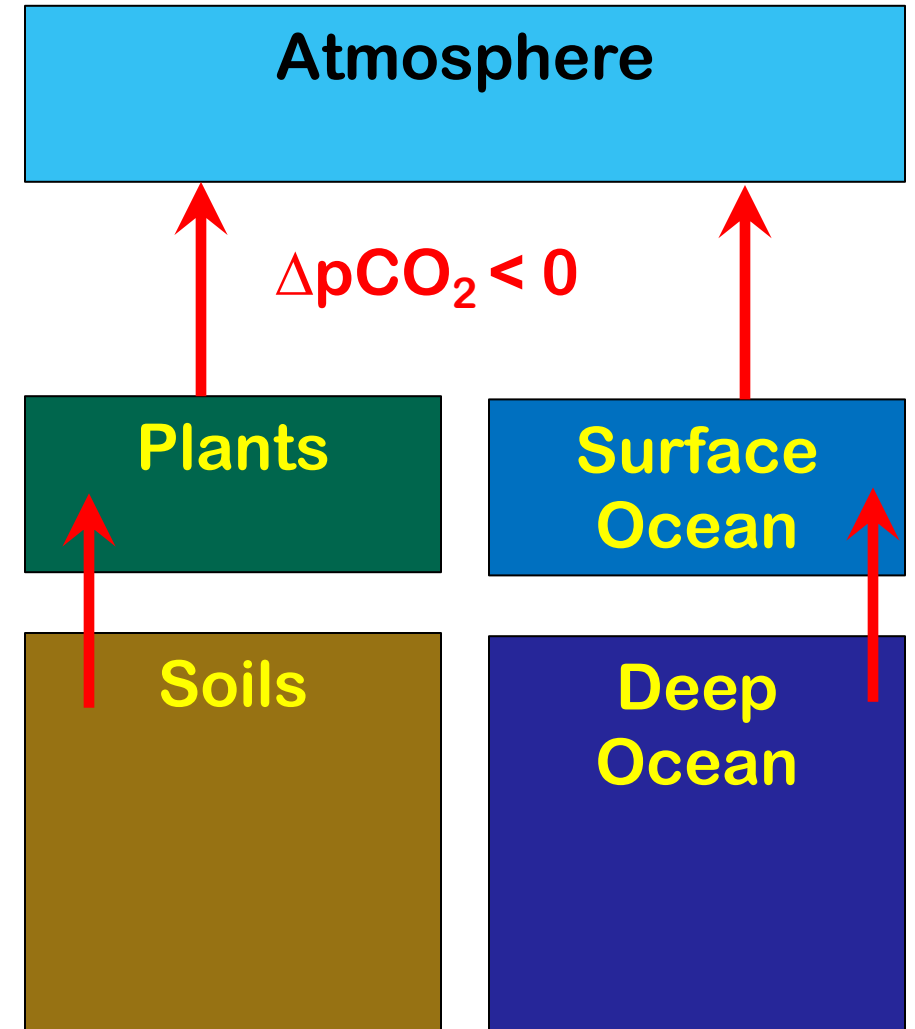
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- As atmospheric CO₂ increased, carbon flowed into the surface ocean and land ecosystems



Simple Conceptual Model

- Preindustrial equilibrium: Historically, there were no carbon sinks
- As atmospheric CO₂ increased, carbon flowed into the surface ocean and land ecosystems
- As emissions slow and cease, $\Delta p\text{CO}_2$ will fall
- If/when emissions reverse, so will the sinks



Transient Climate Response to Emissions

“Definition”

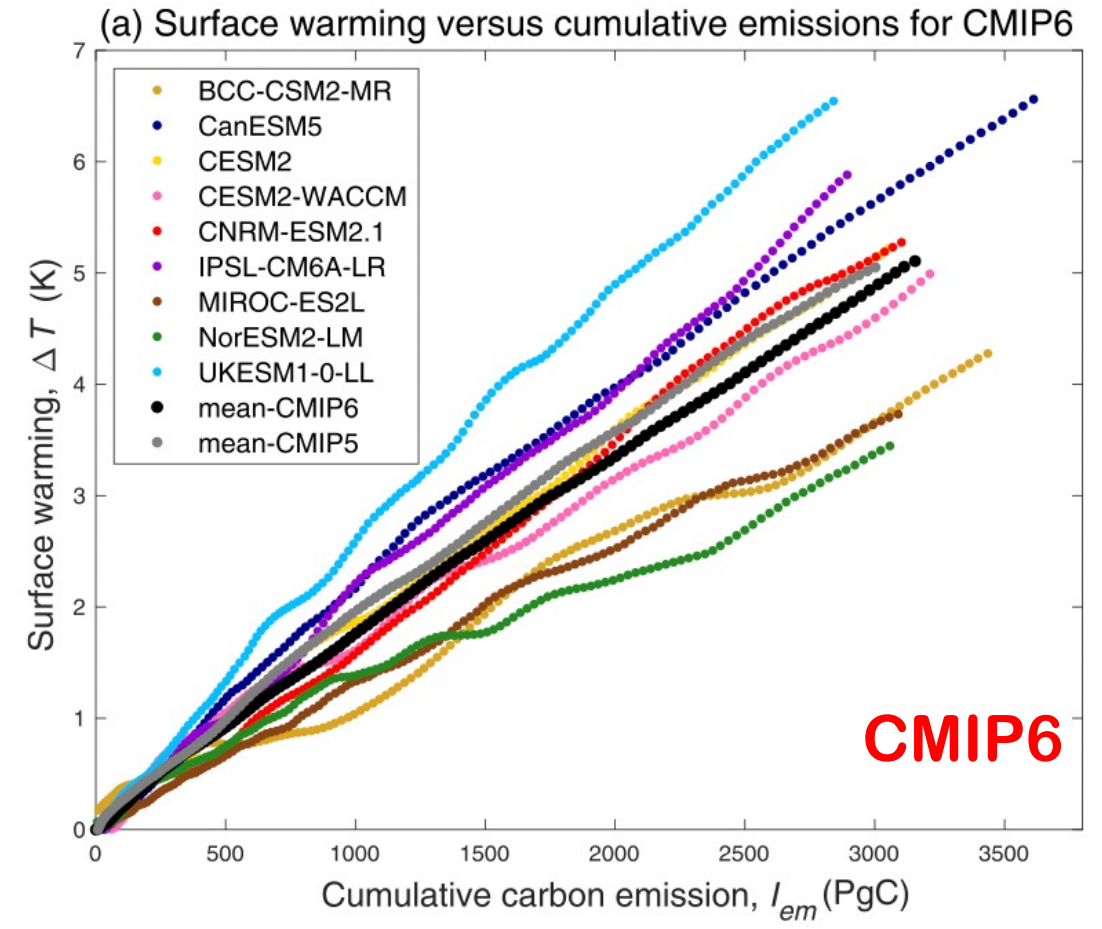
$$\Lambda = \frac{\Delta T}{E} = \frac{\Delta T}{\Delta C_a} \times \frac{\Delta C_a}{E}$$

↑ TCRE

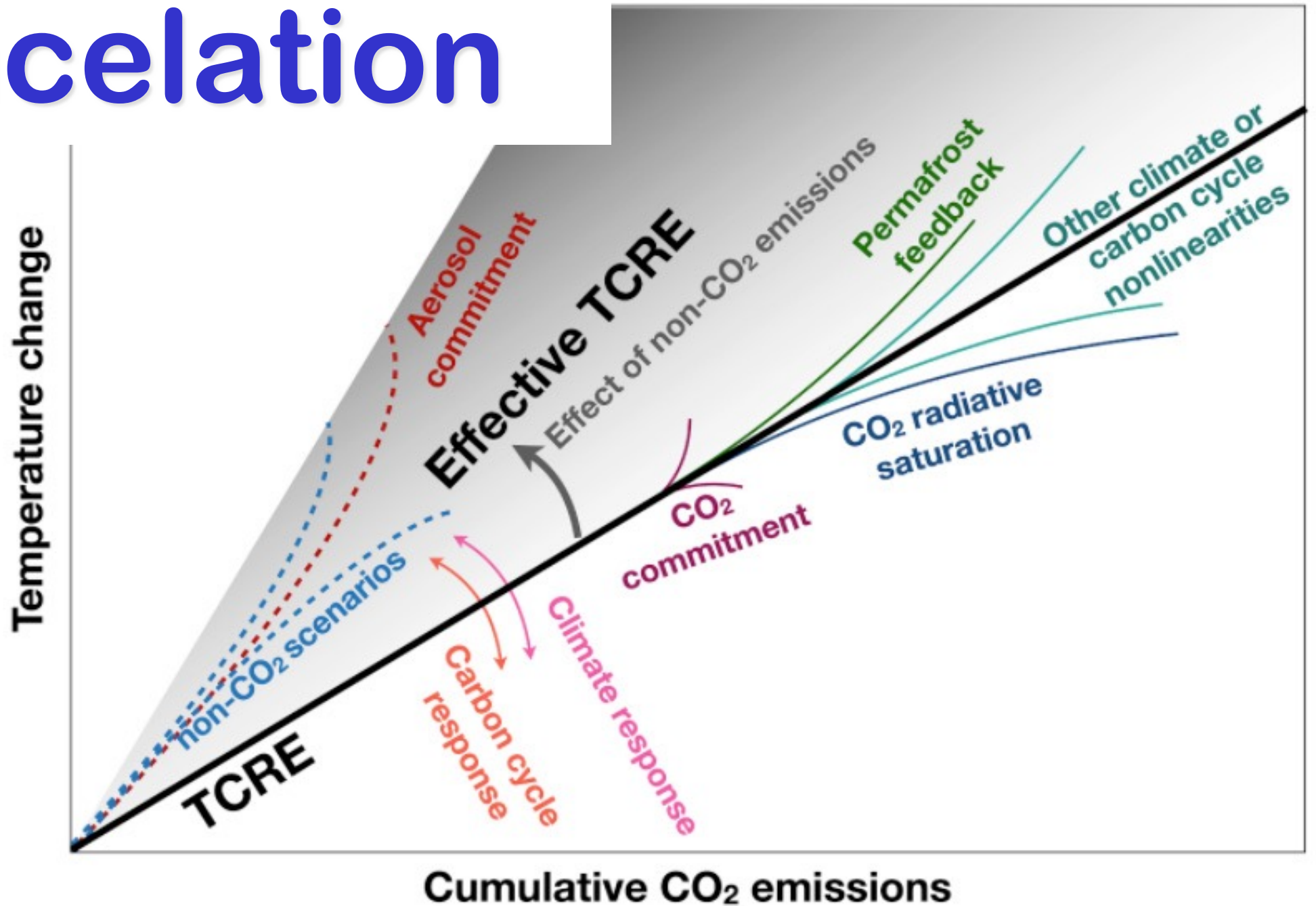
warming

CO₂ increment

cumulative emissions



Cancellation



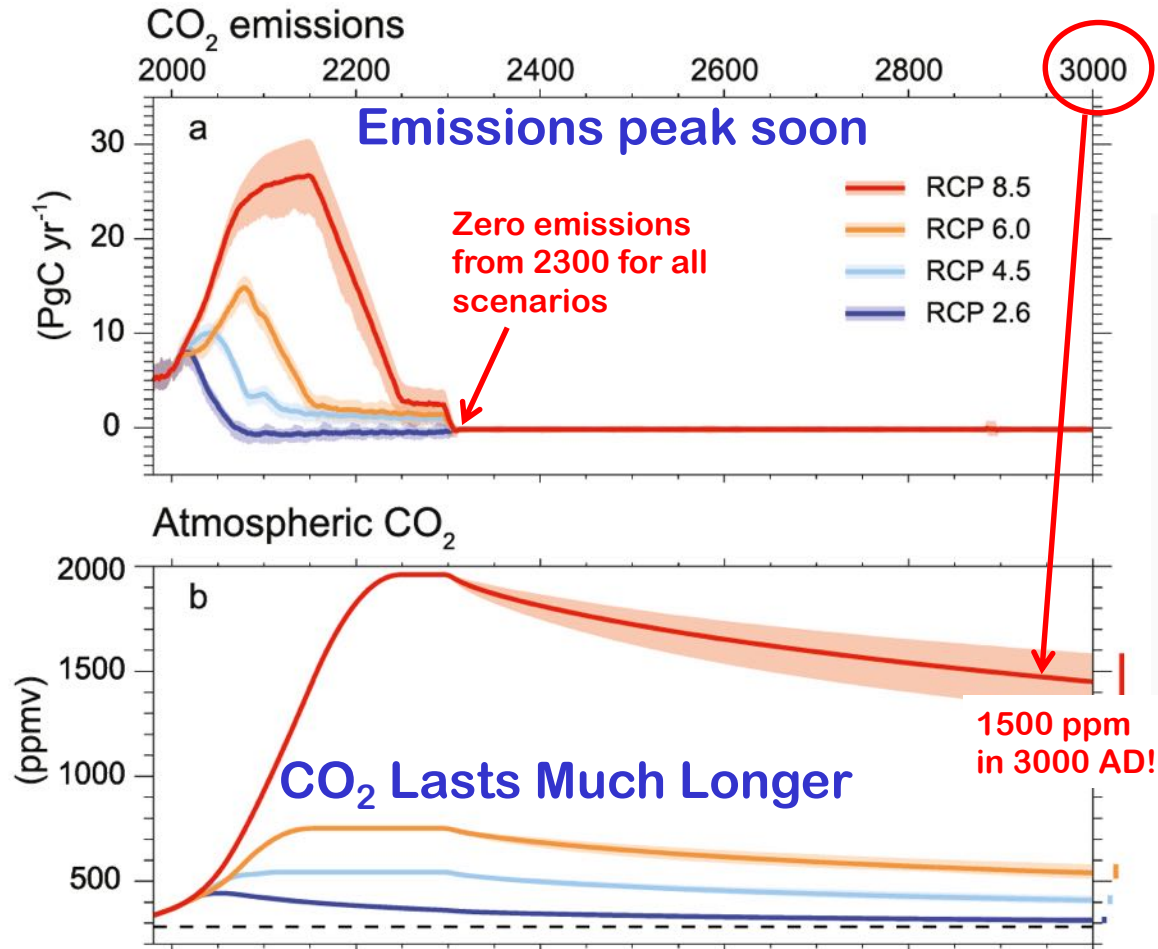
Implications of TCRE

- Every kg of carbon ever burned in all of history warms climate by the same amount
- When emissions stop, warming will stop almost immediately
- Warming is essentially permanent (without negative emissions)
- Negative emissions will only be about 50% effective



One-Way Warming

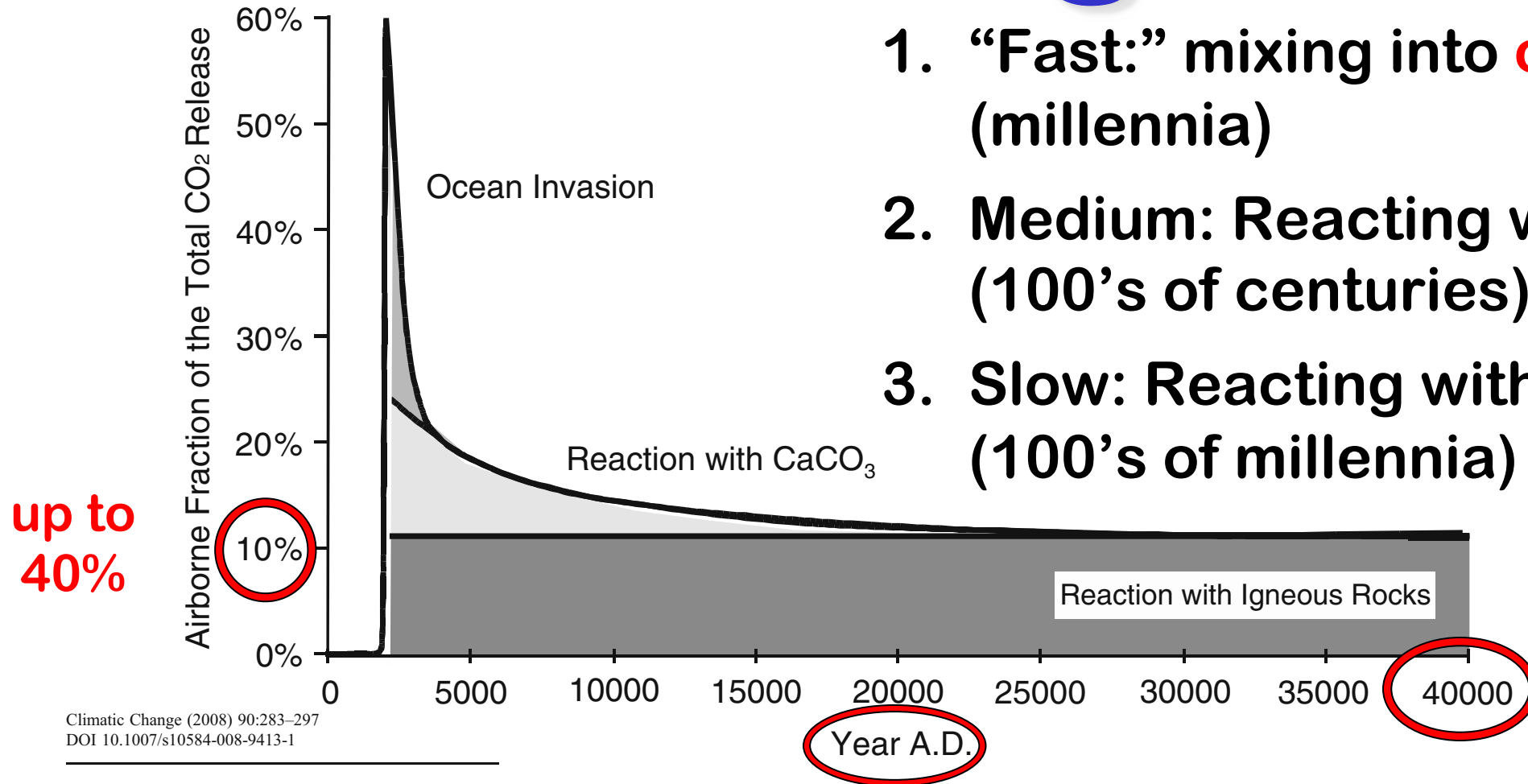
- Heating continues until we stop burning carbon
- After we stop burning coal, oil, & gas the **CO₂ will stay in the air**
- Climate will remain hot for **thousands of years**



Thermostat only turns one way!

The Long Tail

1. “Fast:” mixing into **oceans** (millennia)
2. Medium: Reacting w/**seashells** (100’s of centuries)
3. Slow: Reacting with **rocks** (100’s of millennia)



The millennial atmospheric lifetime of anthropogenic CO_2

David Archer • Victor Brovkin

Some of the CO_2 we emit today will still be warming the climate 100,000 years from now!